

Body Torsional Analysis

Computational Design Laboratory
Department of Automotive Engineering
Hanyang University, Seoul, Korea



한양대학교
HANYANG UNIVERSITY

CDL Computational
Design
Lab

OUTLINE

- **Lecture Goals**

- ✓ Side frame모델(beam)의 유효전단강성과 passenger cabin모델(beam+shell)의 비틀림 강성을 계산하여 이론해와 비교한다.

- **Contents**

- ✓ Body torsional stiffness analysis #1
 - : Beam elements
- ✓ Body torsional stiffness analysis #2
 - : Shell + beam elements

Body Torsional Stiffness Analysis

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목차

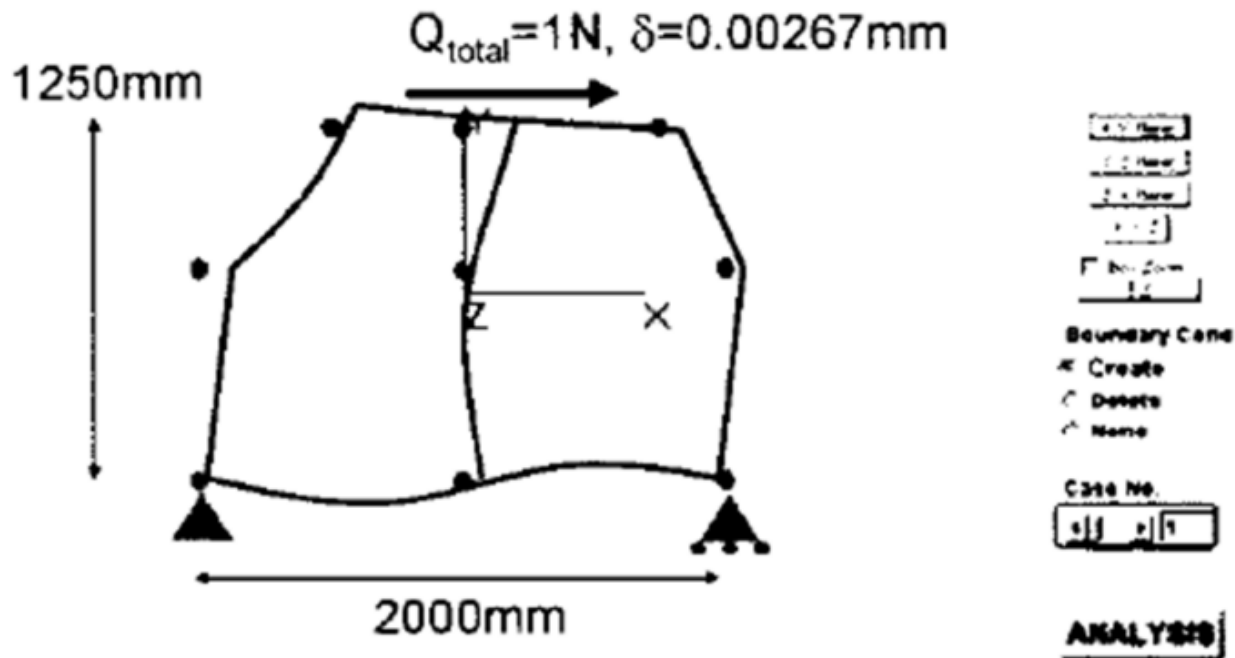
- 예제 문제
 - Effective shear stiffness analysis of side frame
 - Body torsional stiffness analysis
- 해석 프로세스
 - 기하형상 생성
 - 재료 물성 및 특성 입력
 - 요소망 생성
 - 구속조건 설정
 - 하중조건 설정
 - 해석케이스 정의 및 해석 실행
 - 후처리

EFFECTIVE SHEAR RIGIDITY (SIDE FRAME)

예제: TORSIONAL STIFFNESS (3)

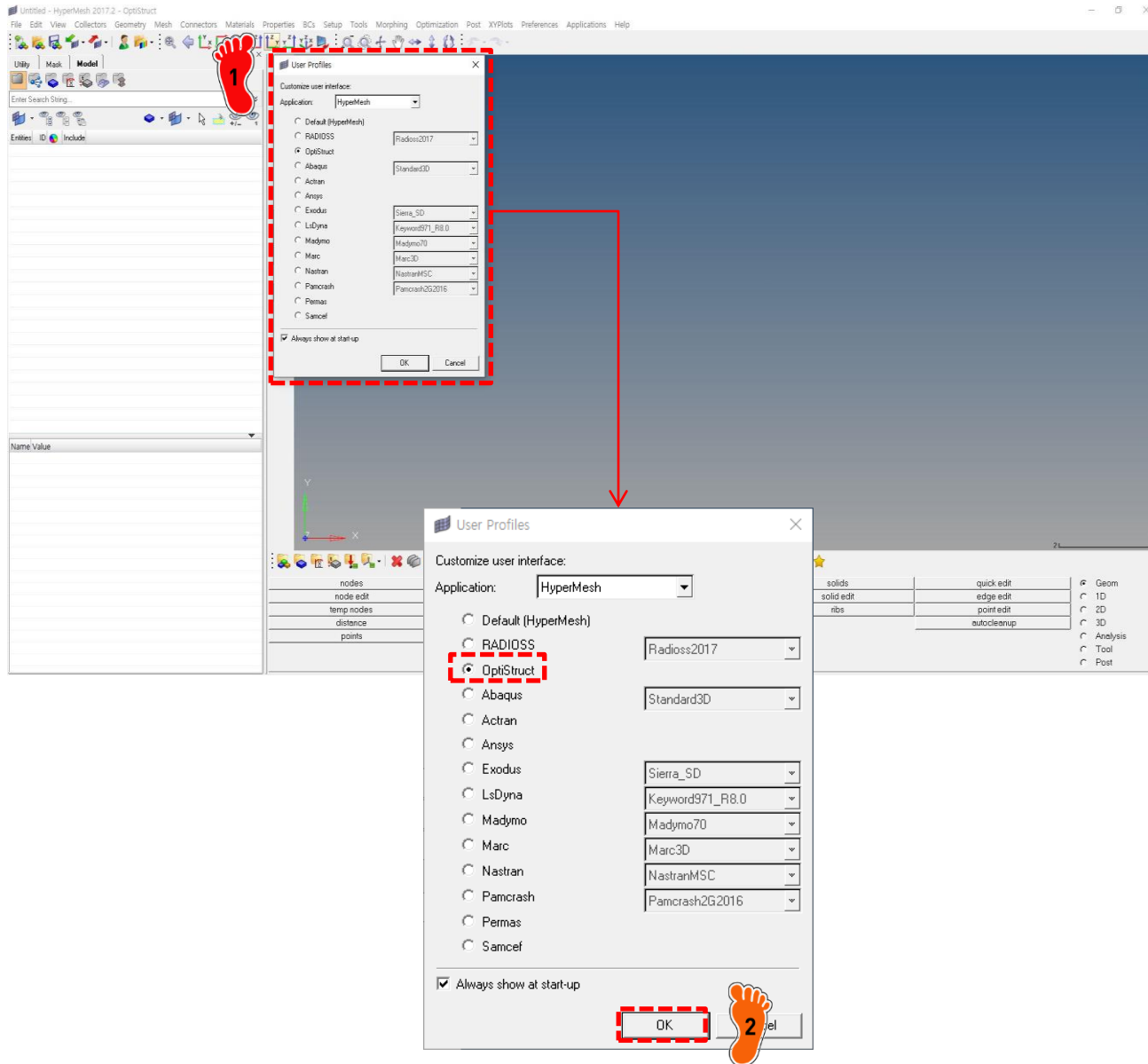
Side Frame Model 의 강성 계산

- FEA under shear loading

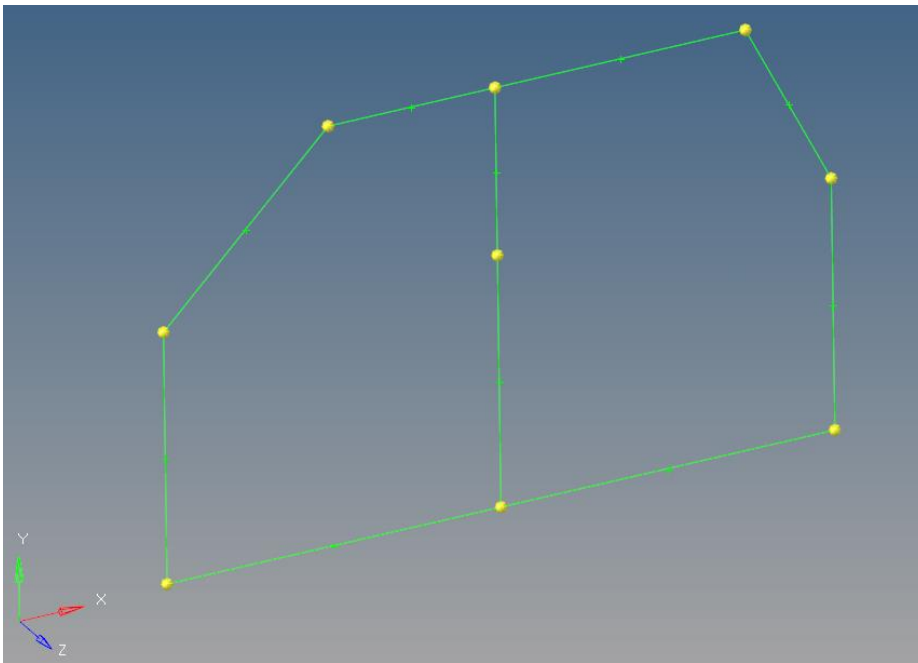
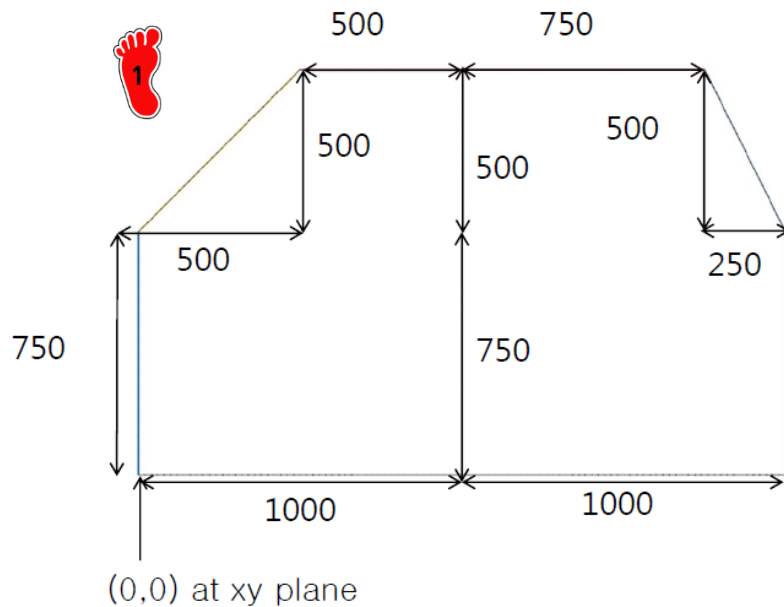


$$(Gt)_{Eff} = \left(\frac{Q}{\delta} \right) \frac{H}{L} = \left(\frac{1N}{.00267mm} \right) \frac{1250mm}{2000mm} = 234N/mm$$

기하형상 생성 (1)



기하형상 생성 (2)

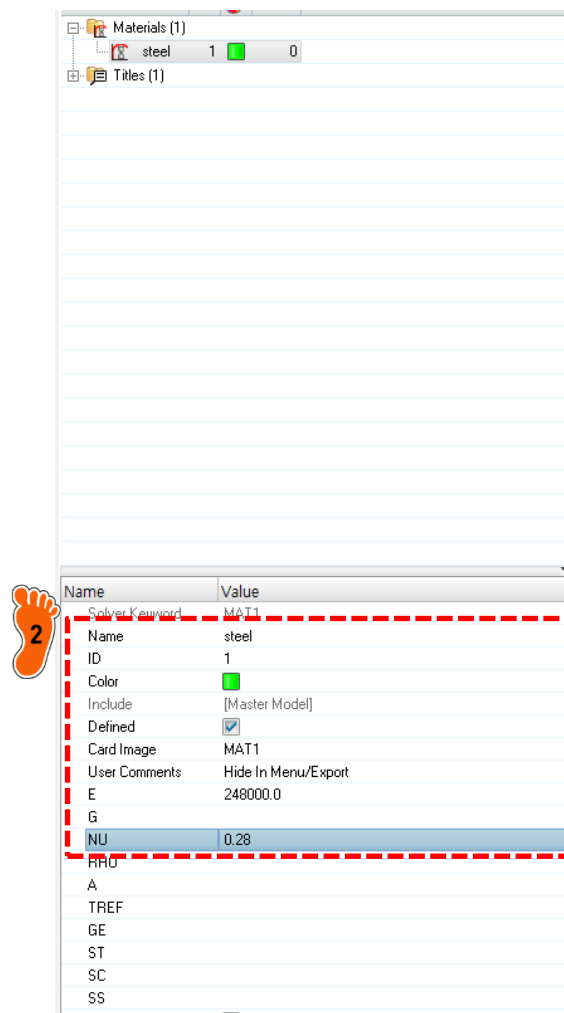
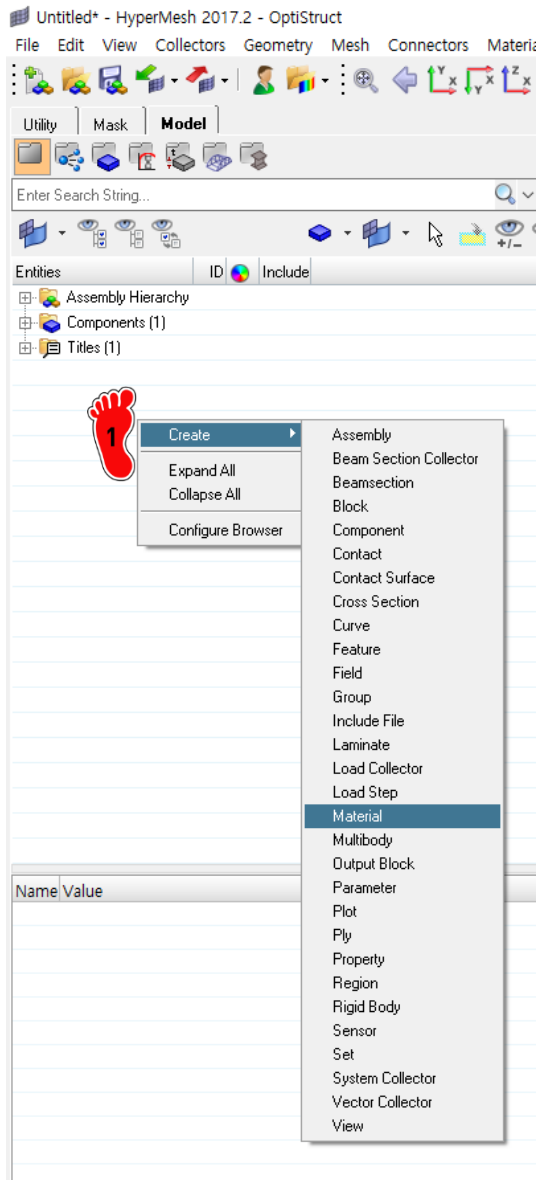


1 주어진 기하형상 생성

좌표(x,y,z)

(0,0,0)
 (0,750,0)
 (500,1250,0)
 (1000,0,0)
 (1000,750,0)
 (1000,1250,0)
 (1750,1250,0)
 (2000,0,0)
 (2000,750,0)

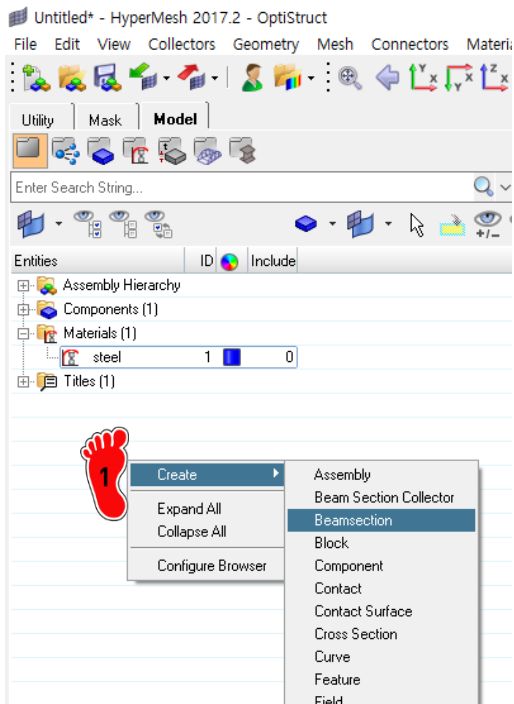
재료 물성 및 특성 입력 (1)



1 우클릭, Create > Material

2 Name > steel
탄성계수(E)
> 248 Gpa (248000 N/mm²)
푸아송비(NU) > 0.28
재료 생성

재료 물성 및 특성 입력 (2)

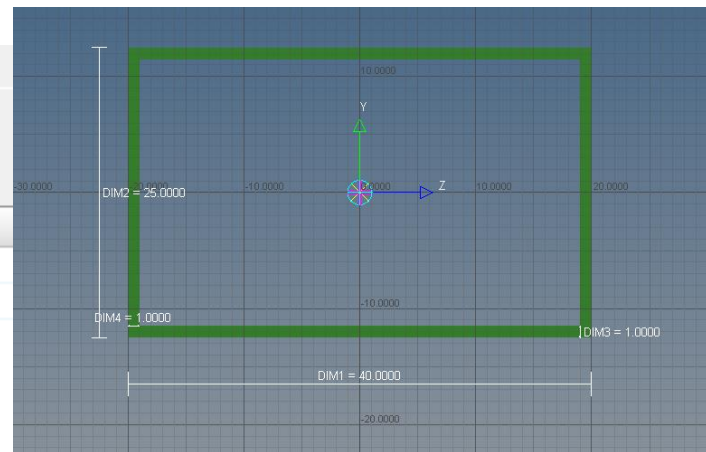
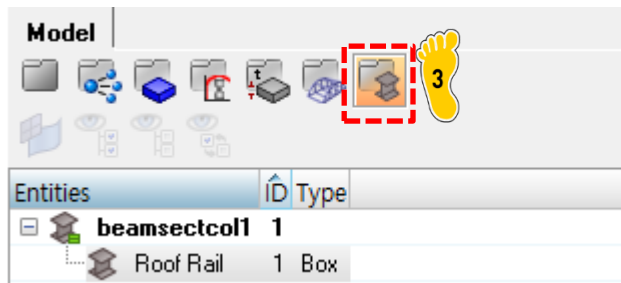


Name	Value
Name	Roof Rail
ID	1
Include	[Master Model]
Collector	(1) beamsectcol1
Config	Standard
Section Type	BOX
Parameter Definitions	
Dimension DIM1	40.0
Dimension DIM2	25.0
Thickness DIM3	1.0
Thickness DIM4	1.0

1 우클릭,
Create > Beamsection

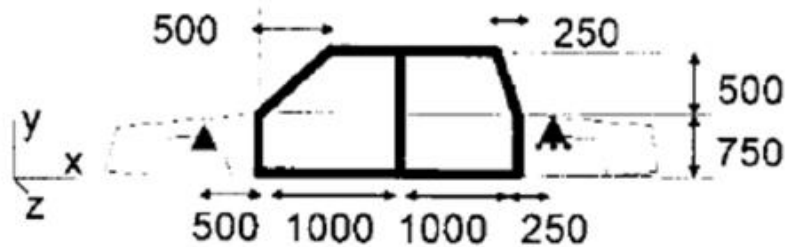
2 Section Type > BOX,
단면형상 입력

3 Hyperbeam view에서 단면
형상 확인 가능

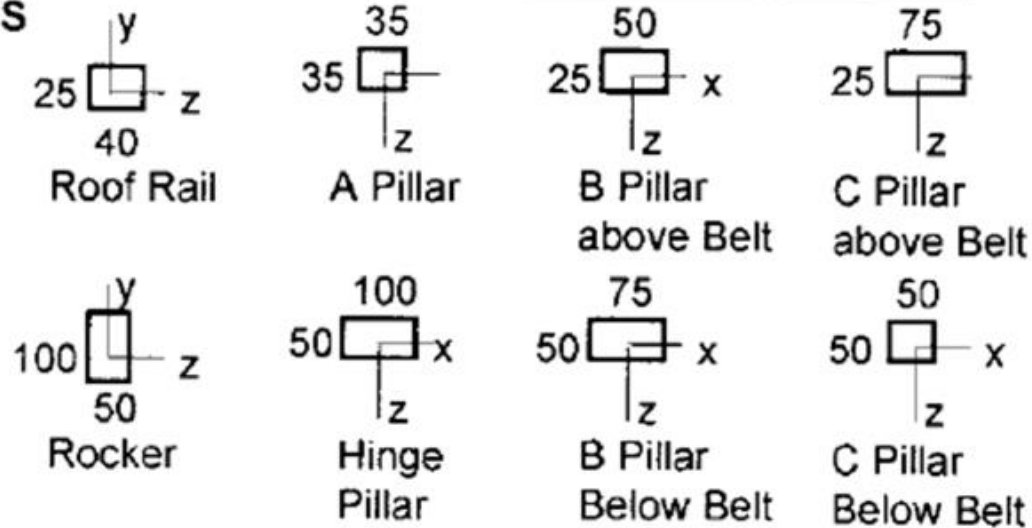


재료 물성 및 특성 입력 (3)

Sideframe
Dimensions
(all in mm)



SECTIONS
(t=1mm)



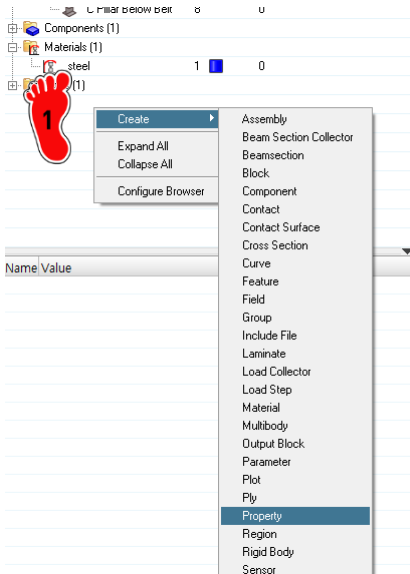
Assembly Hierarchy		
Beam Section Collectors (1)		
beamsectcol1	1	0
Roof Rail	1	0
A Pillar	2	0
B Pillar above Belt	3	0
C Pillar above Belt	4	0
Rocker	5	0
Hinge Pillar	6	0
B Pillar Below Belt	7	0
C Pillar Below Belt	8	0

Name	Value
Name	Roof Rail
ID	1
Include	[Master Model]
Collector	(1) beamsectcol1
Config	Standard
Section Type	BOX
Parameter Definitions	
Dimension DIM1	40.0
Dimension DIM2	25.0
Thickness DIM3	1.0
Thickness DIM4	1.0

1 예제에서 주어진 단면형상 8개를 각각 생성

2 Dimension DIM1에 Z방향 길이 입력

재료 물성 및 특성 입력 (4)



1 우클릭,
Create > Property

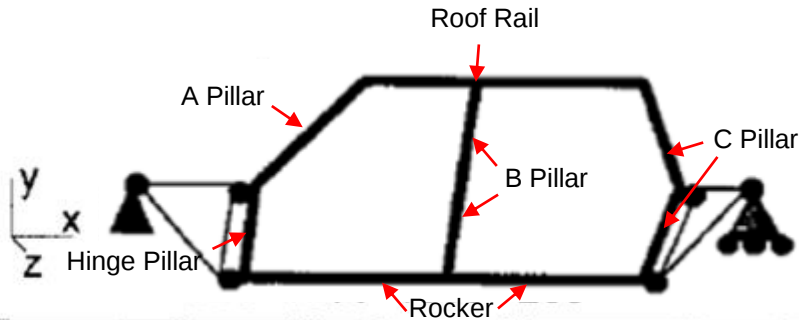
Entities	ID	Color	Include
Beam Section Collectors (1)			
beamsectcol1	1		0
Roof Rail	1		0
A Pillar	2		0
B Pillar above Belt	3		0
C Pillar above Belt	4		0
Rocker	5		0
Hinge Pillar	6		0
B Pillar Below Belt	7		0
C Pillar Below Belt	8		0
Components (1)			
Materials (1)			
steel	1		0
Properties (8)			
Roof Rail	1		0
A Pillar	2		0
B Pillar above Belt	3		0
C Pillar above Belt	4		0
Rocker	5		0
Hinge Pillar	6		0
B Pillar Below Belt	7		0
C Pillar Below Belt	8		0

2 Property 8개 각각 생성, 단
면 형상과 각각 연결
Card Image > PBEAM
Material > steel
Beam Section > 단면형상
각각 선택
Name > 단면 형상과 동일
하게

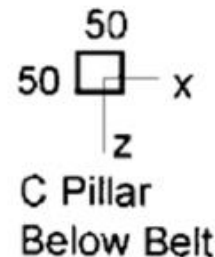
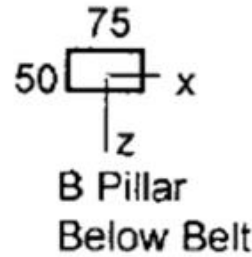
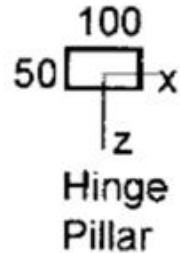
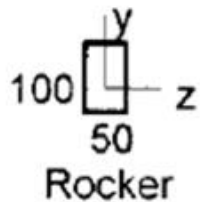
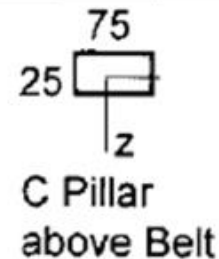
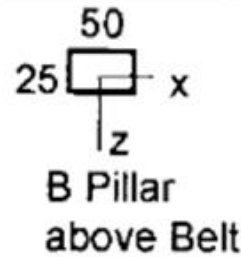
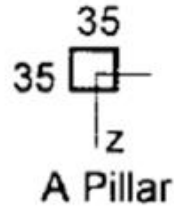
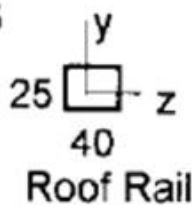
Name	Value
Solver Keyword	PBEAM
Name	Roof Rail
ID	1
Color	
Include	[Master Model]
Defined	☒
Card Image	PBEAM
Material	(1) steel
User Comments	Hide In Menu/Export
Beam Section	(1) Roof Rail
PBEAM_CARD3 =	0

요소망 생성 (1)

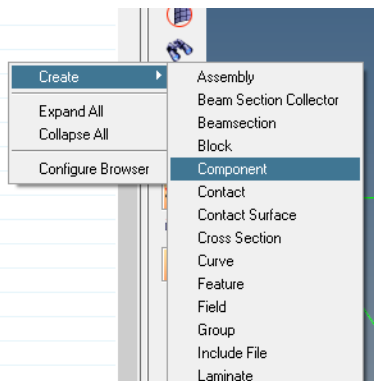
**Sideframe
Dimensions
(all in mm)**



**SECTIONS
(t=1mm)**



1



2

Name	Value
Name	Roof Rail
ID	2
Color	
Include	[Master Model]
Property	(1) Roof Rail
Material	(1) steel

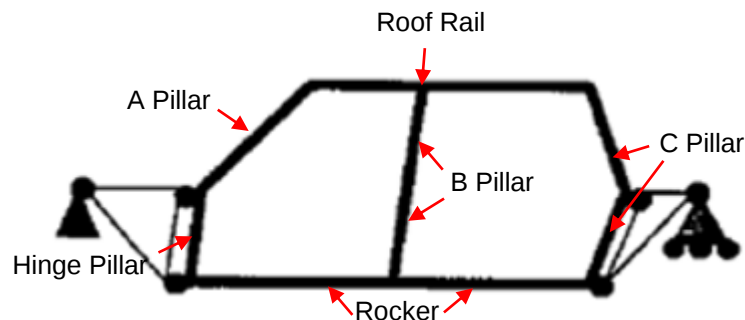
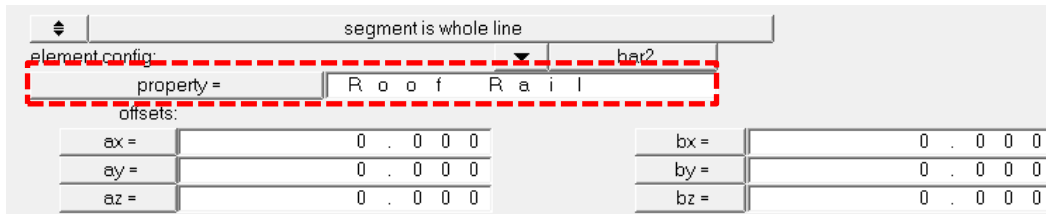
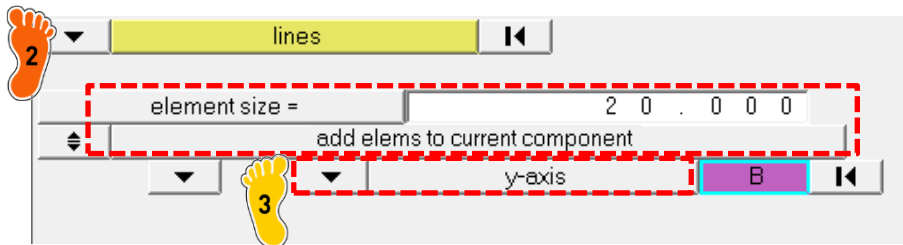
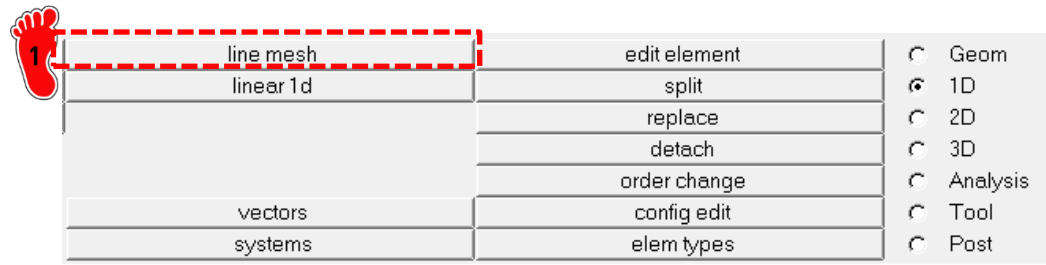
1

우클릭,
Create > Component

2

Name, Property
> 요소망 생성할 단면형상의
이름과 동일하게

요소망 생성 (2)



1 1D > line mesh 클릭

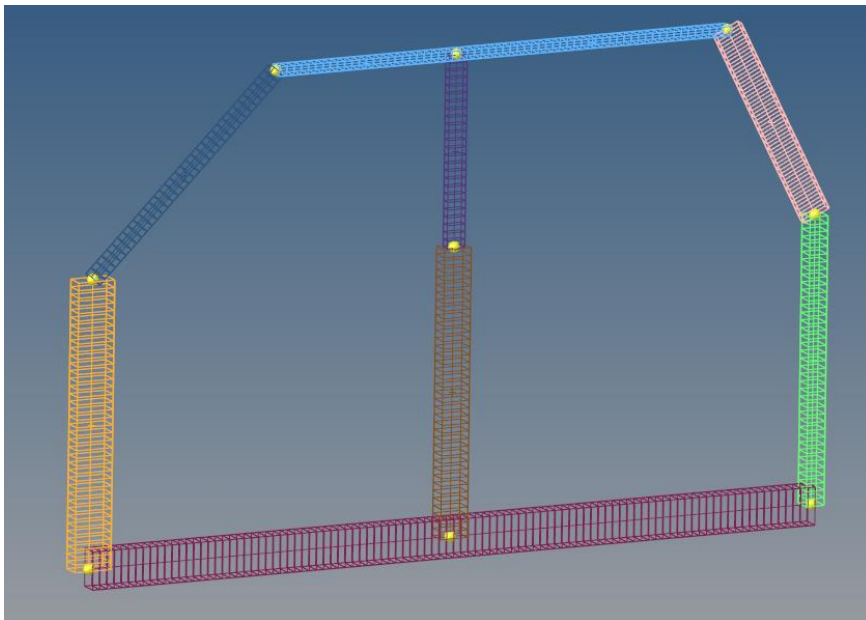
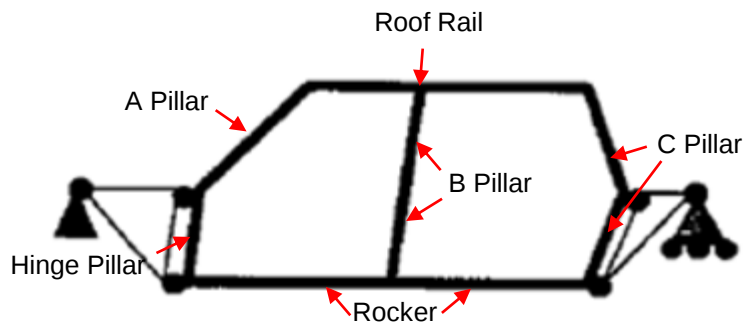
2 요소망 생성
크기 > 20
Add elems to current
component
Property > 단면형상 이름
과 동일하게



3 요소망 생성시 단면 형상이
원하는 좌표축에 놓이도록
주의(x축과 평행한 빔은 y-
axis로 선택, y축과 평행한
빔은 x-axis로 선택)

4 Mesh,
Return

요소망 생성 (3)



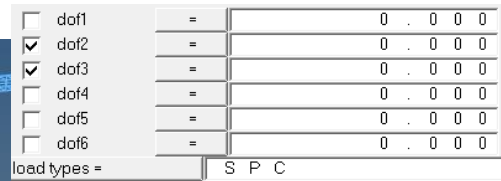
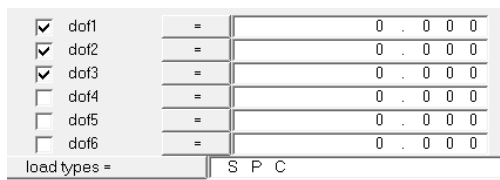
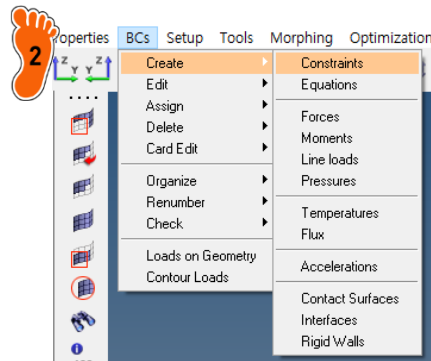
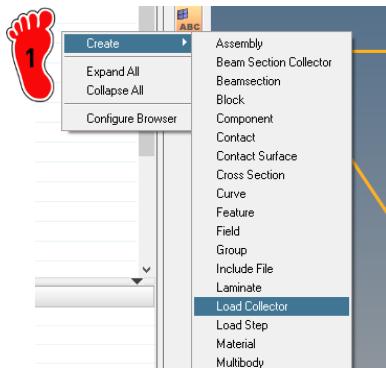
앞의 과정(1,2) 반복해서
8개 빔 요소망 생성

그림과 비슷한 형상이 나와야 함

* Tool -> eedges ->
tolerance -> equivalence
(모서리 병합)

* Geom -> temp nodes ->
clear all (Nodes 제거)

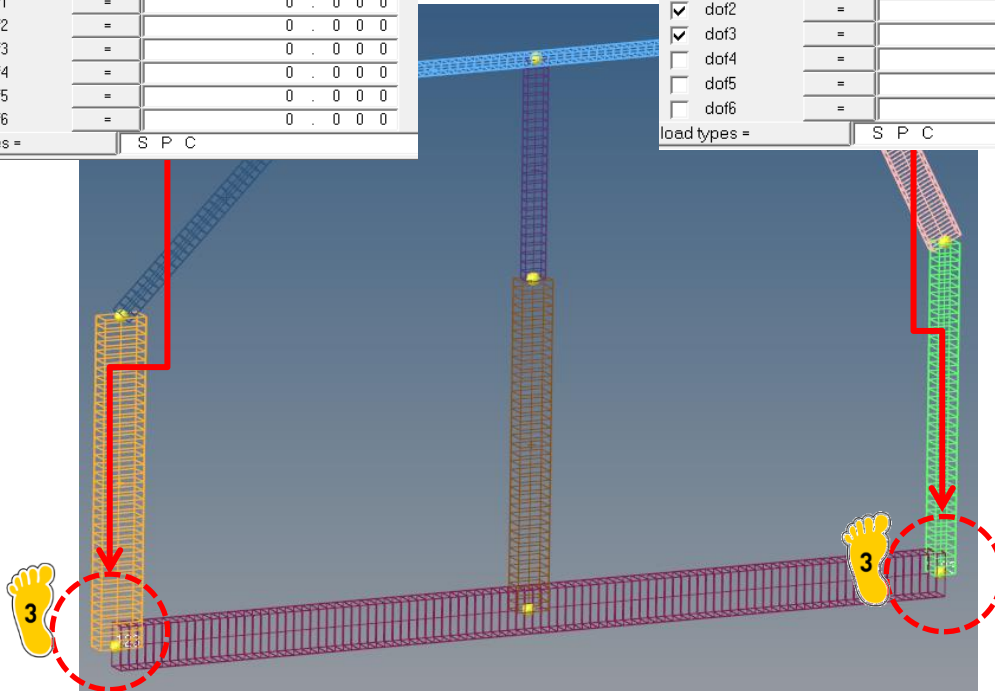
구속조건 및 하중조건 설정 (1)



1 Create > Load Collector
Name > spc

2 BCs > Create
> Constraints

3 좌측 dof1,2,3 check
Create
우측 dof2,3 check
Create

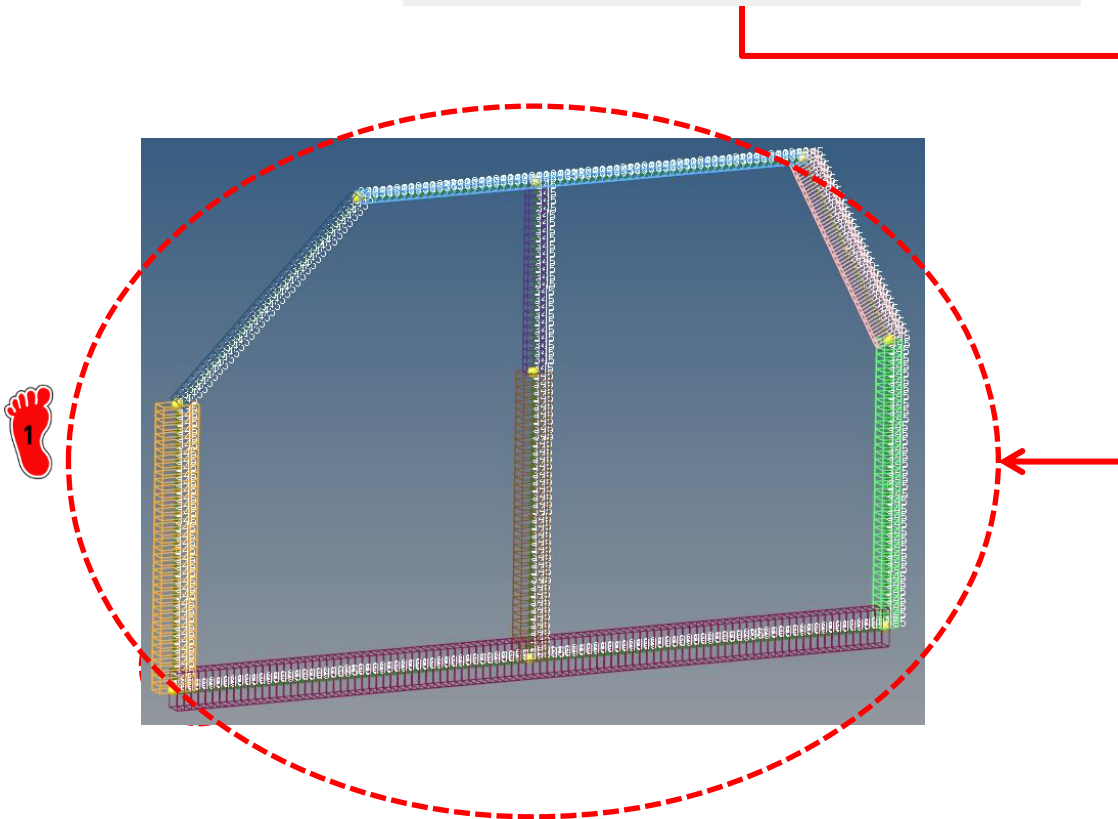


구속조건 및 하중조건 설정 (2)

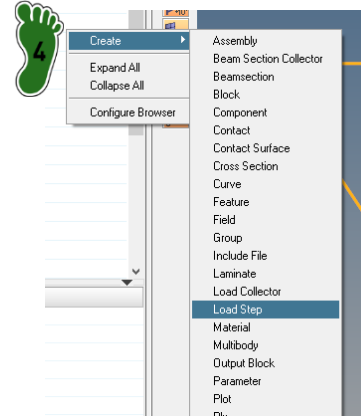
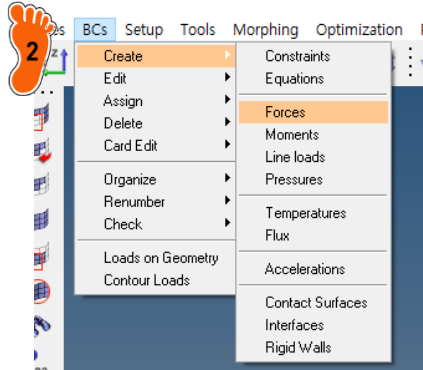
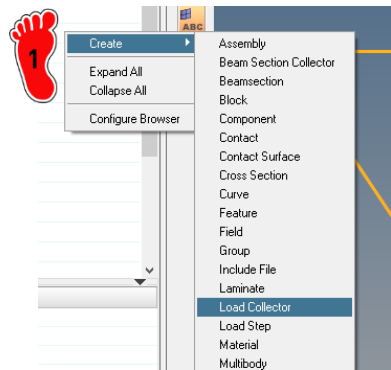
☐ dof1	=	0	0	0	0
☐ dof2	=	0	0	0	0
☒ dof3	=	0	0	0	0
☒ dof4	=	0	0	0	0
☒ dof5	=	0	0	0	0
☐ dof6	=	0	0	0	0

load types = S P C

1 나머지는 평면 거동을 위해
z방향 병진운동, x,y 방향 회
전운동 구속
(dof3,4,5)



구속조건 및 하중조건 설정 (3)



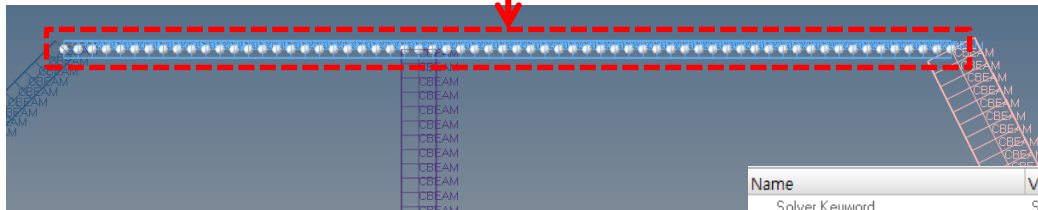
1 Create > Load Collector
Name > Force

2 BCs > Create
> Forces

3 상단에 x방향으로 0.0156N
Create (1N/64개 노드)

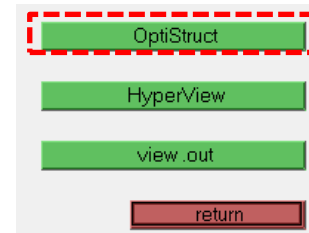
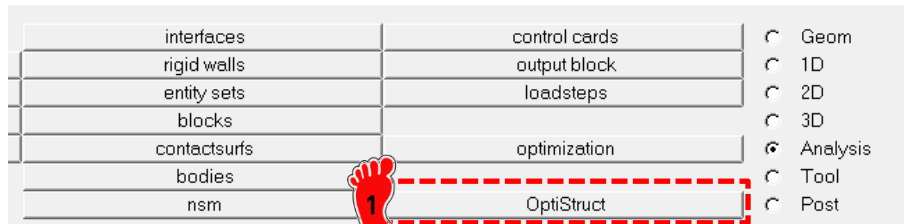
4 Create > Load Step

5 Analysis type
> Linear Static
SPC > spc
LOAD > Force



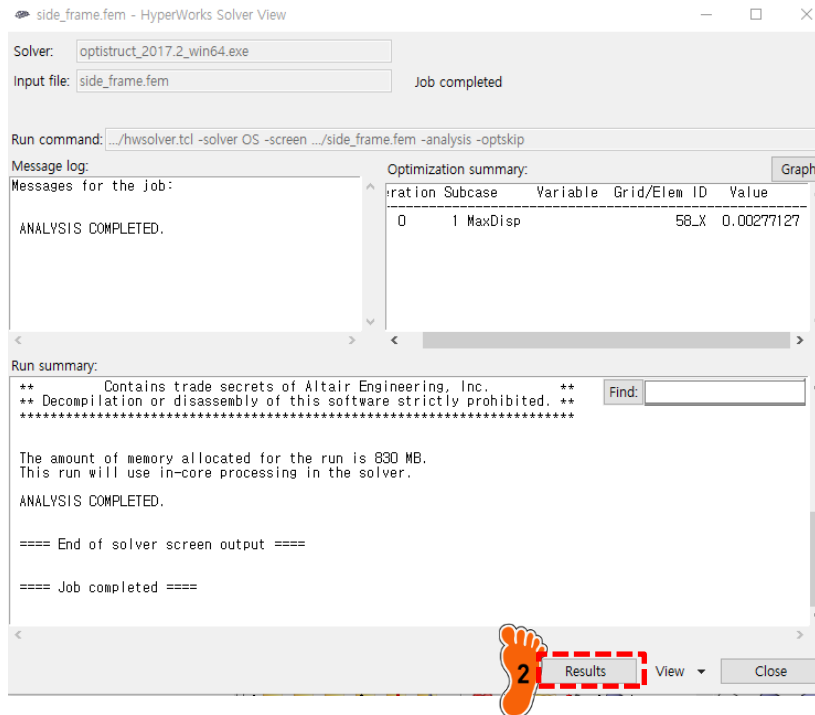
Name	Value
Solver Keyword	SUBCASE
Name	loadstep1
ID	1
Include	[Master Model]
User Comments	Hide In Menu/Export
Subcase Definition	
Analysis type	Linear Static
SPC	(1) spc
LOAD	(2) Force
SUPPORT1	<Unspecified>
PRETENSION	<Unspecified>
MPC	<Unspecified>
DEFORM	<Unspecified>
STATSUB (PRELOAD)	<Unspecified>
STATSUB (PRETENS)	<Unspecified>
SUBCASE OPTIONS	

해석 케이스 정의 및 해석 실행

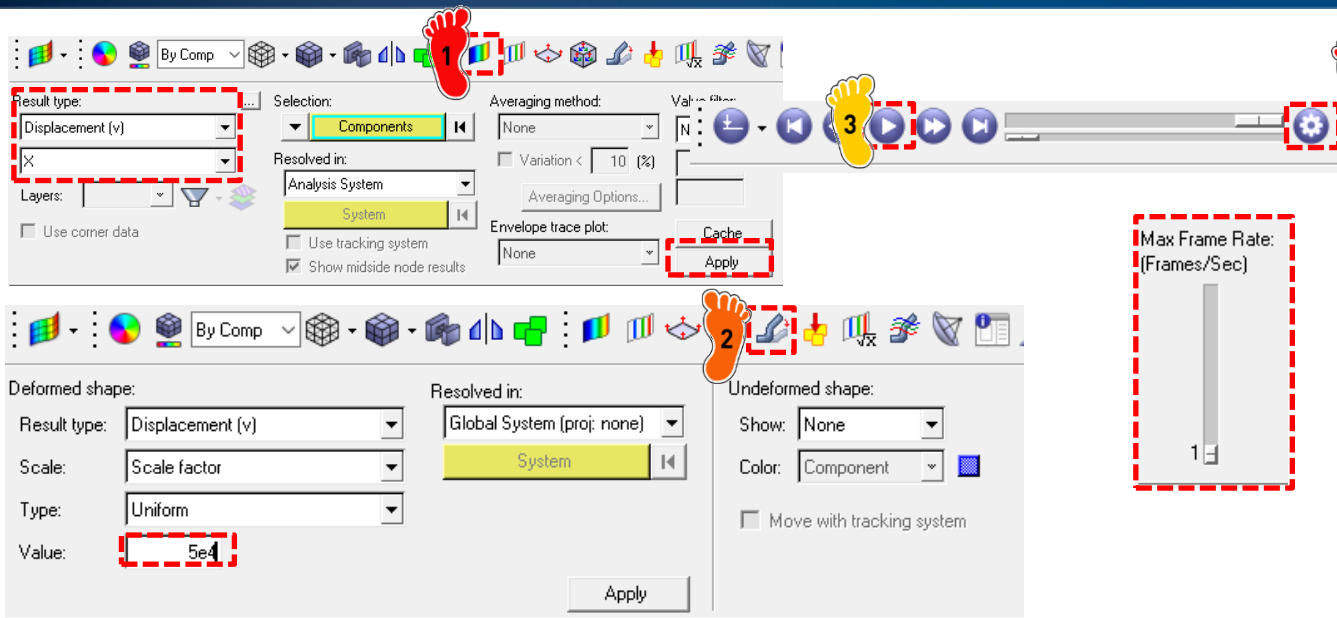


1 Analysis > OptiStruct 클릭
OptiStruct

2 Results 클릭



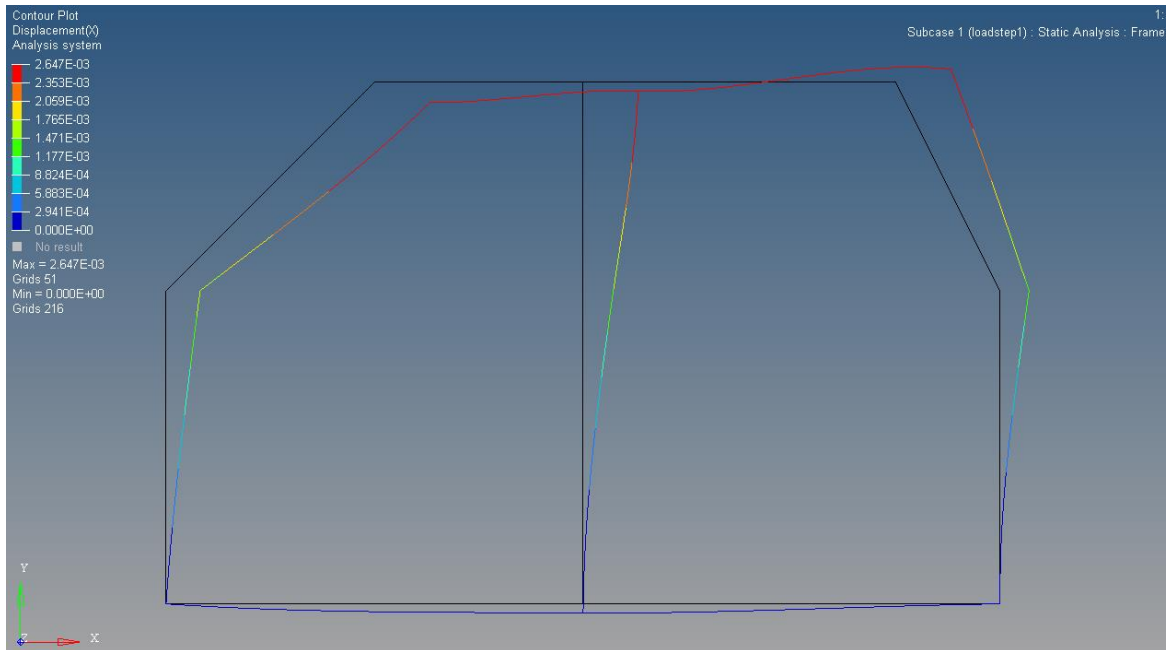
후처리



1 Contour 클릭
Displacement, X
Apply

2 Deformed 클릭
Value > 5e4
Apply

3 Animation Control 클릭
Max Frame Rate > 1
Start animation



후처리

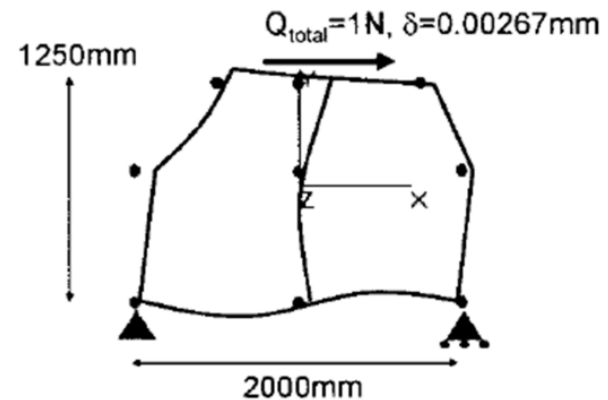


Contour Plot
Displacement(X)
Analysis system

2.647E-03
2.363E-03
2.059E-03
1.765E-03
1.471E-03
1.177E-03
8.824E-04
5.883E-04
2.941E-04
0.000E+00
No result

Max = 2.647E-03
Grids 51
Min = 0.000E+00
Grids 216

• FEA under shear loading



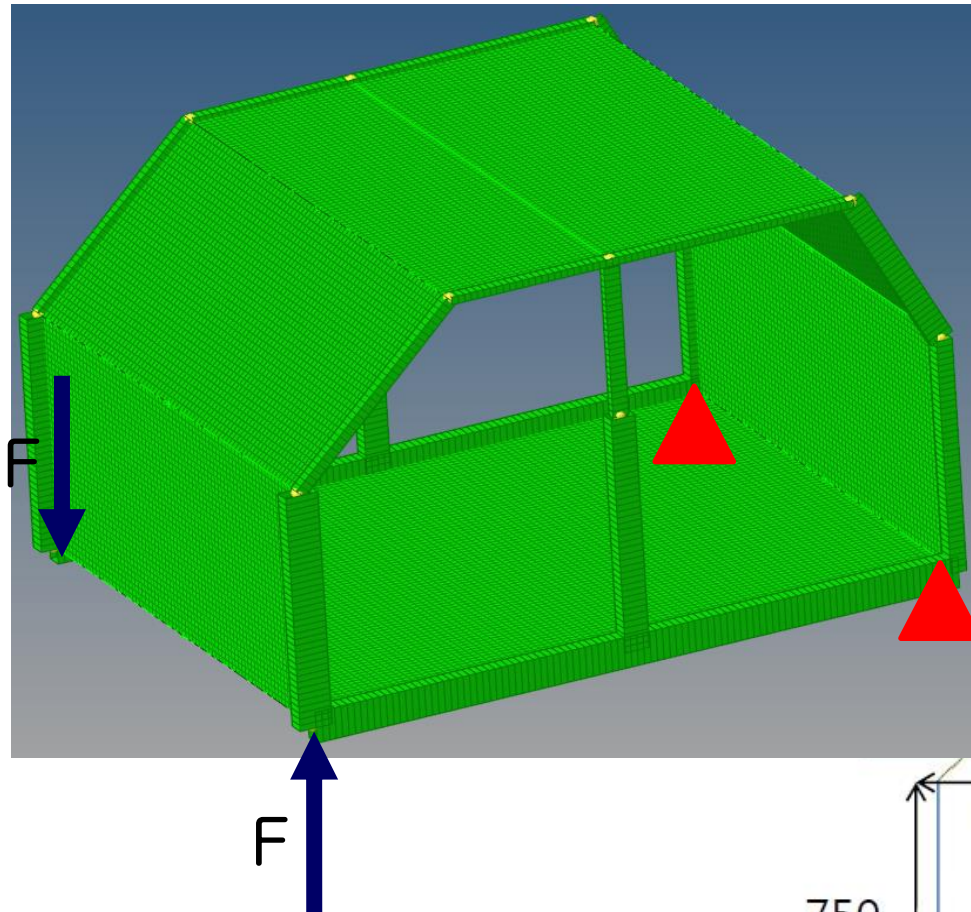
$$(Gt)_{eff} = \left(\frac{Q}{\delta} \right) \frac{H}{L} = \left(\frac{1N}{0.00267mm} \right) \frac{1250mm}{2000mm} = 234N/mm$$

$$(G_f)_{eff} = \left(\frac{1N}{0.002647mm} \right) \cdot \frac{1250mm}{2000mm} = 236.1N/mm$$

TORSIONAL STIFFNESS (SHELL + BEAM ELEMENTS)

예제: TORSIONAL STIFFNESS (1)

다음 주어진 기하형상의 비틀림 강성을 구하시오. (프레임은 앞 예제의 모델 이용)

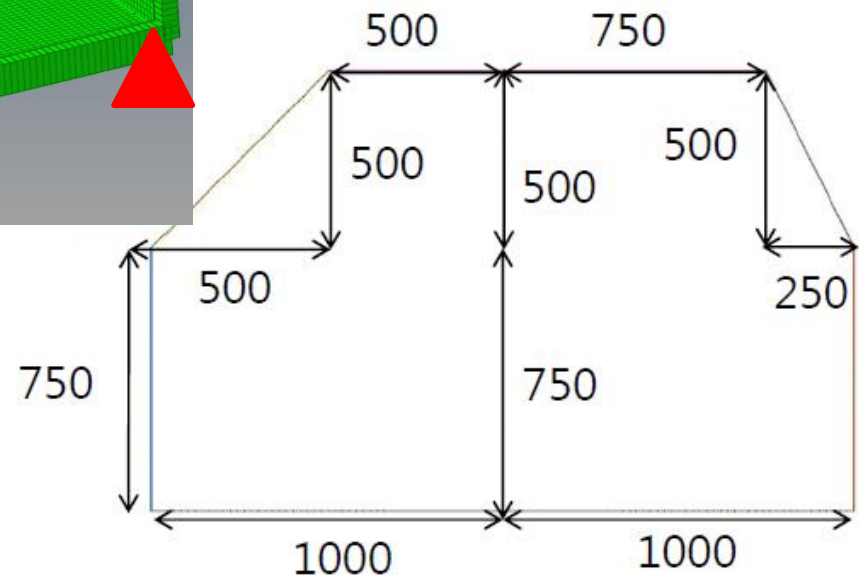


Material

- $E = 204.8 \text{ GPa}$
- $\nu = 0.28$
- $G = 80 \text{ GPa}$

Force

- $T = 7730000 \text{ Nmm}$
- $F = 7730000/1560$
 $= 4955.13 \text{ N}$



예제: TORSIONAL STIFFNESS (2)

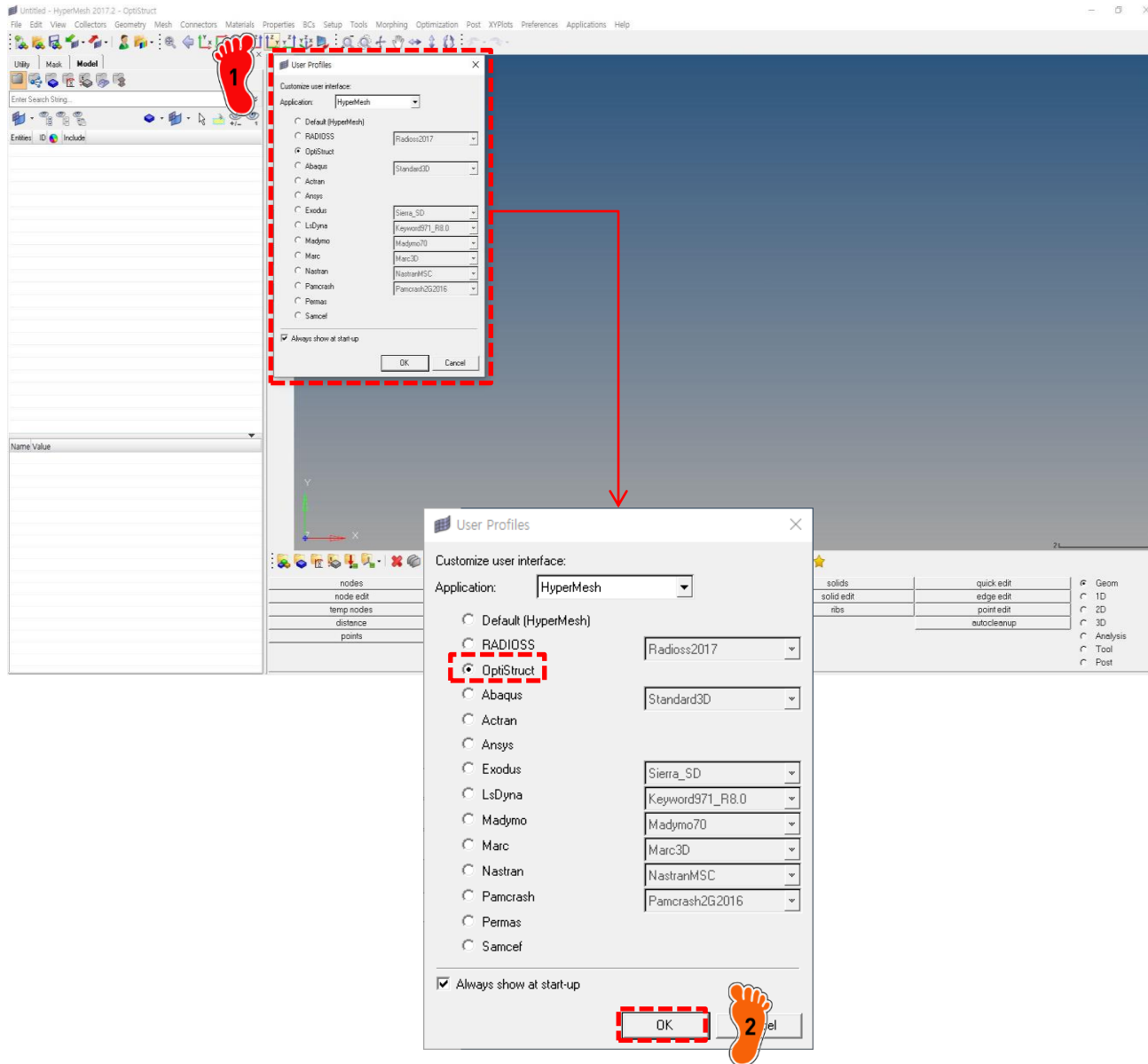
다음 주어진 기하형상의 비틀림 강성을 구하시오

$$T = 7,730,000 \text{ Nmm}, q = 2678 \text{ N} / 1250 \text{ mm} = 2.1414 \text{ N/mm}$$

Panel	Area of panel (mm ²)	Effective shear rigidity (Gt) _{EFF} (N/mm)	Area of surface / (Gt) _{EFF} (mm ³ /N)
dash	1170000	80000	14.6
windshield	1103087	80000	13.8
roof	1950000	80000	24.4
back light	872067	80000	10.9
seat back	1170000	80000	14.6
floor	3120000	80000	29.0
side frame-left	2312500	234	9882.5
side frame-right	2312500	234	9882.5

$$K = \frac{1}{\left(\frac{q}{T}\right)^2 \sum_{\text{ALL SURFACE}} \left[\frac{\text{area of surface}}{(Gt)_{\text{EFF}}} \right]} = 6.55 \times 10^8 \text{ Nmm/rad}$$

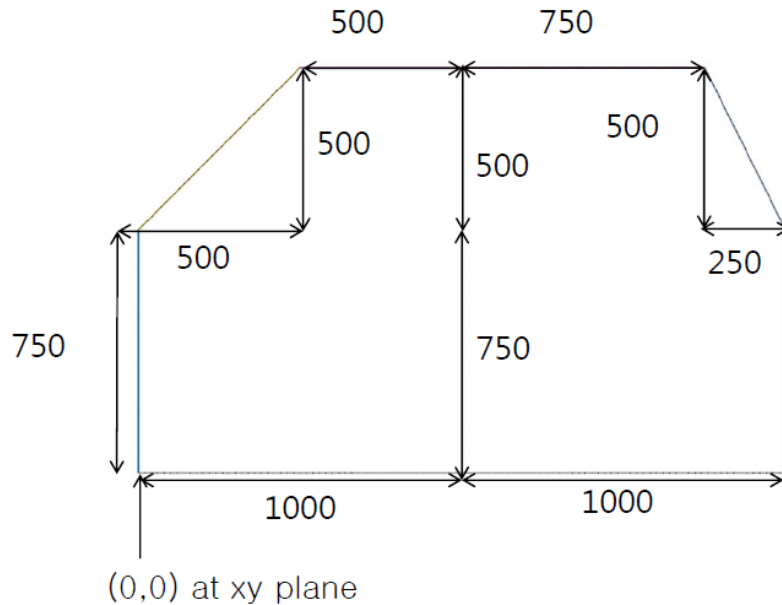
기하형상 생성 (1)



1 OptiStruct 선택

2 OK

기하형상 생성 (2)



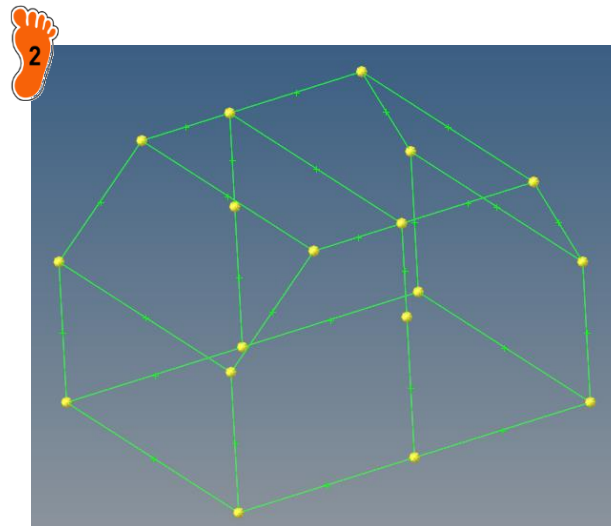
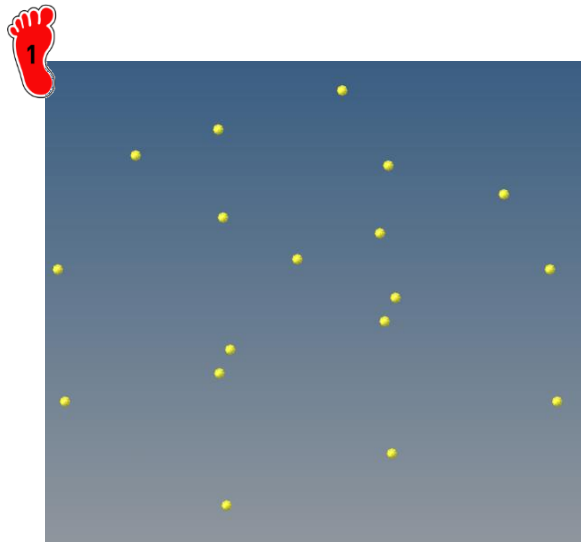
1 주어진 기하형상 생성

점 좌표

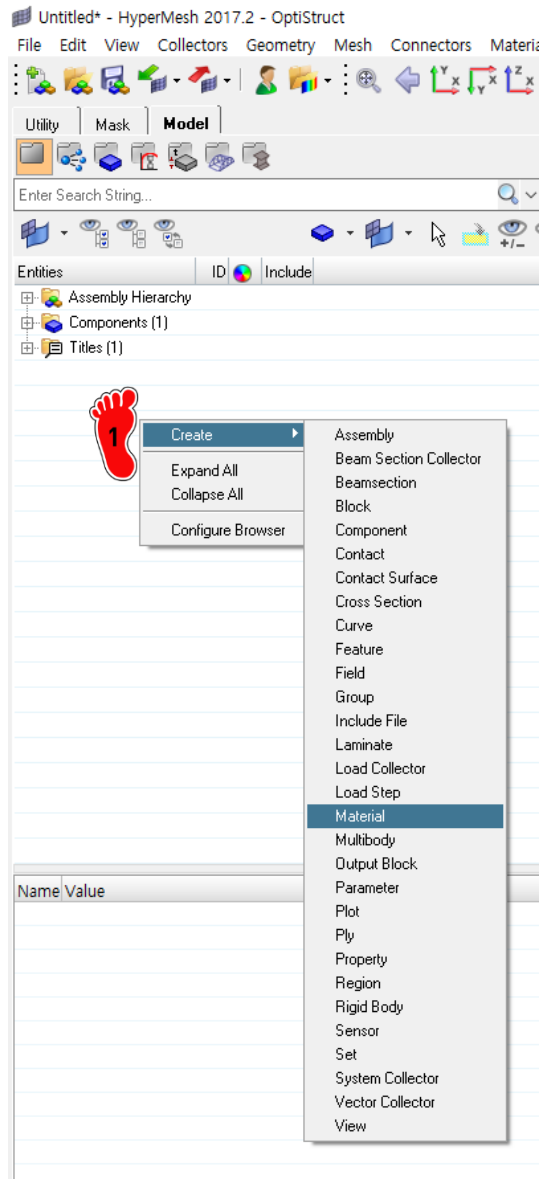
(0,0,0)
 (0,750,0)
 (500,1250,0)
 (1000,0,0)
 (1000,750,0)
 (1000,1250,0)
 (1750,1250,0)
 (2000,0,0)
 (2000,750,0)

반대편 sideframe을 모델링
 하기 위해,
 Z축방향으로 1560mm 평행
 이동된 점 9개 추가로 생성

2 생성한 점들을 연결하여 그 림과 같이 선 생성



재료 물성 및 특성 입력 (1)

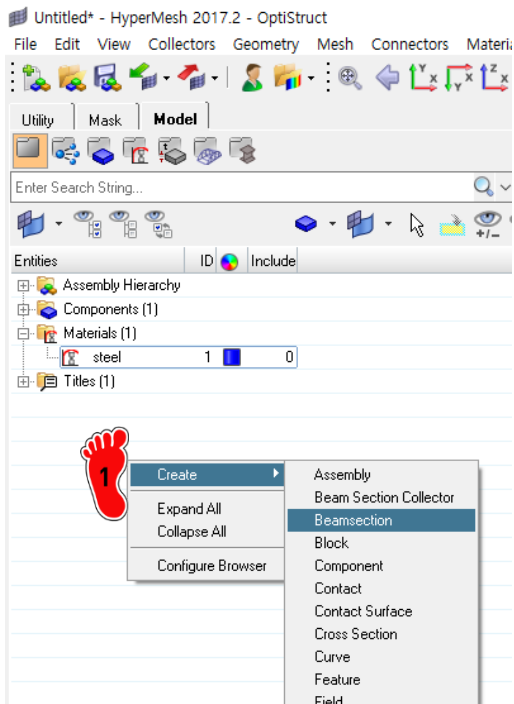



Name	Value
Solver Keyword	MAT1
Name	steel
ID	1
Color	
Include	[Master Model]
Defined	☒
Card Image	MAT1
User Comments	Do Not Export
E	204800.0
G	
NU	0.28

1 우클릭, Create > Material

2 Name > steel
탄성계수(E)
> 204.8Gpa (204800
N/mm²)
푸아송비(NU) > 0.28
재료 생성

재료 물성 및 특성 입력 (2)

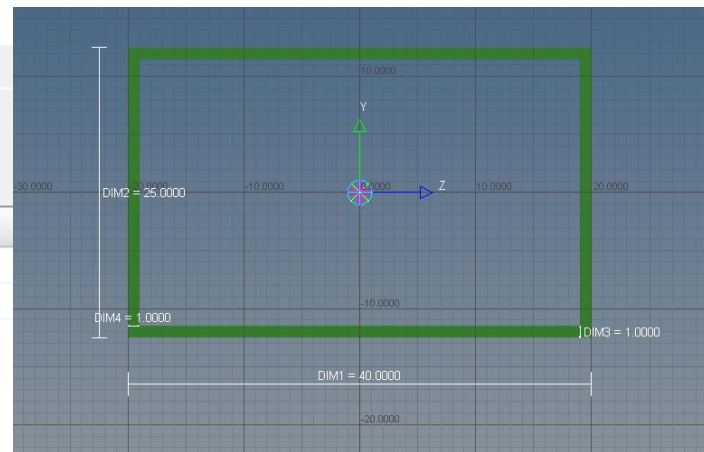
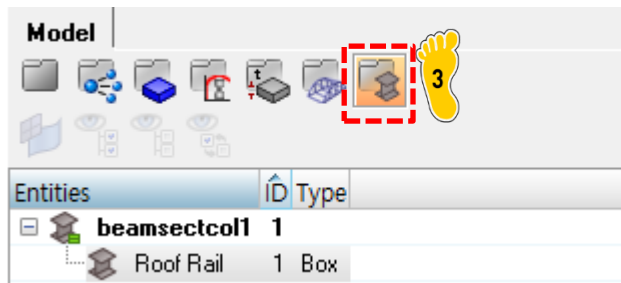


Name	Value
Name	Roof Rail
ID	1
Include	[Master Model]
Collector	(1) beamsectcol1
Config	Standard
Section Type	BOX
Parameter Definitions	
Dimension DIM1	40.0
Dimension DIM2	25.0
Thickness DIM3	1.0
Thickness DIM4	1.0

1 우클릭,
Create > Beamsection

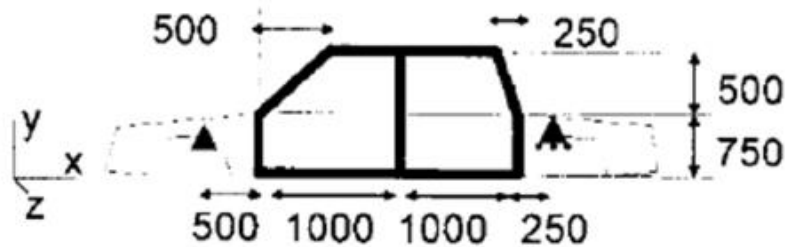
2 Section Type > BOX,
단면형상 입력

3 Hyperbeam view에서 단면
형상 확인 가능

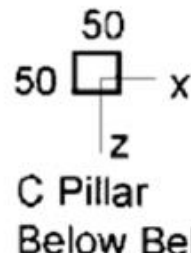
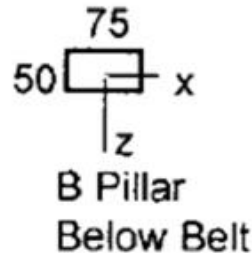
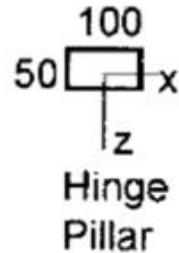
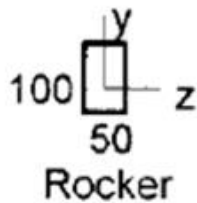
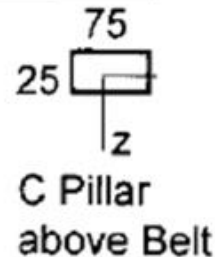
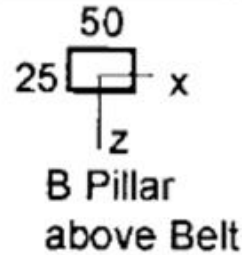
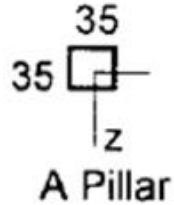
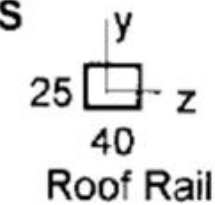


재료 물성 및 특성 입력 (3)

Sideframe
Dimensions
(all in mm)



SECTIONS
(t=1mm)



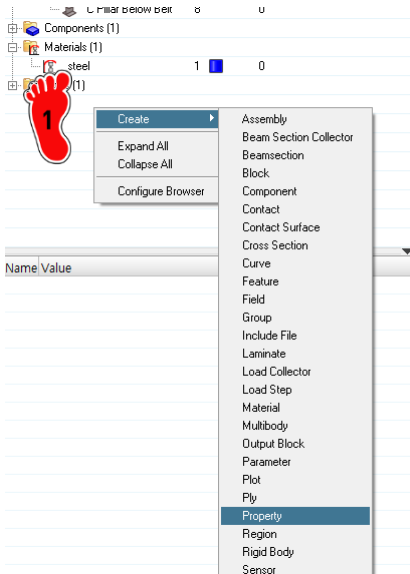
Assembly Hierarchy		
Beam Section Collectors (1)		
beamsectcol1	1	0
Roof Rail	1	0
A Pillar	2	0
B Pillar above Belt	3	0
C Pillar above Belt	4	0
Rocker	5	0
Hinge Pillar	6	0
B Pillar Below Belt	7	0
C Pillar Below Belt	8	0

Name	Value
Name	Roof Rail
ID	1
Include	[Master Model]
Collector	(1) beamsectcol1
Config	Standard
Section Type	BOX
Parameter Definitions	
Dimension DIM1	40.0
Dimension DIM2	25.0
Thickness DIM3	1.0
Thickness DIM4	1.0

1 예제에서 주어진 단면형상
8개를 각각 생성

2 Dimension DIM1에
Z방향 길이 입력

재료 물성 및 특성 입력 (4)



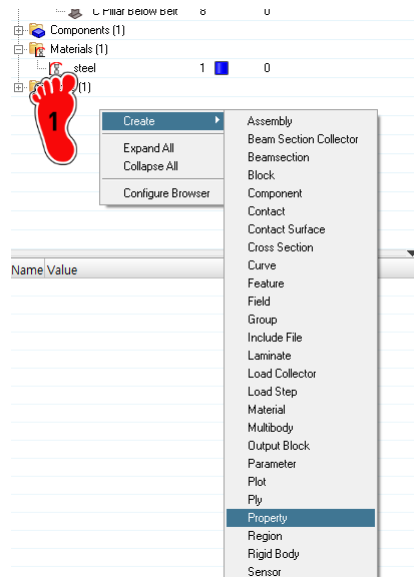
1 우클릭,
Create > Property

Entities	ID	Color	Include
Beam Section Collectors (1)			
beamsectcol1	1		0
Roof Rail	1		0
A Pillar	2		0
B Pillar above Belt	3		0
C Pillar above Belt	4		0
Rocker	5		0
Hinge Pillar	6		0
B Pillar Below Belt	7		0
C Pillar Below Belt	8		0
Components (1)			
Materials (1)			
steel	1		0
Properties (8)			
Roof Rail	1		0
A Pillar	2		0
B Pillar above Belt	3		0
C Pillar above Belt	4		0
Rocker	5		0
Hinge Pillar	6		0
B Pillar Below Belt	7		0
C Pillar Below Belt	8		0

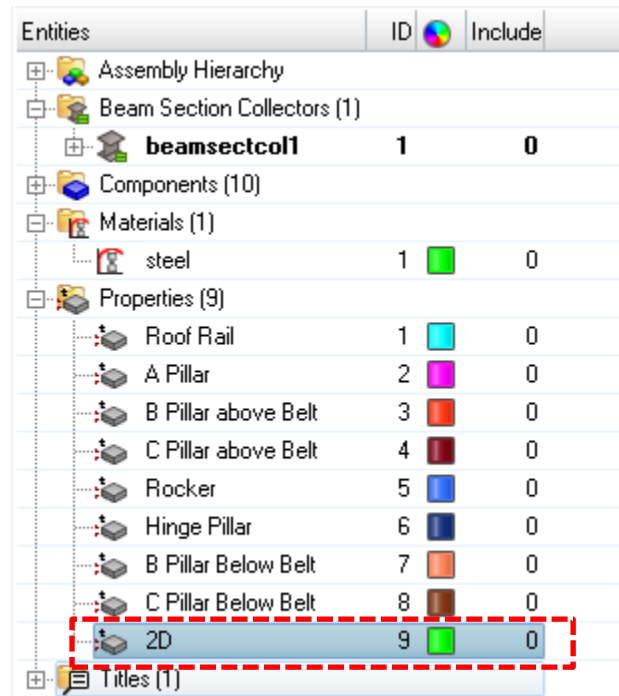
2 Property 8개 각각 생성, 단
면 형상과 각각 연결
Card Image > PBEAM
Material > steel
Beam Section > 단면형상
각각 선택
Name > 단면 형상과 동일
하게

Name	Value
Solver Keyword	PBEAM
Name	Roof Rail
ID	1
Color	
Include	[Master Model]
Defined	☒
Card Image	PBEAM
Material	(1) steel
User Comments	Hide In Menu/Export
Beam Section	(1) Roof Rail
PBEAM_CARD3 =	0

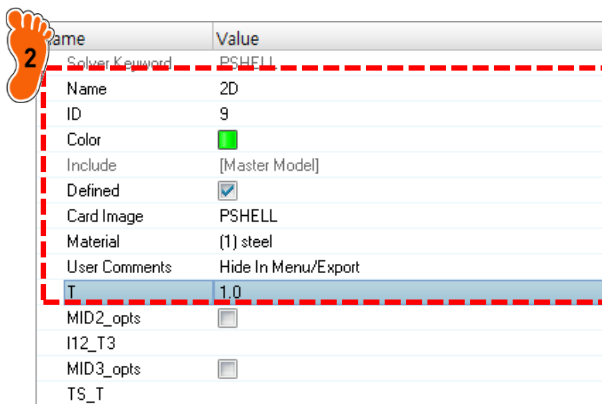
재료 물성 및 특성 입력 (5)



1 우클릭,
Create > Property

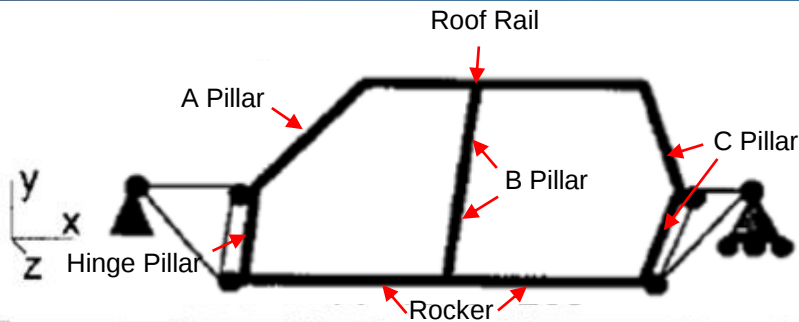


2 Card Image > PSHELL
Material > steel
T > 1mm
Name > 2D

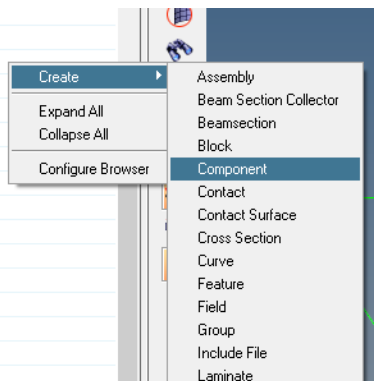
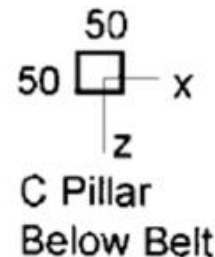
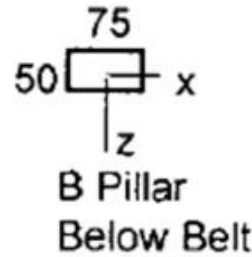
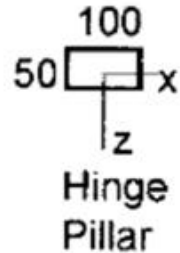
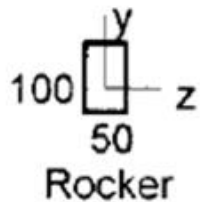
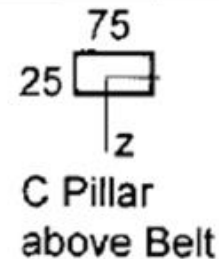
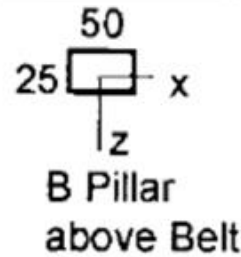
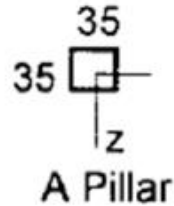
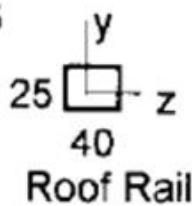


요소망 생성 (1)

**Sideframe
Dimensions
(all in mm)**



**SECTIONS
(t=1mm)**



Name	Value
Name	Roof Rail
ID	2
Color	
Include	[Master Model]
Property	(1) Roof Rail
Material	(1) steel

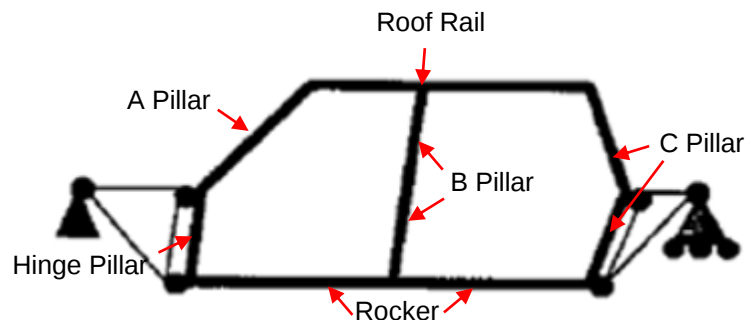
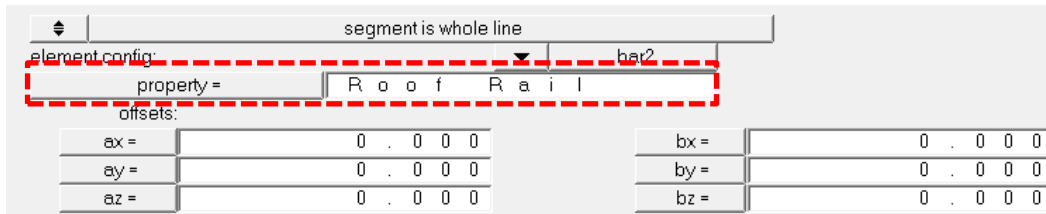
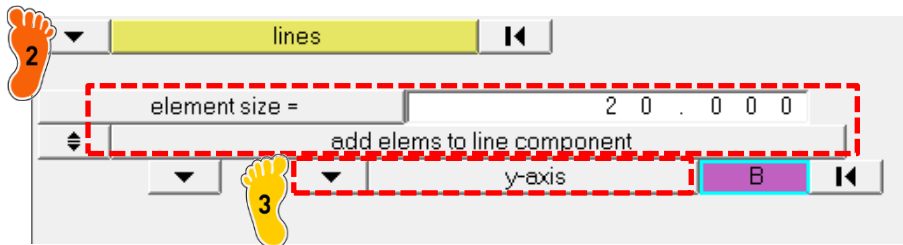
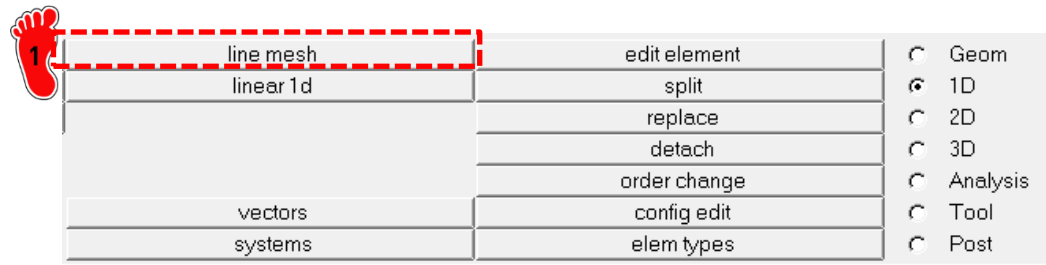


우클릭,
Create > Component



Name, Property
> 요소망 생성할 단면형상의
이름과 동일하게

요소망 생성 (2)



1 1D > line mesh 클릭

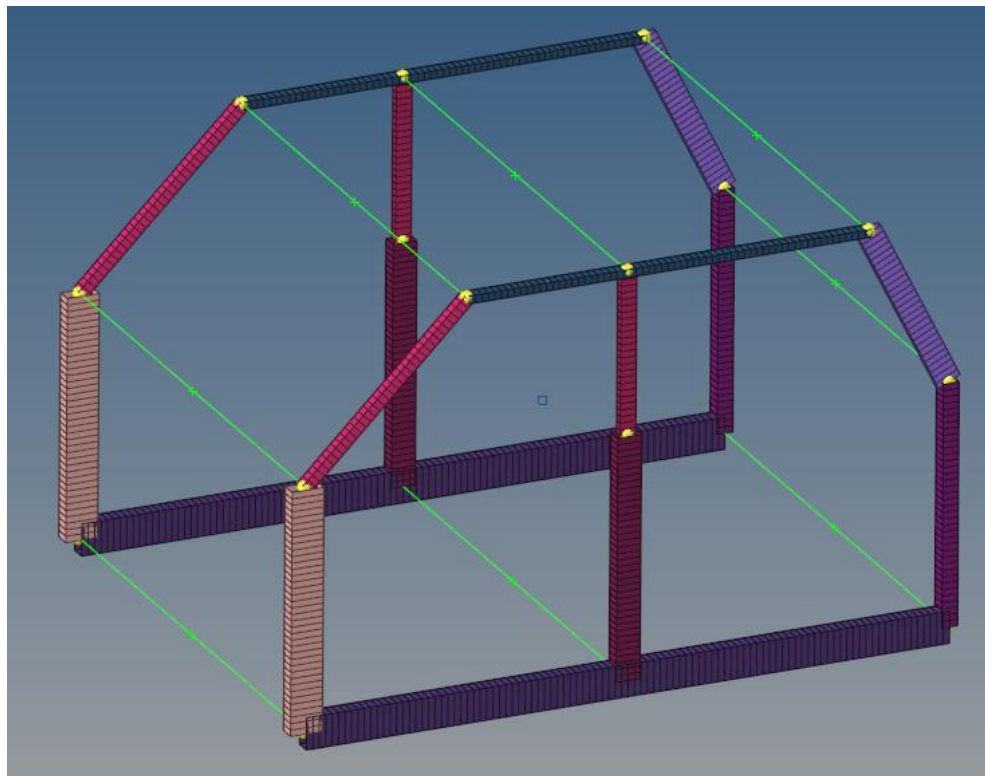
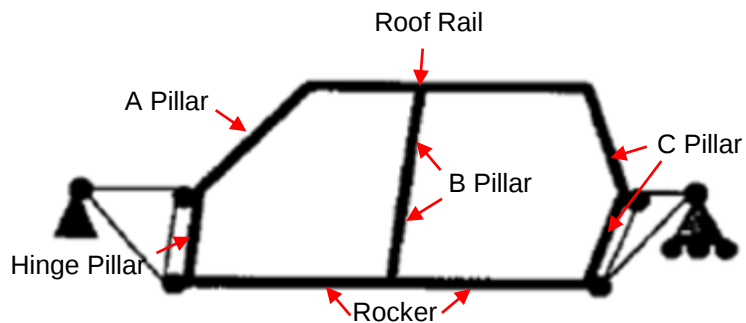
2 요소망 생성
크기 > 20
Add elems to current
component
Property > 단면형상 이름
과 동일하게



3 요소망 생성시 단면 형상이
원하는 좌표축에 놓이도록
주의(x축과 평행한 빔은 y-
axis로 선택, y축과 평행한
빔은 x-axis로 선택)

4 Mesh,
Return

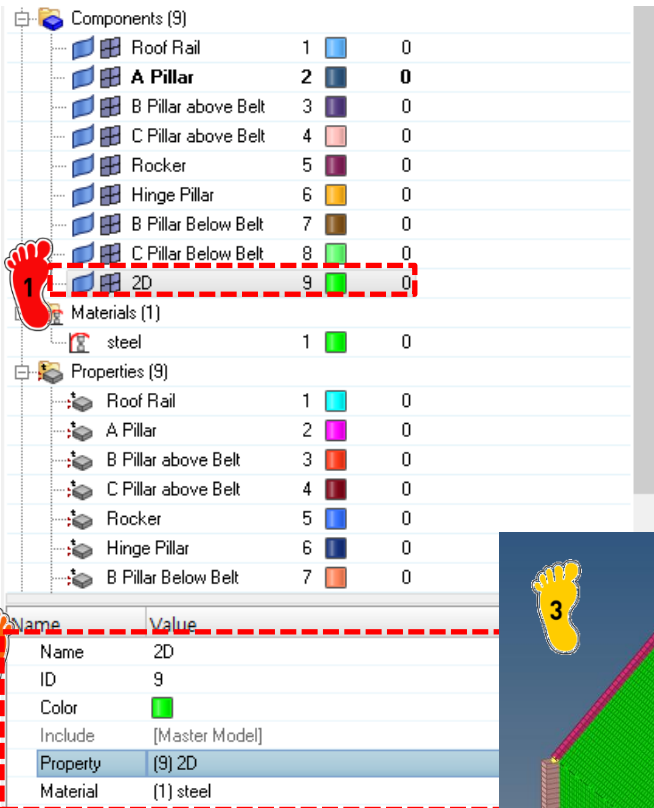
요소망 생성 (3)



앞의 과정(1,2) 반복해서
8개 빔 요소망 생성

그림과 비슷한 형상이
나와야 함

요소망 생성 (4)



1 우클릭,
Create > Component

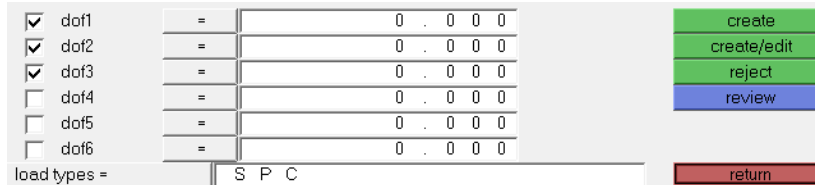
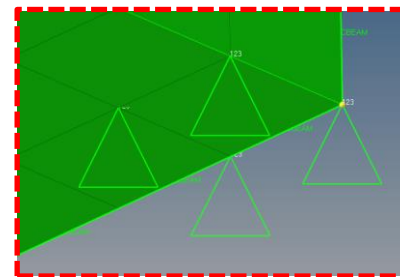
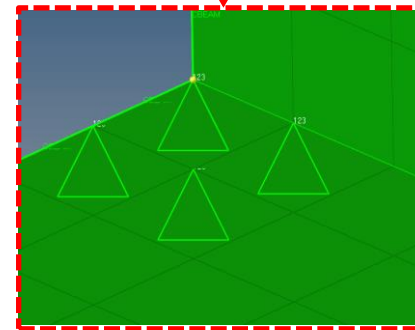
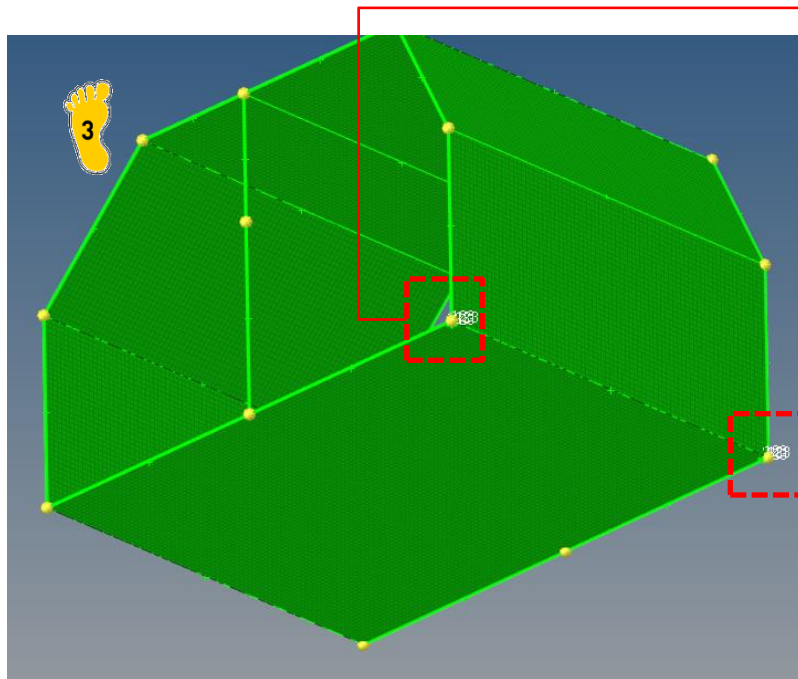
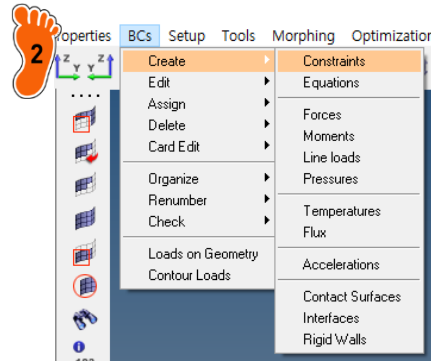
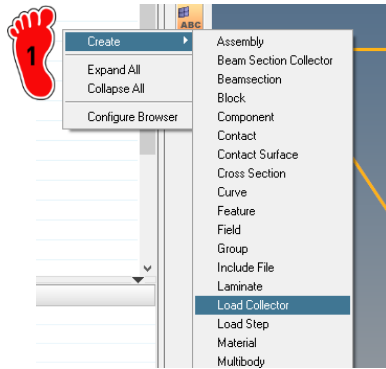
2 Name > 2D
Property > 2D
Material > steel

3 2D > planes
20 mm 인 크기로 평면요소
생성

* Tool -> eadges ->
tolerance -> equivalence
(모서리 병합)

* Geom -> temp nodes ->
clear all (Nodes 제거)

구속조건 및 하중조건 설정 (1)

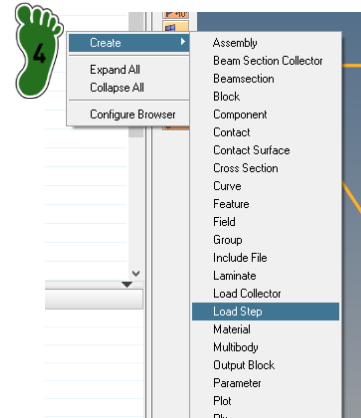
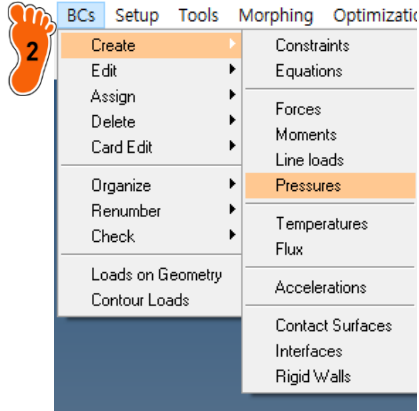
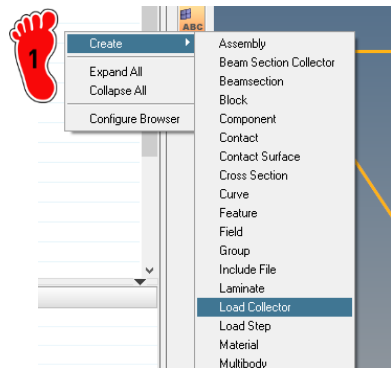


1 Create > Load Collector
Name > spc

2 BCs > Create
> Constraints

3 뒤쪽 양 끝 요소의 절점 4개를
핀 구속조건으로 구속

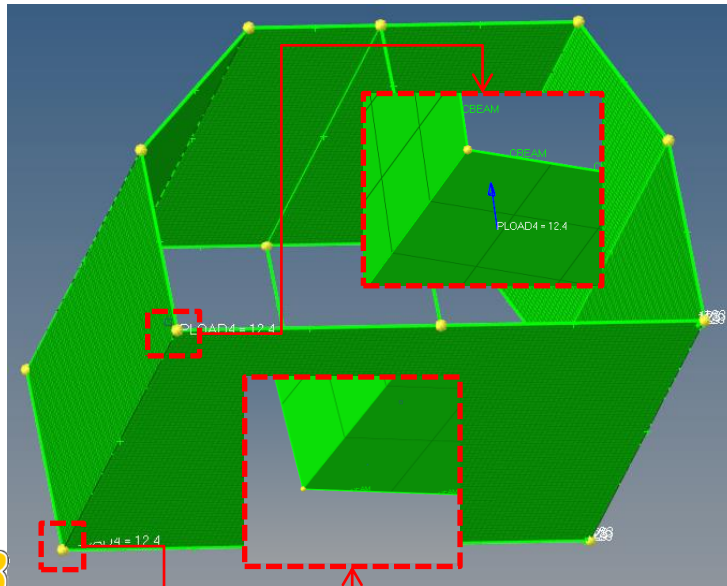
구속조건 및 하중조건 설정 (2)



1 Create > Load Collector
Name > Pressures

2 BCs > Create
> Pressures

3 하중/면적
 $= (4955/400) = 12.4 \text{ N/mm}^2$
 인 압력하중으로 비틀림 하
 중을 적용
 (양쪽 부호 다르게)

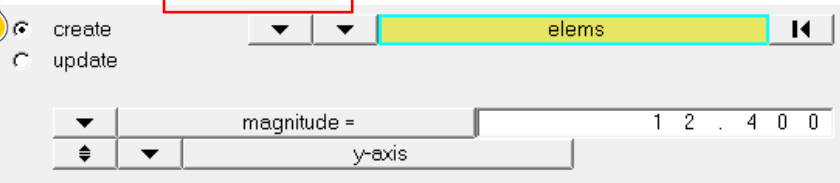


Name	Value
Solver Keyword	SUBCASE
Name	loadstep1
ID	1
Include	[Master Model]
User Comments	Hide In Menu/Export
Subcase Definition	
Analysis type	Linear Static
SPC	(1) SPC
LOAD	(2) Pressures
SUPPORT1	<Unspecified>
PRETENSION	<Unspecified>
MPC	<Unspecified>
DEFORM	<Unspecified>
STATSUB (PRELOAD)	<Unspecified>
STATSUB (PRETENS)	<Unspecified>

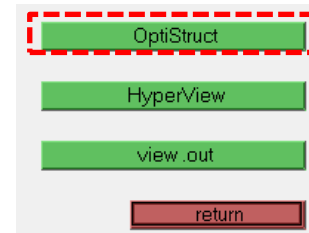
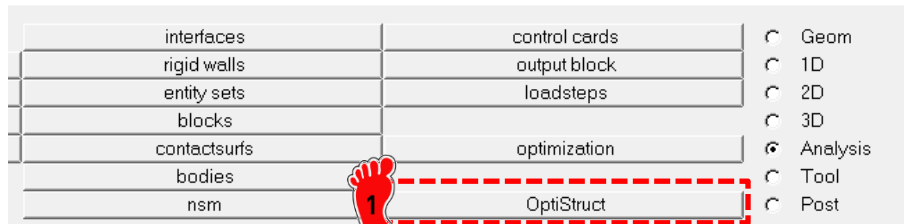
5

4 Create > Load Step

5 Analysis type
 > Linear Static
 SPC > spc
 LOAD > Pressures

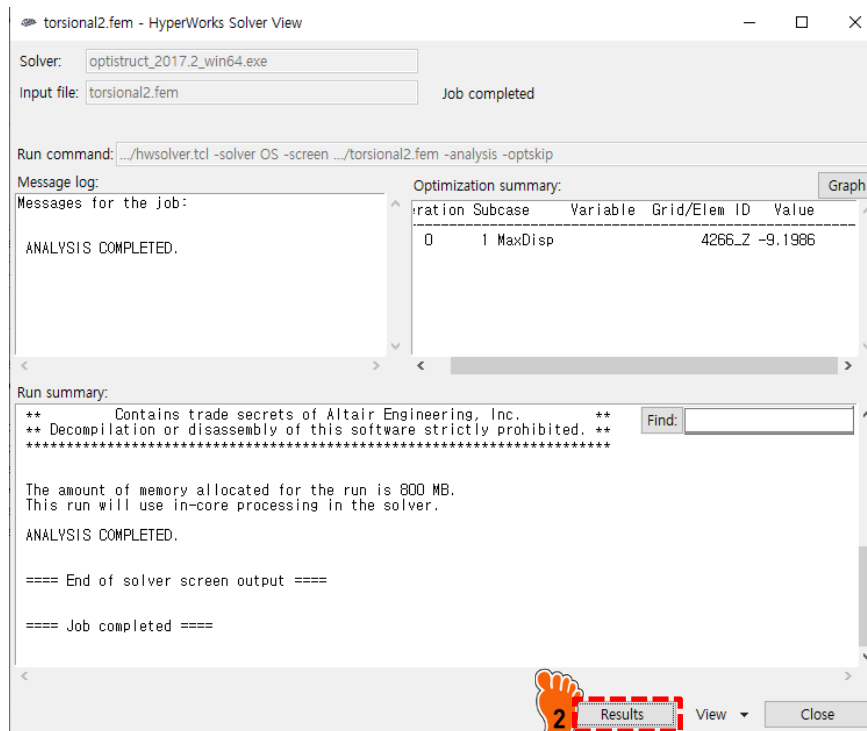


해석 케이스 정의 및 해석 실행

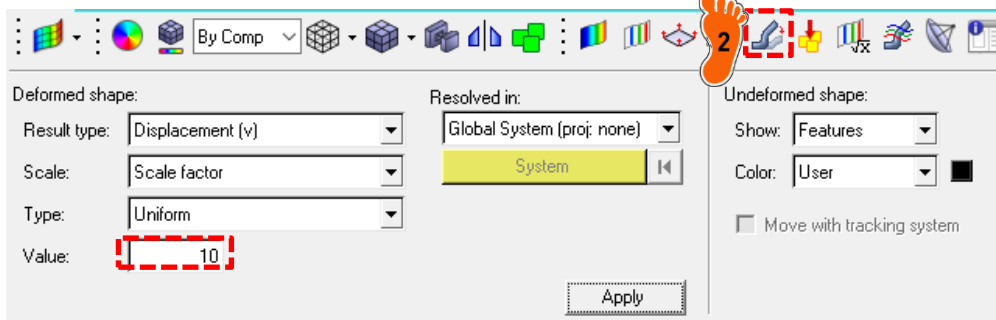
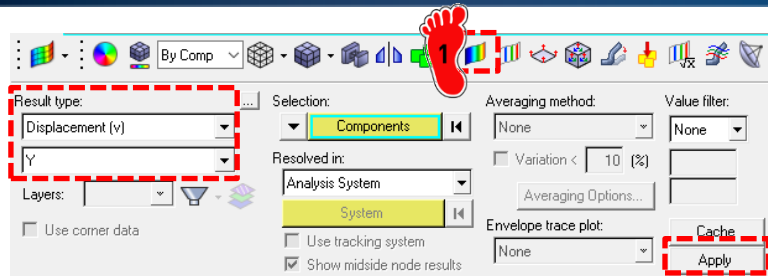


1 Analysis > OptiStruct 클릭
OptiStruct

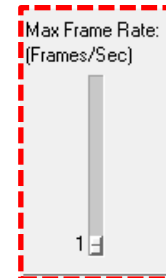
2 Results 클릭



후처리



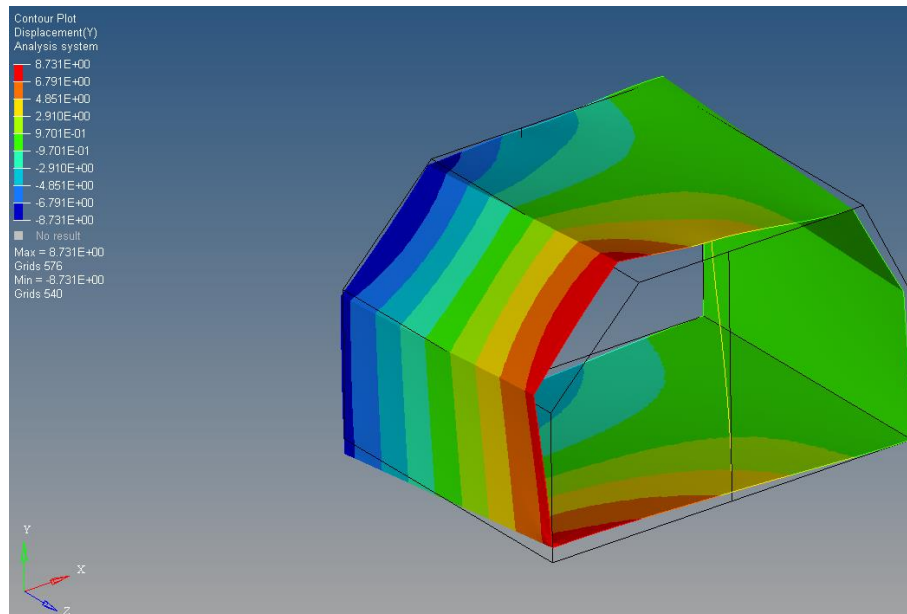
Contour 클릭
Displacement, Y
Apply



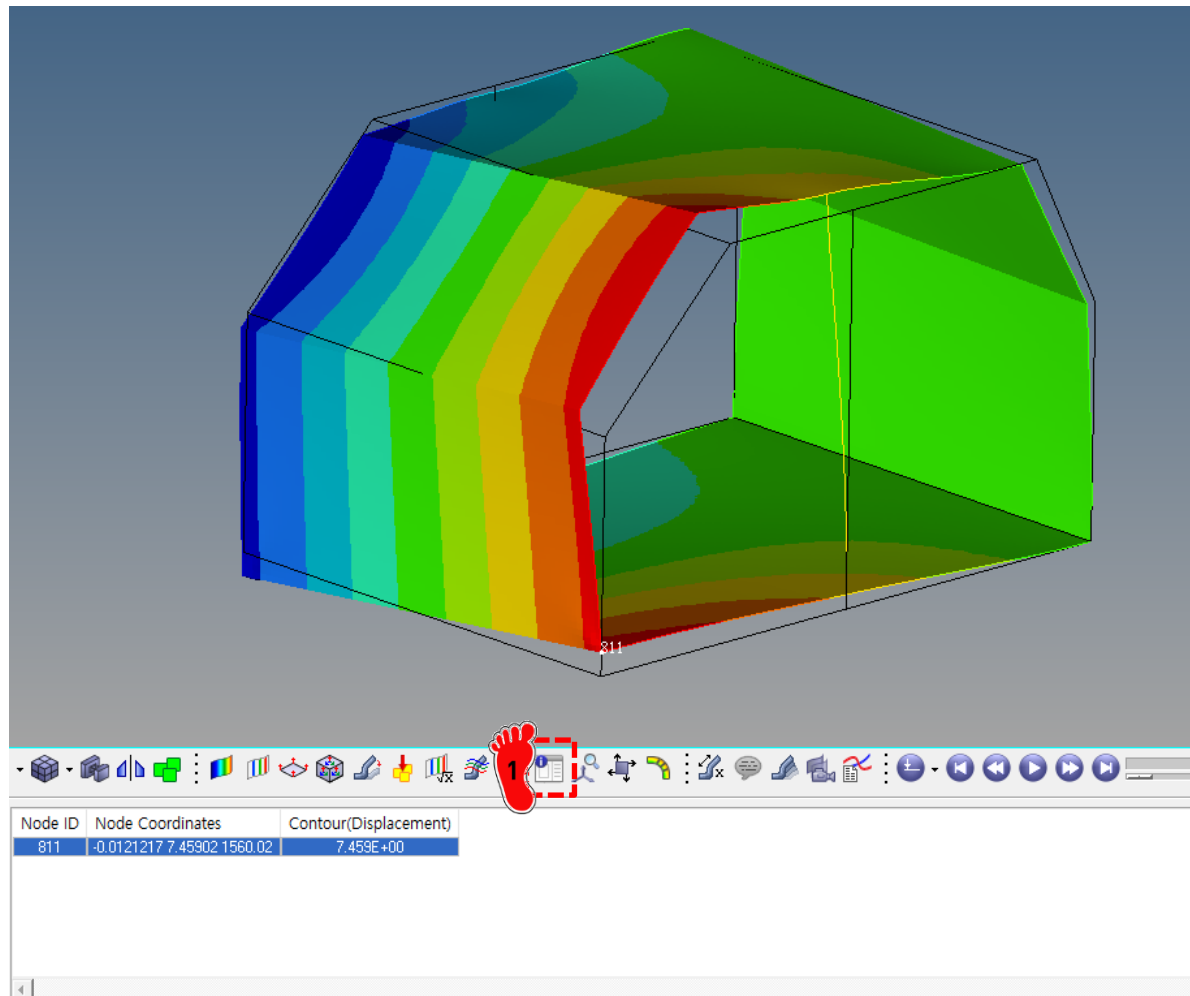
Deformed 클릭
Value > 10
Apply



Animation Control 클릭
Max Frame Rate > 1
Start animation



후처리



1 Query 클릭

2 앞쪽 끝 노드 클릭

3

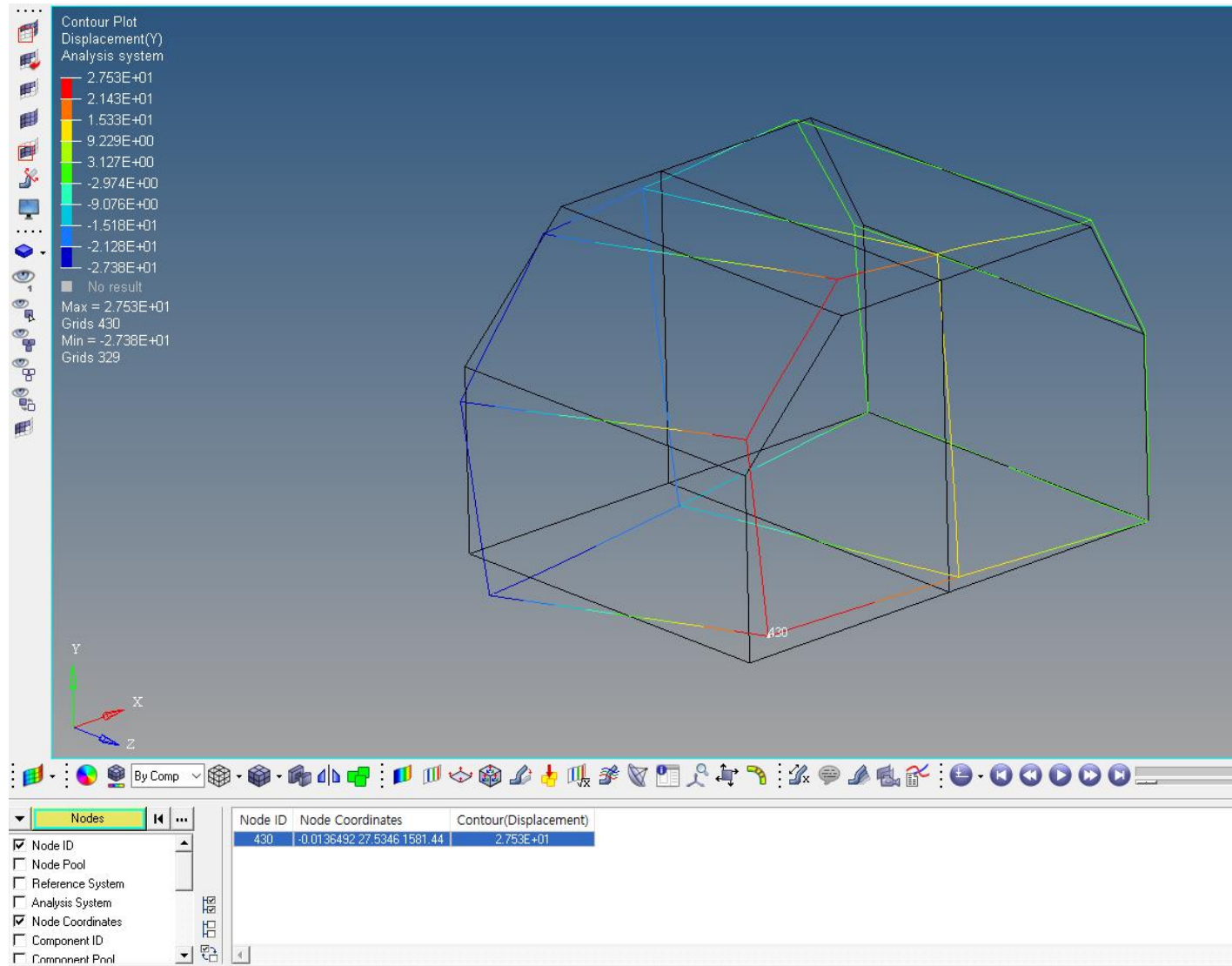
$$K = \frac{T}{\theta} = \frac{Fw}{(2\delta/w)}$$

$$= \frac{7730000}{(2 \times 7.459/1560)}$$

$$= 8.08e8 \text{ Nmm/rad}$$

(이론: $6.55e8 \text{ Nmm/rad}$)

숙제



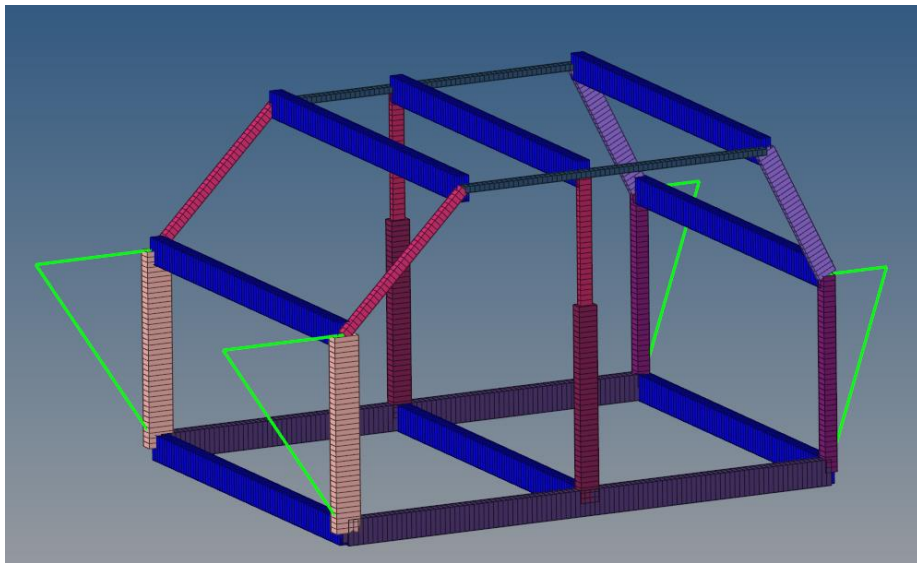
1차원 Beam으로 모델링 후 비틀림 강성을 구하고 앞선 예제와 비교
(Side frame 외 보강 빔(z축)의 단면 형상은 rocker로 가정하고 해석 수행)

ADDITIONAL EXAMPLE #1 (MODAL ANALYSIS)

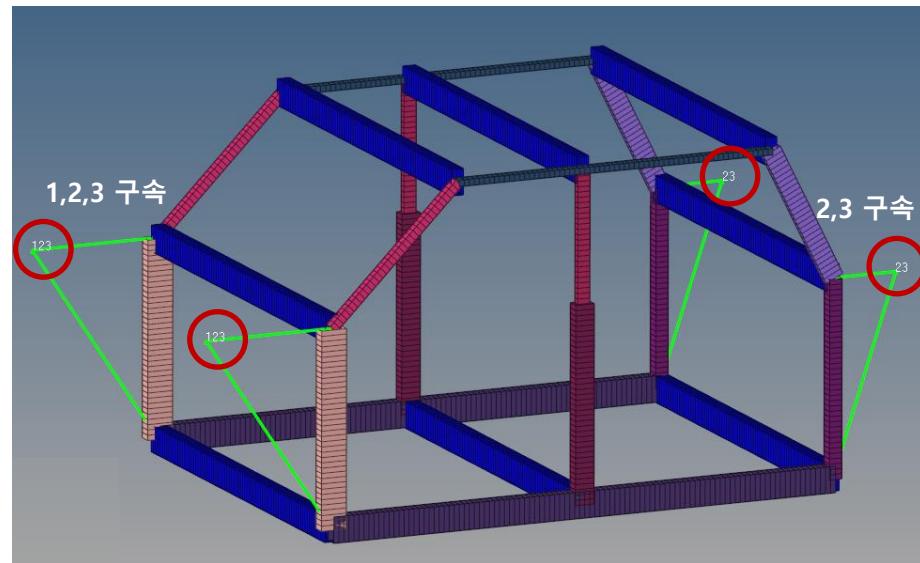
MODAL ANALYSIS

- 1차원 beam으로 모델링 후 modal analysis 수행 (자유진동 vs. 끝단 구속)

자유진동 가정

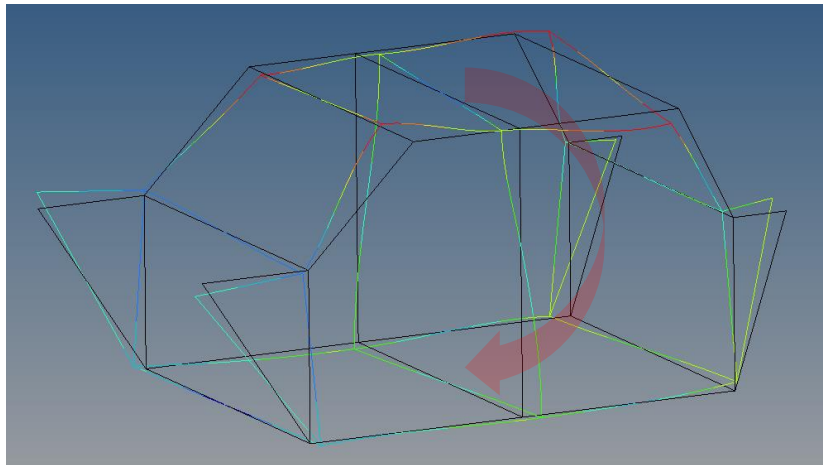


Front & Rear 구속

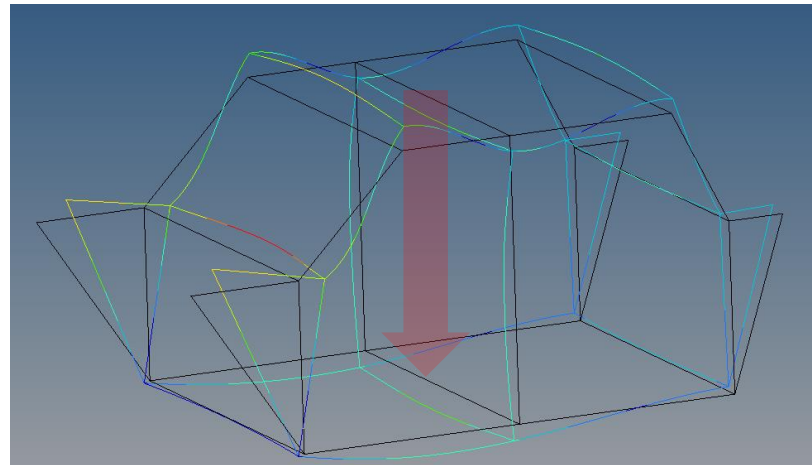


MODAL ANALYSIS

- 자유진동 가정

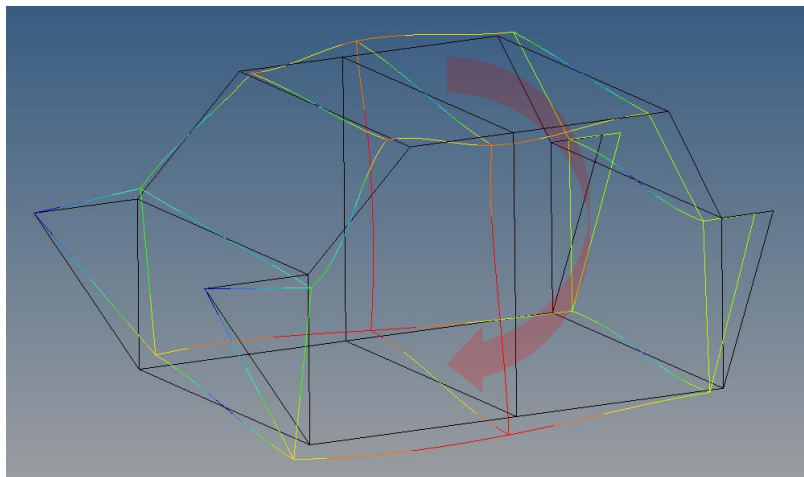


Mode 6(68.89 Hz): Torsion

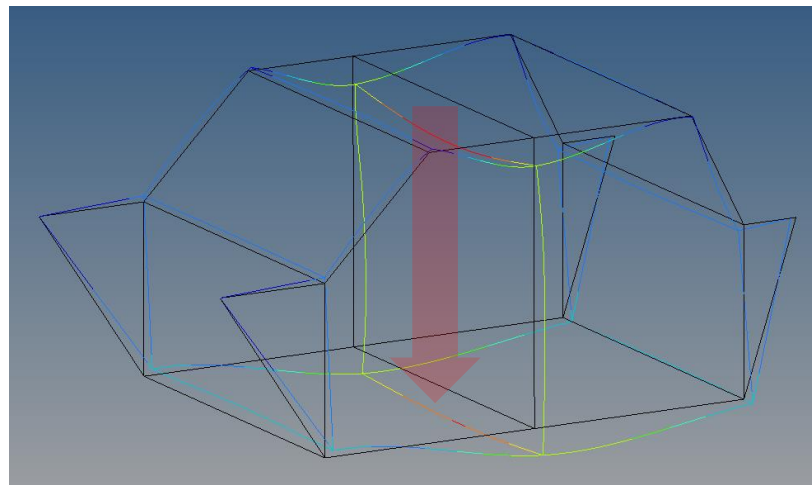


Mode 7(70.04 Hz): Bending

- Front & Rear 구속



Mode 5(54.77 Hz): Torsion

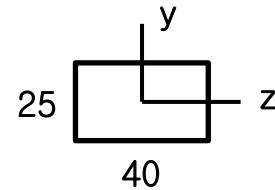
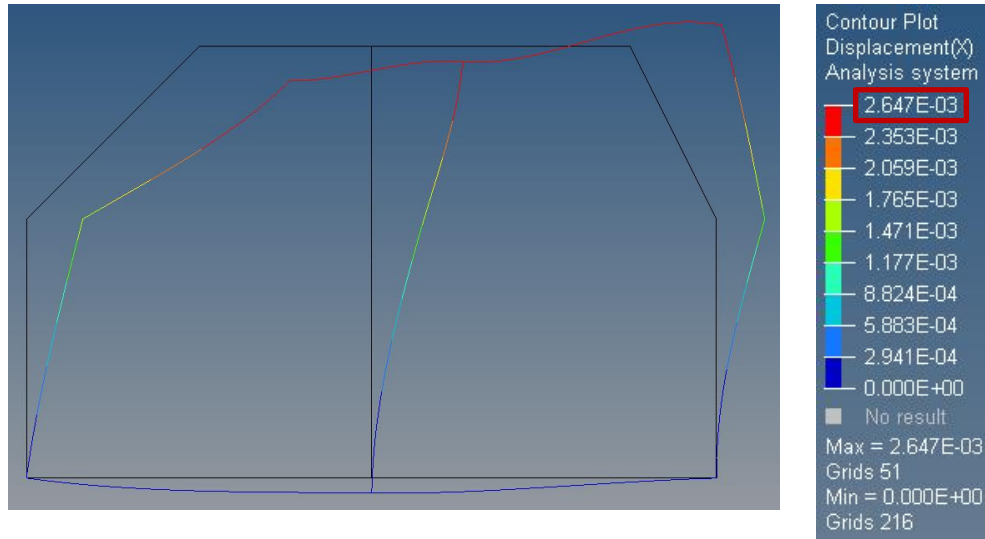


Mode 8(75.92 Hz): Bending

ADDITIONAL EXAMPLE #2 (EFFECT OF BEAM SECTION)

EFFECT OF BEAM SECTION

- Side frame 모델 비교(effective shear rigidity): Roof rail 변경

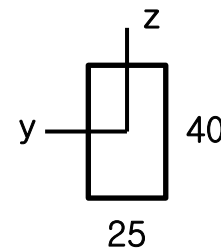
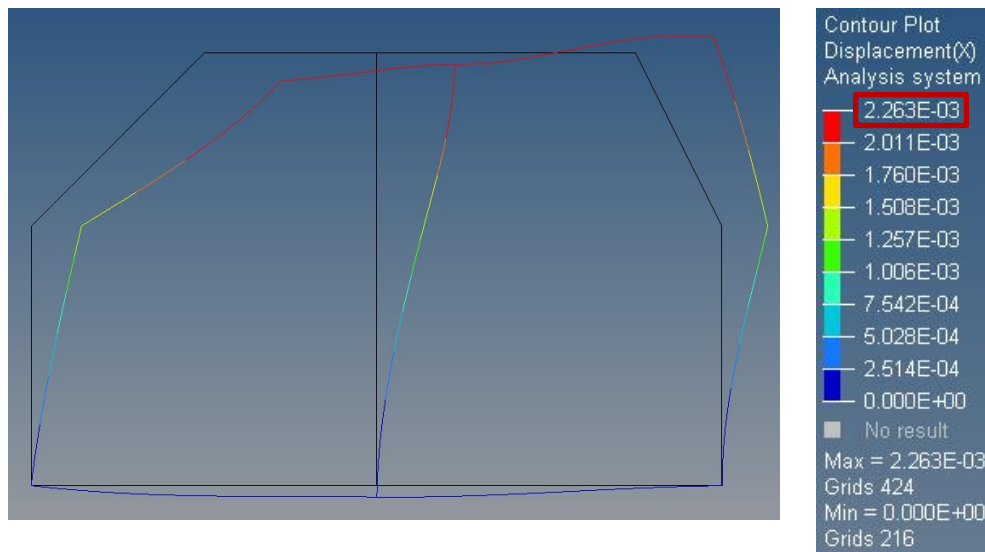


Roof Rail
(y-axis)

Original axis

$$(G_f)_{eff} = \left(\frac{1N}{0.002647mm} \right) \cdot \frac{1250mm}{2000mm} = 236.1N / mm$$

$$\delta = 0.002647mm$$



Roof Rail
(z-axis)

Rotate axis

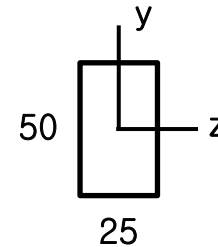
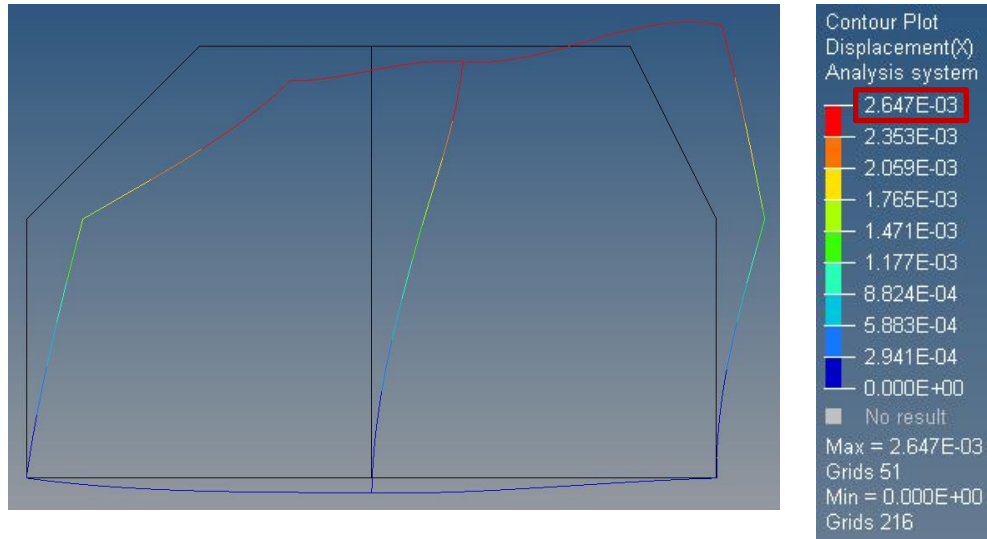
$$(G_f)_{eff} = \left(\frac{1N}{0.002263mm} \right) \cdot \frac{1250mm}{2000mm} = 276.2N / mm$$

$$\delta = 0.002263mm$$

Difference: 16.9%

EFFECT OF BEAM SECTION

- Side frame 모델 비교(effective shear rigidity): B Pillar above belt 변경

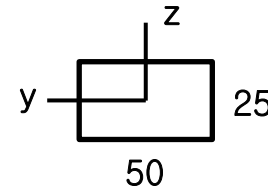
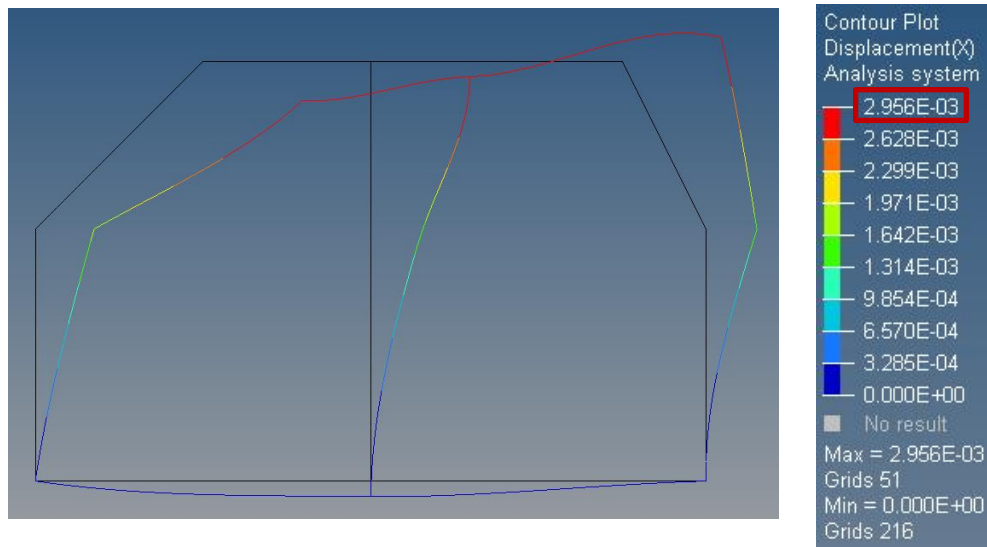


B Pillar above belt
(y-axis)

Original axis

$$(G_f)_{eff} = \left(\frac{1N}{0.002647mm} \right) \cdot \frac{1250mm}{2000mm} = 236.1N / mm$$

$$\delta = 0.002647mm$$



B Pillar above belt
(z-axis)

Rotate axis

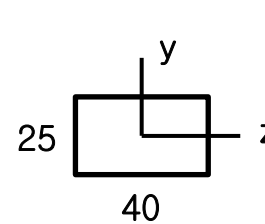
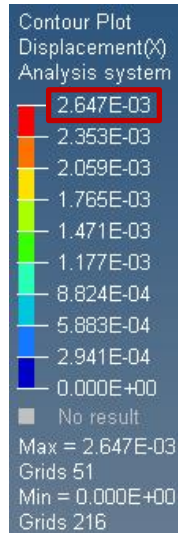
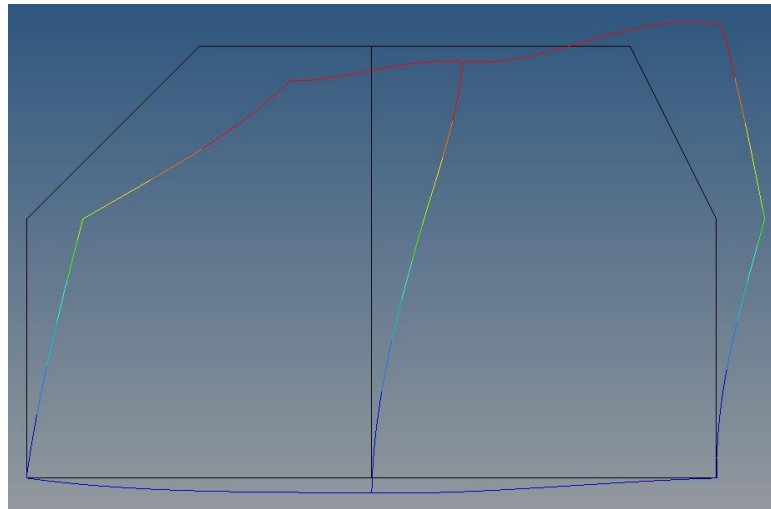
$$(G_f)_{eff} = \left(\frac{1N}{0.002956mm} \right) \cdot \frac{1250mm}{2000mm} = 211.4N / mm$$

$$\delta = 0.002956mm$$

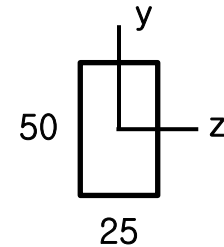
Difference: 10.4%

EFFECT OF BEAM SECTION

- Side frame 모델 비교(effective shear rigidity): Roof Rail 및 B Pillar above belt 변경



Roof Rail
(y-axis)

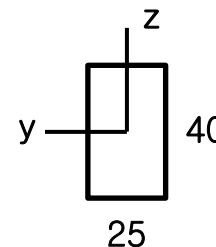
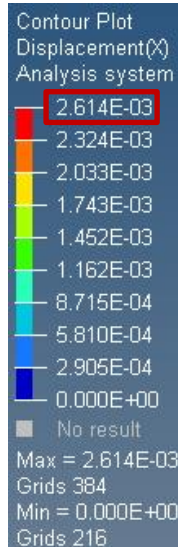
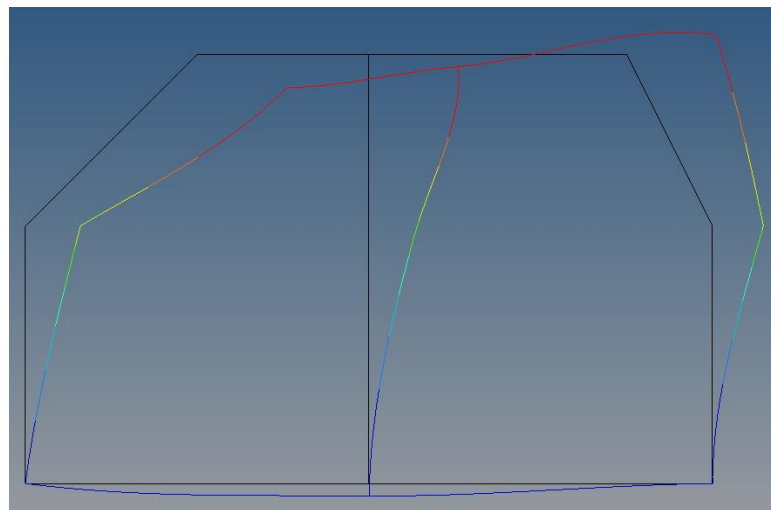


B Pillar above belt
(y-axis)

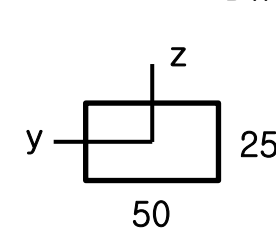
Original axis

$$(G_f)_{eff} = \left(\frac{1N}{0.002647mm} \right) \cdot \frac{1250mm}{2000mm} = 236.1N / mm$$

$$\delta = 0.002647mm$$



Roof Rail
(z-axis)



B Pillar above belt
(z-axis)

Rotate axis

Difference: 1.2%

$$(G_f)_{eff} = \left(\frac{1N}{0.002614mm} \right) \cdot \frac{1250mm}{2000mm} = 239.1N / mm$$

$$\delta = 0.002614mm$$