## 2.13 Hemisphere under point loads

REFERENCE	NAFEMS [2-3]
KEYWORDS	shell elements, solid elements, layered solid elements
MODEL FILENAME	Linearstatic13.nfxa

Figure 2.13.1 shows a quadrant of the hemispheric shell with inward and outward forces at point A and point C. Utilizing symmetric conditions, the quadrant model is discretized using shell, solid and layered solid elements. Single element in the thickness direction is used for meshes with solid and layered solid elements. Radial displacement at point A is determined. The reference solution is taken from the standard NAFEMS benchmarks.



Figure 2.13.1 Hemisphere quadrant model

Material data	Young's modulus	E = 68.25  GPa
	Poisson's ratio	V = 0.3
Section property	Thickness	t = 0.04 m

		$u_X^A$ [m]		
Reference		1.850×10 <sup>-1</sup>		
Number of elements per side		4	8	
Element type	TRIA-3	1.837×10 <sup>-1</sup>	1.850×10 <sup>-1</sup>	
	QUAD-4	1.089×10 <sup>-1</sup>	1.832×10 <sup>-1</sup>	
	TRIA-6	0.132×10 <sup>-2</sup>	0.703×10 <sup>-2</sup>	
	QUAD-8	1.480×10 <sup>-1</sup>	1.832×10 <sup>-1</sup>	

Table 2.13.1Displacement  $u_X$  at point A obtained using shell elements

Table 2.13.2 Displacement  $u_{\chi}$  at point A obtained using solid elements

		$u_X^A$	[ <i>m</i> ]
Reference		1.850×10 <sup>-1</sup>	
Number of elements per side		4	8
Element type	PENTA-6	9.426×10 <sup>-5</sup>	3.534×10 <sup>-4</sup>
	HEXA-8	9.962×10 <sup>-3</sup>	1.193×10 <sup>-1</sup>
	PENTA-15	7.708×10 <sup>-3</sup>	0.621×10 <sup>-1</sup>
	HEXA-20	1.234×10 <sup>-1</sup>	1.818×10 <sup>-1</sup>

Table 2.13.3	Displacement	$u_x$ at point A obtained using layered solid elements
--------------	--------------	--

		$u_X^A$ [m]	
Reference		1.850×10 <sup>-1</sup>	
Number of elements per side		4	8
Element type	PENTAL-6	0.165×10 <sup>-1</sup>	1.005×10 <sup>-1</sup>
	HEXAL-8	1.016×10 <sup>-1</sup>	1.786×10 <sup>-1</sup>
	PENTAL-15	7.708×10 <sup>-3</sup>	0.621×10 <sup>-1</sup>
	HEXAL-20	2.435×10 <sup>-3</sup> 1.203×10 <sup>-1</sup> *	0.312×10 <sup>-1</sup> 1.824×10 <sup>-1</sup> *
* obtained using	higher order lavered hevahed	al elements with reduced integration	

obtained using higher order layered hexahedral elements with reduced integration

[Note]

If the mesh is not perfectly symmetric, averaged displacement from point A and B is used.

If there is no node at point A and B, the averaged value is calculated from the nearest two nodes.