

Kinematics and Kinetics

- Kinematics
 - The study of motion without concern of what forces cause the motion, first step in the analysis or design of a mechanism
- Kinetics
 - The study of forces on systems in motion
- Design requires the knowledge both
- Dynamics
 - Combination of kinematics and kinetics
- However, first must know the acceleration before applying Newton's 2nd Law (F=ma)

- Designs require some finite service life, with this in mind the following must be taken into consideration:
 - The stresses on the system must be within some allowable range
 - The maximum forces on the system must be within some allowable range
 - The acceleration must be known
- How do we accomplish this? Kinematics

Mechanism and Machine

Mechanism

- A device that transforms motion into some desirable pattern and typically develops very low forces and transmits very little power
- Combination of rigid or resilient bodies joined together to provide a specific absolute motion

Machine

- Contains mechanisms which are designed to provide significant forces and transmit significant power
- Mechanism capable of performing useful work or capable of transmitting significant forces

Degrees of Freedom (DOF)

- Number of independent parameters (coordinates)
 which are needed to uniquely define position in space
 at any instant in time
 - In a 3-D frame: x, y, z, θ, ϕ , ρ
- Rigid body: essentially nondeformable
 - Assume: rigid & massless
- Types of motion

Rotation + Translation = Complex Motion

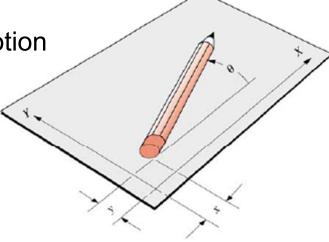
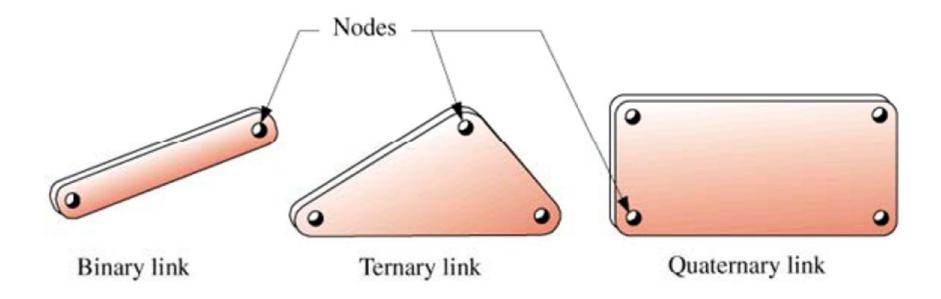


FIGURE 2-1

A rigid body in a plane has three DOF

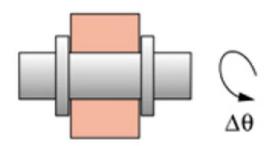
Links, Joints and Kinematic Chains

- Link: rigid or flexible members have at least two nodes (points of attachment)
- Linkage: basic building block of all mechanisms
- Links of different order

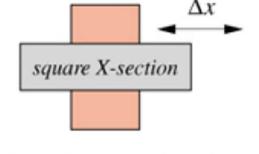


Six Lower Pairs

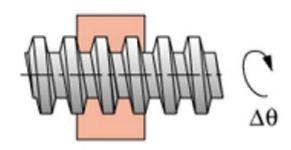
 Joint: connection between two or more links (at their nodes), which allows some motion between the links



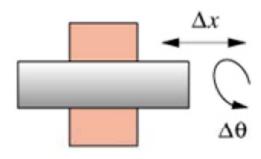
Revolute (R) joint-1 DOF



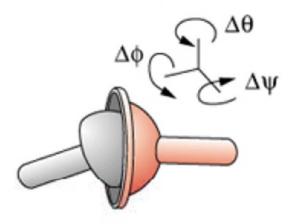
Prismatic (P) joint-1 DOF



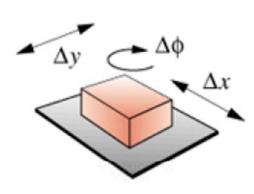
Helical (H) joint-1 DOF



Cylindric (C) joint—2 DOF



Spherical (S) joint-3 DOF

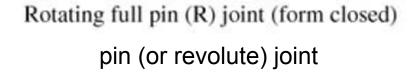


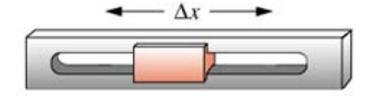
Planar (F) joint—3 DOF

Joint (1)

- Joints are classified into several ways:
 - Number of DOF allowed at a joint
 - By type of contact
 - By type of physical closure (Force or Form closed)
 - Number of links (order of joint)
- Full joints: 1 DOF



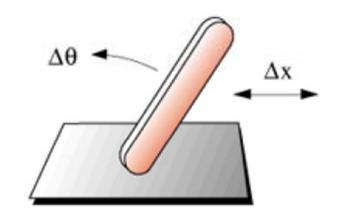




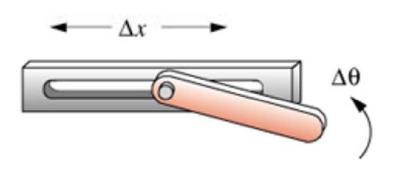
Translating full slider (P) joint (form closed)
sliding (or prismatic) joint

Joint (2)

• Half (or RP, Roll-Slide) joints: 2 DOF



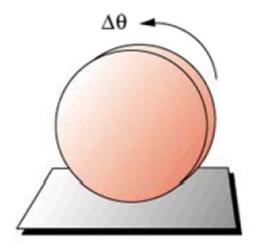
Link against plane (force closed)

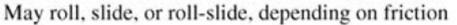


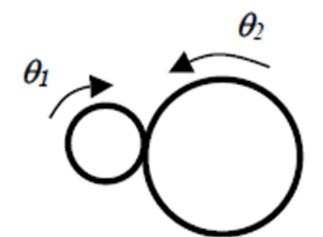
Pin in slot (form closed)

Joint (3)

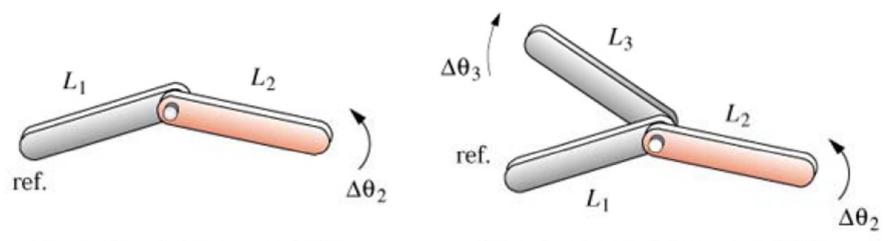
- Rolling joint: 1 or 2 DOF (may roll, slide, or roll-slide depending on friction)
 - Pure-roll (R), pure-slide (P), roll-slide (RP)







Order = (number of links joined) – 1



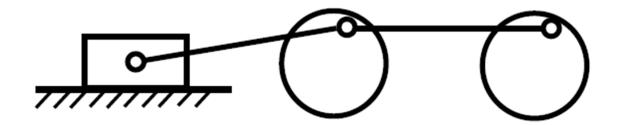
First order pin joint - one DOF (two links joined)

Second order pin joint - two DOF (three links joined)

- Links are combined using joints to form kinematic chain or just linkage
- Linkage without at least one link fixed → mechanism

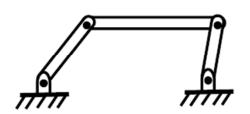
Planar Motion

- Rectilinear translation
 - Points in the body move in parallel straight lines
- Curvilinear translation
 - Points in the body move along identical curves
 - Link does not rotate wi.r.t. the ground
- Rotation
 - Points in the body rotate about a single point, which is usually fixed to the ground
- General planar motion
 - General combination of rotation and translation

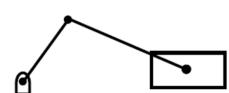


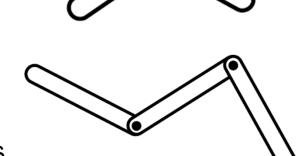
Linkage Classification by Number of Links

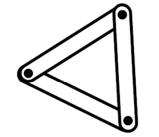
- Two links with one joint (dyad)
- Three links (triad)
- Four links (four-bar mechanism)
 - Joined by 4 pin-joints
 - Slider joint replaces one of the pin joints

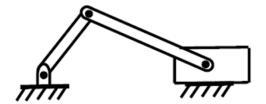


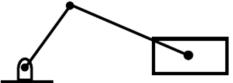












Kinematic chain

 An assemblage of links and joints to provide a controlled output motion in response to a supplied input motion

Crank

A link which makes a complete revolution and is pivoted to ground

Rocker

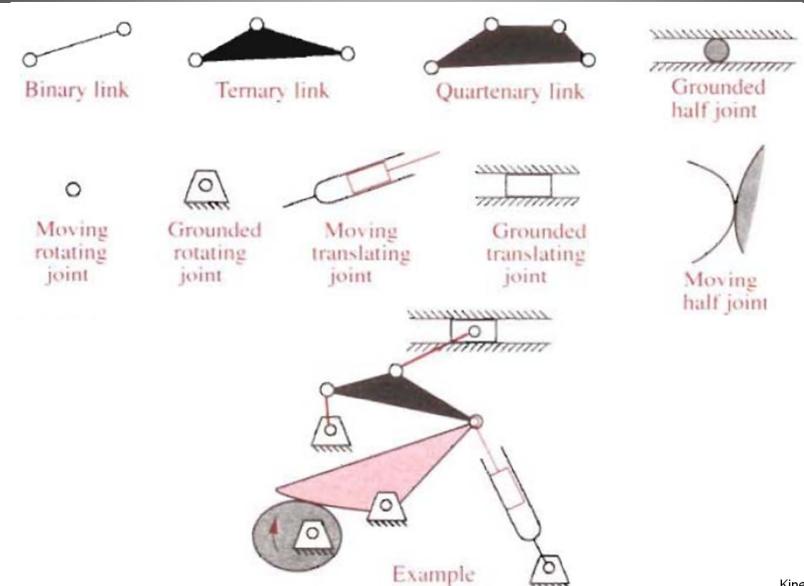
- A link which has an oscillatory rotation and is pivoted to ground
- Coupler (aka Connecting Rod)
 - Has a complex motion and is not pivoted to ground

Ground

- Any link that is fixed w.r.t. the reference frame
- Note: reference frame may be in motion

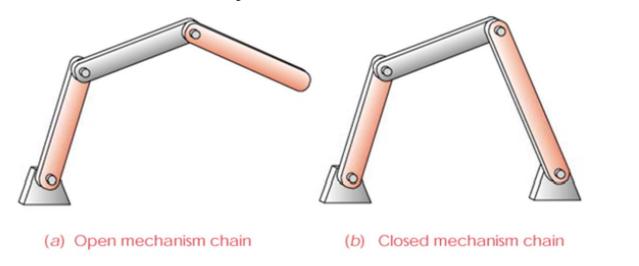


Drawing Kinematic Diagrams



Determining DOF (1)

Kinematic chains may be either OPEN or CLOSED



- Dyad
 - An open kinematic chain of two binary links and one joint

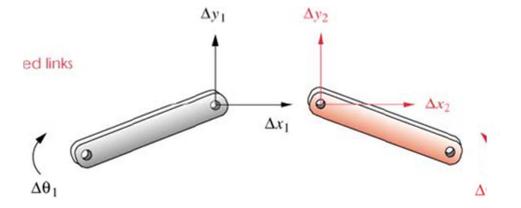


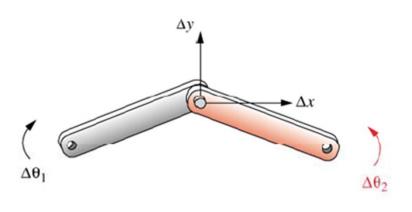
Determining DOF (2)

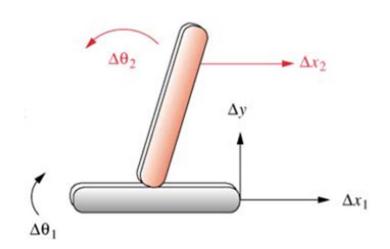
- To determine the overall DOF
 - Account for number of links and joints and their interactions
- Any free link on a plane has 3 DOF: Δx, Δy, Δθ
- Gruebler's Equation
 - DOF = 3L 2J 3G
 - L: number of links
 - J: number of joints
 - G: number of ground
 - As there is always only one ground plane, G=1 always
 - DOF = 3(L 1) 2J
 - Note: J=1/2 for half joints because a half joint only removes one DOF

Determining DOF (3)

- Kutzbach's modification
 - $DOF = 3(L 1) 2J_1 J_2$
 - L: number of links
 - J₁: number of full joints
 - J₂: number of half joints

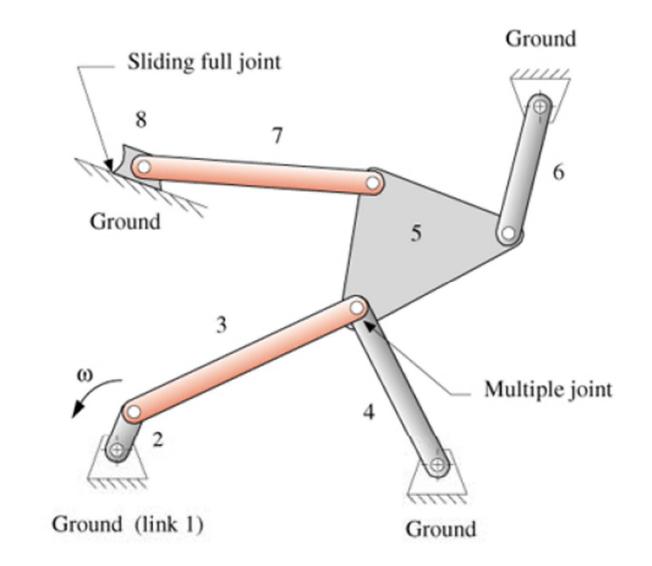




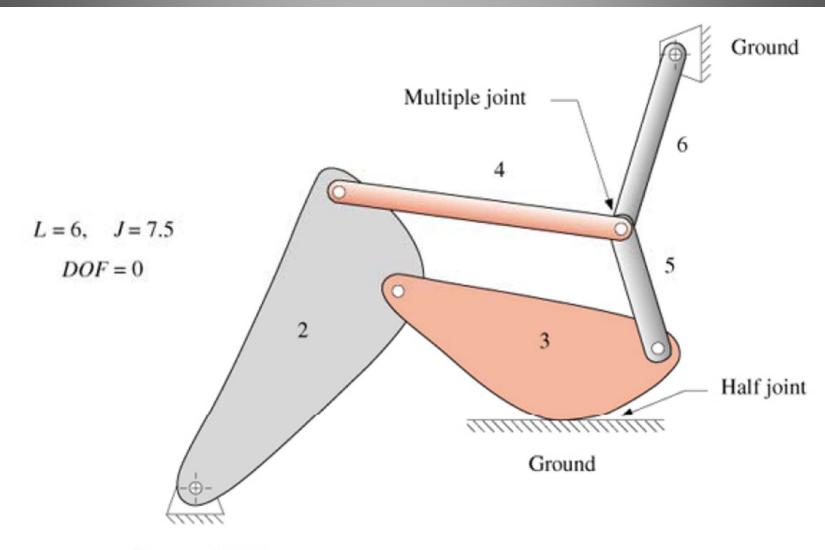


Determining DOF (4)

Name (Symbol)	DOF	OF Contains	
Revolute (R)	1	R	
Prismatic (P)	1	Р	
Helical (H)	1	RP	
Cylindric (C)	2	RP	
Spherical (S)	3	KKK	
Planar (F)	3	RPP	

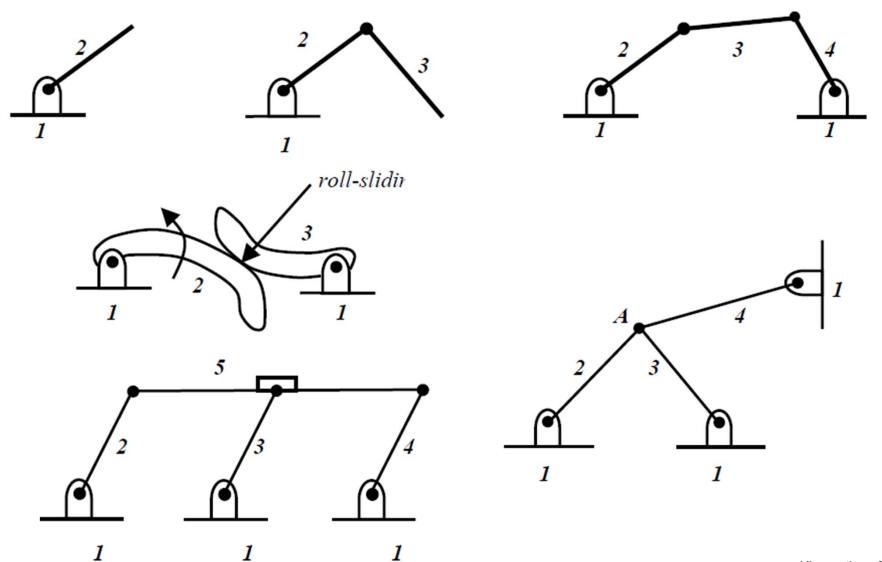


Determining DOF (5)



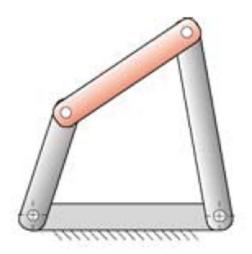
Ground (link 1)

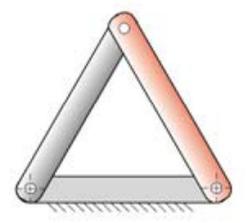
Calculation of Mobility

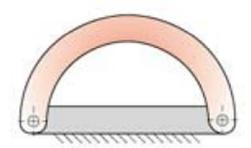


Mechanisms and Structures

- Mechanism: DOF > 0 → possible motion
- Structure: DOF = $0 \rightarrow$ no motion possible
- Preloaded structure: DOF < 0 → no motion and possible stresses

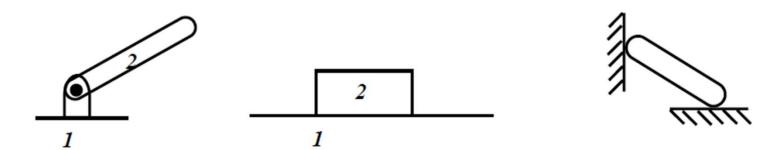






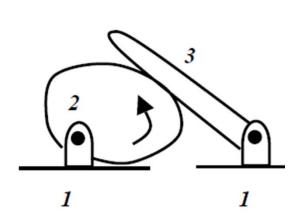
Simple Mechanisms (1)

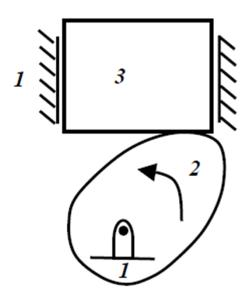
• 2 links: [3*(2-1)-2*1=1] by adding a single pin or slider joint



• 3 links: [3*(3-1)-2*1-1=1] by adding two pins and a roll-

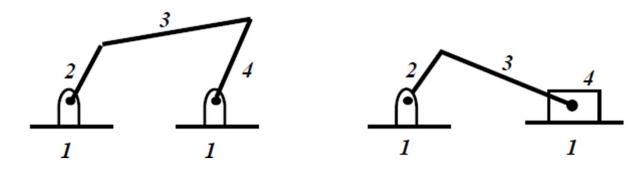
slider joint





Simple Mechanisms (2)

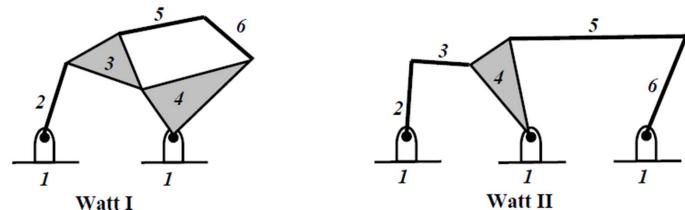
• 4 bars + 4 pins: 4-bar mechanism [3*(4-1)-2*4=1]



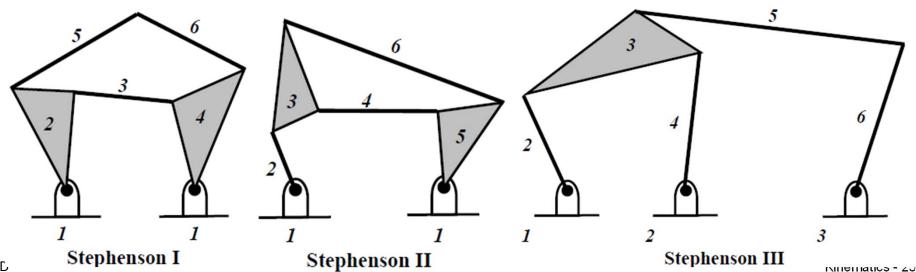
- 5 links + pin or slider joints: not possible
- 6-bar linkage: [3*(6-1)-2*7=1]
 - 6 binary links? 6 pin joints (x)
 - 2 ternary (adjacent) + 4 binary links : Watt linkage
 - 2 ternary (separate) + 4 binary links : Stephenson linkage

Simple Mechanisms (3)

Watt six-bar mechanism



• Stephenson six-bar mechanism



Number Synthesis

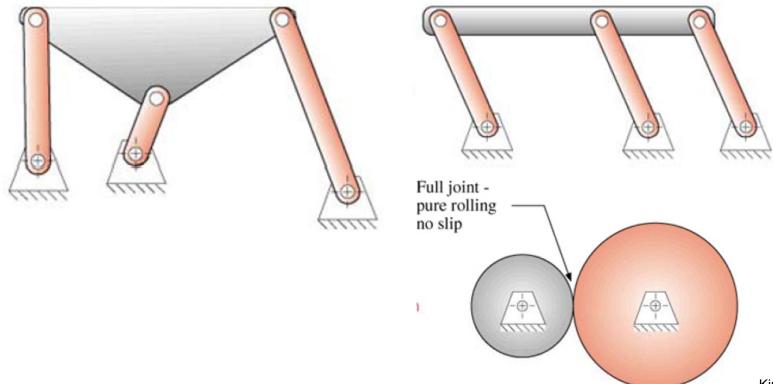
- The determination of the number and order of links and joints necessary to produce motion of a particular DOF
 - Gives all possible combinations of linkage combinations from which to choose
- Order: number of nodes per link
 - Binary, ternary, quaternary
- Example: drive all possible link combinations for one DOF for sets ≤ 8 links and link orders ≤ 6
 - Assume only full rotating joints

TABLE 2-2 1-DOF Planar Mechanisms with Revolute Joints and Up to 8 Links

Total Links					
IOGITURKS	Binary	Temary	Quatemary	Pentagonal	Hexagonal
4	4	0	0	0	0
6	4	2	0	0	0
6	5	0	1	0	0
8	7	0	0	0	1
8	4	4	0	0	0
8	5	2	1	0	0
8	6	О	2	О	0
8	6	1	0	1	0

Paradoxes

- Gruebler Equation ignores link sizes and shapes
 - It can give misleading conclusions for unique geometric configurations
 - Example: E-quintet

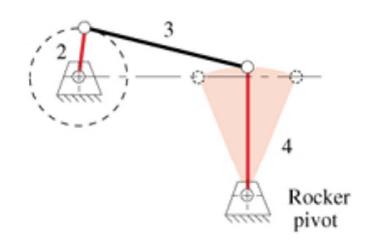


Linkage Transformation (1)

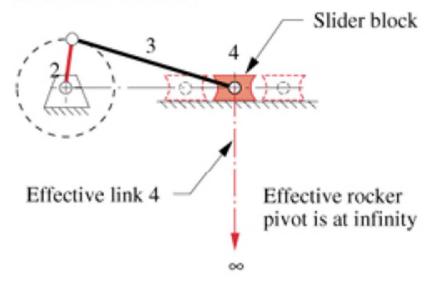
- [1] Any full rotating joint can be replaced by a sliding full joint with no change in DOF of the mechanism
- [2] Any full joint can be replaced by a half joint, but this will increase DOF by 1
- [3] Removal of a link will reduce DOF by 1
- [4] The combination of [2] and [3] will keep the original DOF unchanged
- [5] Any ternary or higher order link can be partially 'shrunk' to a lower order link by coalescing nodes
 - Creation of a multiple joint, but will not change DOF
- [6] Complete shrinkage of a link is equivalent to its removal
 - Creation of a multiple joint and DOF will be reduced

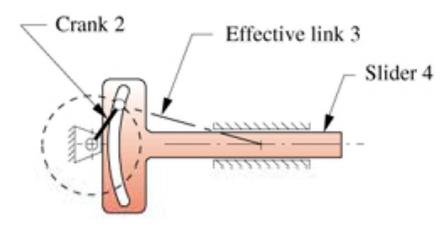
Linkage Transformation (2)

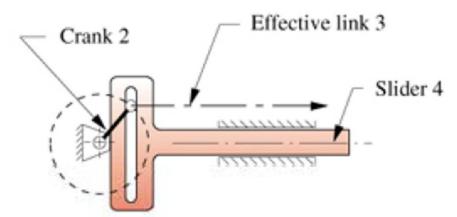
Grashof crank-rocker



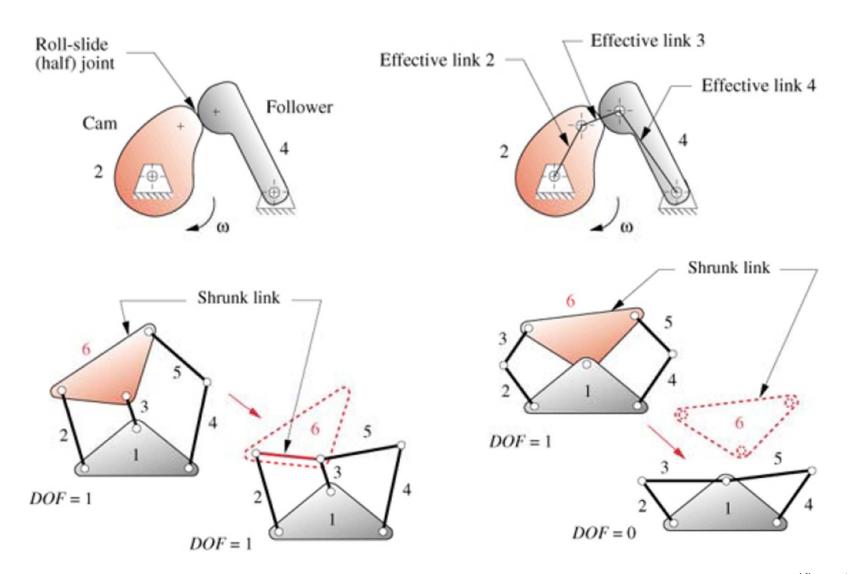
Grashof slider-crank





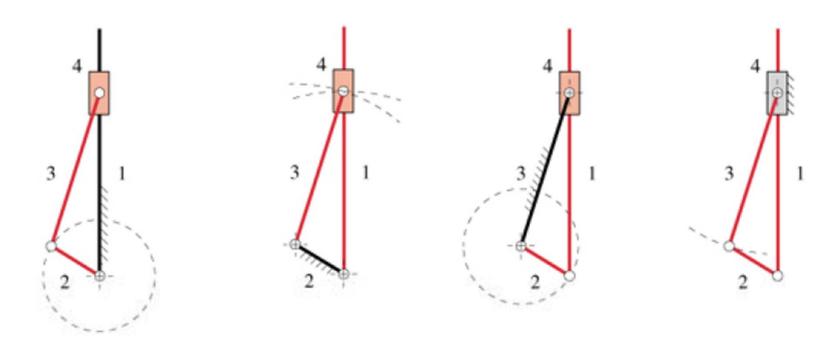


Linkage Transformation (3)



Inversion

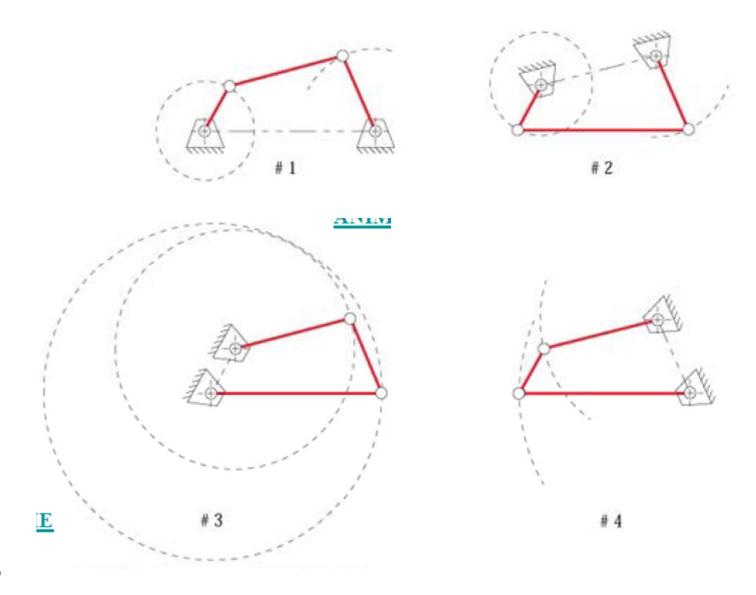
 An inversion is created by grounding a different link in the kinematic chain → there are as many inversions of a given linkage as there are links



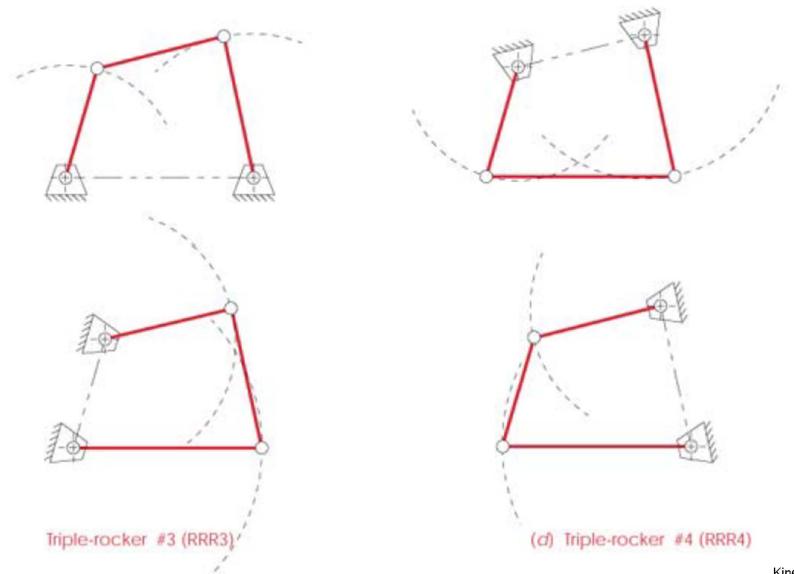
The Grashof Condition

- A Fourbar linkage is the simplest possible pin jointed mechanism for a 1 DOF controlled motion
- Grashof Condition is a simple relation which predicts the behavior of fourbar linkage inversions
 - S : length of shortest link
 - L : length of longest link
 - P : length of one remaining link
 - Q : length of other remaining link
 - If S + L ≤ P + Q, then the linkage is Grashof → At least one link will be capable of making full revolution w.r.t. the ground

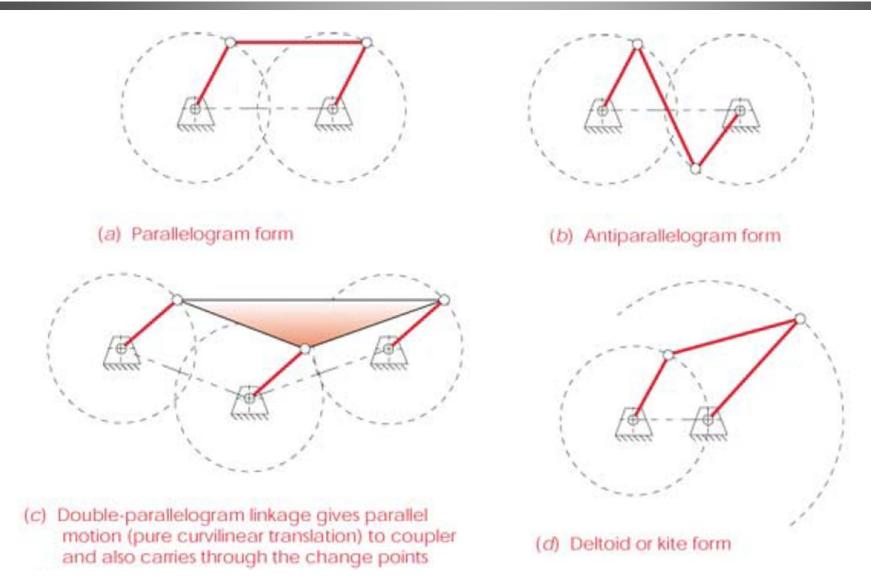
All Inversions of the Grashof Fourbar Linkage



All Inversions of the non-Grashof Fourbar Linkage



Special-case of Grashof Linkage



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