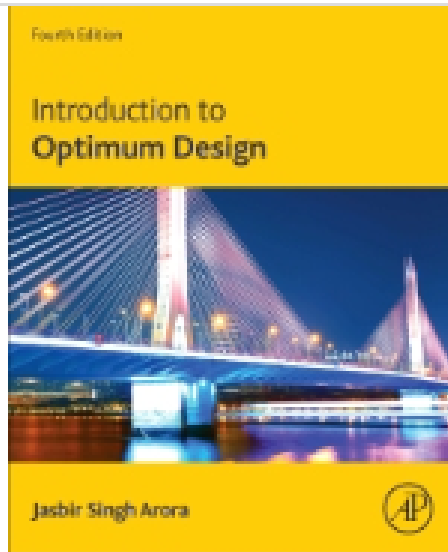


# Textbook



## Introduction to Optimum Design 4th Edition

☆☆☆☆☆ [Write a review](#)

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Hardcover ISBN: 9780128008065

eBook ISBN: 9780128009185

[View on ScienceDirect](#) ↗



Imprint: Academic Press

Published Date: 28th April 2016

Page Count: 968

<https://www.elsevier.com/books/introduction-to-optimum-design/arora/978-0-12-800806-5>

<https://www.sciencedirect.com/book/9780128008065/introduction-to-optimum-design#book-info>

# Table of Contents (1)

Part I. The Basic Concepts				
Ch	Title	U/G1	G1	G2
1	Introduction to Design Optimization	O	O	
2	Optimum Design Problem Formulation	O	O	
3	Graphical Optimization and Basic Concepts	O	O	
4	Optimum Design Concepts: Optimality Conditions	O	O	
5	More on Optimum Design Concepts: Optimality Conditions		O	

U/G1: Undergraduate/First-Year Graduate Level Course  
G1: First Graduate Level Course  
G2 Second Graduate Level Course

# Table of Contents (2)

Part II. Numerical Methods for Continuous Variable Optimization				
Ch	Title	U/G1	G1	G2
6	Optimum Design with Excel Solver	O		O
7	Optimum Design with MATLAB	O		O
8	Linear Programming Methods for Optimum Design	O	O	O
9	More on Linear Programming Methods for Optimum Design		O	O
10	Numerical Methods for Unconstrained Optimum Design	O	O	O
11	More on Numerical Methods for Unconstrained Optimum Design		O	O
12	Numerical Methods for Constrained Optimum Design	O	O	O
13	More on Numerical Methods for Constrained Optimum Design		O	O
14	Practical Applications of Optimization			O

# Table of Contents (3)

Part III. Advanced and Modern Topics on Optimum Design				
Ch	Title	U/G1	G1	G2
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16	Global Optimization Concepts and Methods			O
17	Nature-Inspired Search Methods			O
18	Multi-Objective Optimum Design Concepts and Methods			O
19	Additional Topics on Optimum Design			O

# Introduction

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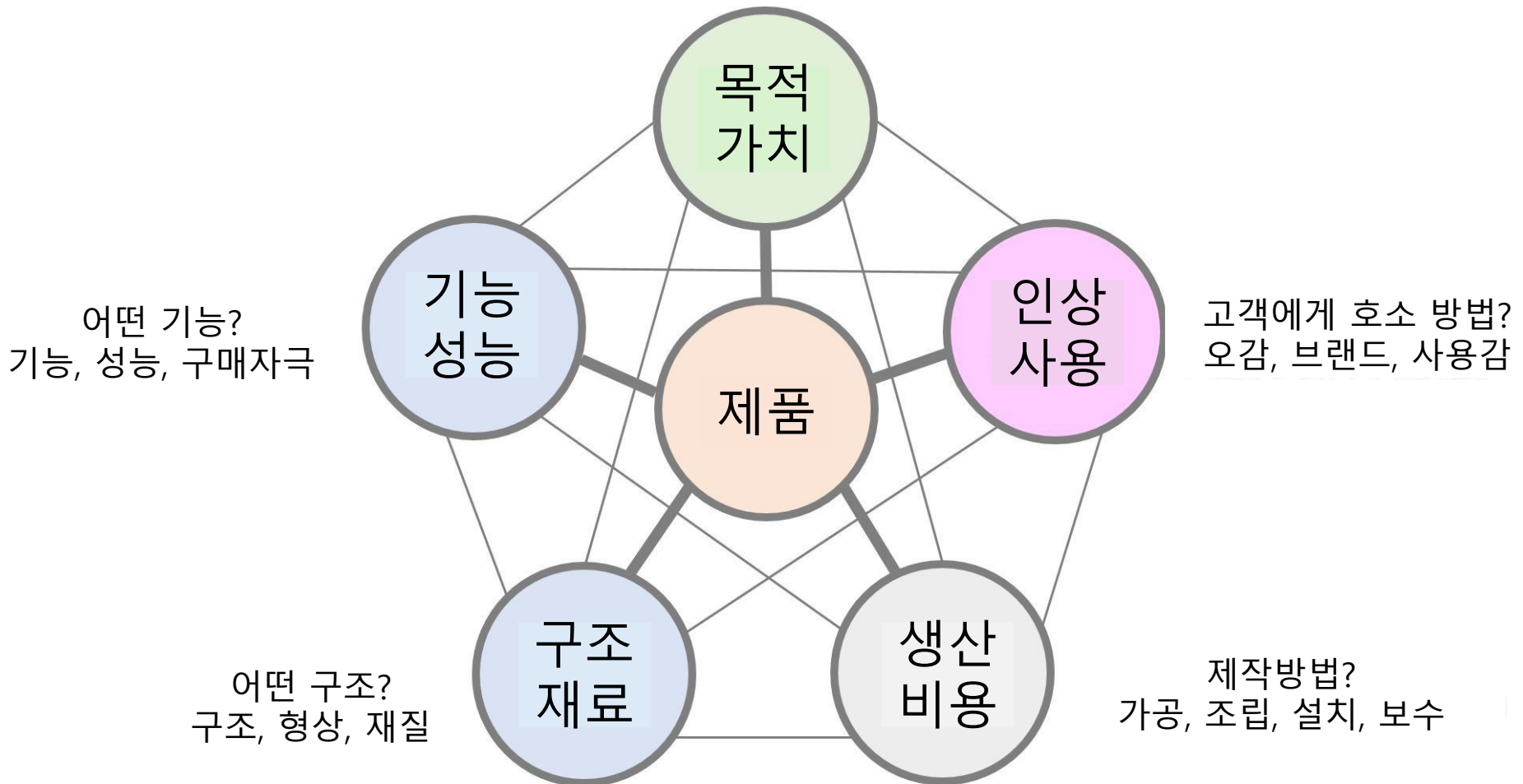
- Engineer
  - Design devices and products that perform tasks in an efficient fashion
  - Constrained by the limitations of the physical world and must keep costs down
  - Confronting optimization problems that balance performance and limitations
- Mechanical Design
  - Selection of materials and geometry
  - which satisfies specified and implied functional requirements
  - while remaining within the confines of inherently unavoidable limitations

# 모델링

- 설계 시작부터 종료까지 프로세스를 통해 설계대상을 구성하는 파라미터와 이들간 관계를 각 프로세스로 이해가능한 형식으로 표현함으로써 각 설계결과를 평가 가능하도록 하는 것. 즉, 모델링의 결과가 **모델**임.
- 설계 자체를 제삼자가 이해 가능한 형식으로 표현하여 설계를 효율적으로 창조적인 것으로 하기 위한 프로세스를 가능한 이론적으로 표현하고 가시화하는 방법
- 기술(記術)모델: 언어, 그림으로 표현, 의사 전달
- 해석(解析)모델: 식으로 표현, 계산 가능 (CAE)
- 형상(型狀)모델: 생산 가능한 형태로 표현 (CAD)

# 제품설계와 모델링

이 제품의 목적?  
고객, 경제성, 환경, 성능, 가격



# 모델링 사례: 가치 (헤어드라이어)

- QFD: 고객 요청 → 기능(공학적 지표) → 부품(구조)으로 전개
  - 건조속도, 안전, 그립감, 소음, 신뢰도, 전기료, 휴대성, 조작성
  - 유량, 공기온도, 밸런스, 중량, 크기, 소음레벨, 소비전력, 스위치 개수
  - 모터, 팬, 히터, 스위치, 하네스, 관체

	顧客の声	重み付け	工学的指標 (機能)							ベンチマーク				
			流量	空気温度	持ったバランス	重量	大きさ	騒音レベル	消費電力	スイッチの数	1 悪い	2	3	4 悪い
	早く乾く	9	9	9							C	B	A	
	安全である	3	1	9	3			1			A	B,C		
	持ち易い	9		3	9	9	3				A	B	C	
	静かである	3	3					9			A	B	C	
	信頼できる	3	1	1				1			C	A	B	
	電気代が安い	3							9			B	A,C	
	携帯できる	1				9	9			3	C	B		A
	操作が簡単	1			3	3					C	B		A
目標値			>1.2 m³ / min	>90 °C	<10 Nm	<500gram	<300mmx100mmx100mm	<60 dB	<1500 W	<4				
ベンチマーク	良い	5	A	B	C	A		C	A					
	4		B	A	B			A	B		A	C		
	3					B		B	B					
	2		C	C	A			C	A					
	悪い	1				C			C					
	積算値	96	138	93	93	36	33	27	3					
	正規化	0.18	0.27	0.18	0.18	0.07	0.06	0.05	0.01					

	工学的指標 (機能)	正規化後の重み	部品 (構造)					
			モータ	ファン	ヒータ	スイッチ	ハネス	筐体
	流量	0.18	9	9	3			3
	空気温度	0.27	3	3	9			1
	持ったバランス	0.18	9	3	1			9
	重量	0.18	9	3	3	1	1	9
	大きさ	0.07	3	3	3	1	1	9
	騒音レベル	0.06	9	9				3
	消費電力	0.05	3	3	9	1	1	
	スイッチの数	0.01	3		3	9		
	積算値	6.64	6.47	4.36	0.35	0.57	4.60	
	正規化	31.6%	21.3%	20.8%	1.7%	2.7%	21.9%	
	材料費	30	6	4	2	2	2	
	加工費		2	4		3	10	
	開発費		1	1			1	
	コスト	30	9	9	2	5	13	
	正規化	44.1%	13.2%	13.2%	2.9%	7.4%	19.1%	

출력  
[가치, 비용]

입력  
[고객 요청]



# 모델링 사례: 비용 (주조)

- 파라미터: 재료, 생산개수, 상각기간
- 선택 가능한 설계변수: 재료, 제조방법
- 정확도가 높지는 않지만 상대적 비교는 가능

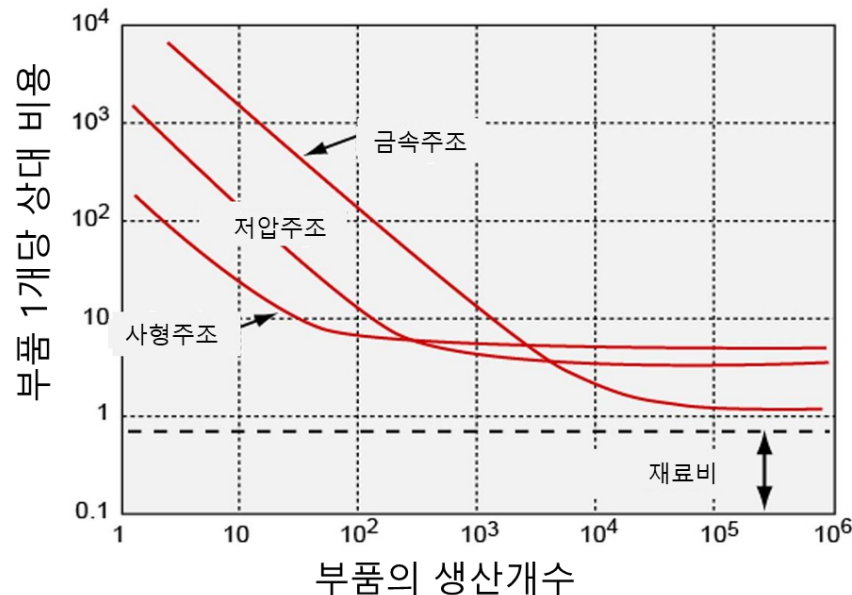
재료비

공구비

설비비

간접비

부품 1개당 비용 
$$C = \left[ \frac{mC_m}{1-f} \right] + \left[ \frac{C_t}{n} \right] + \frac{1}{dn/dt} \left[ \frac{C_c}{Lct} \right] (1+d)^{ct} + \frac{dC_{oh}/dt}{dn/dt}$$

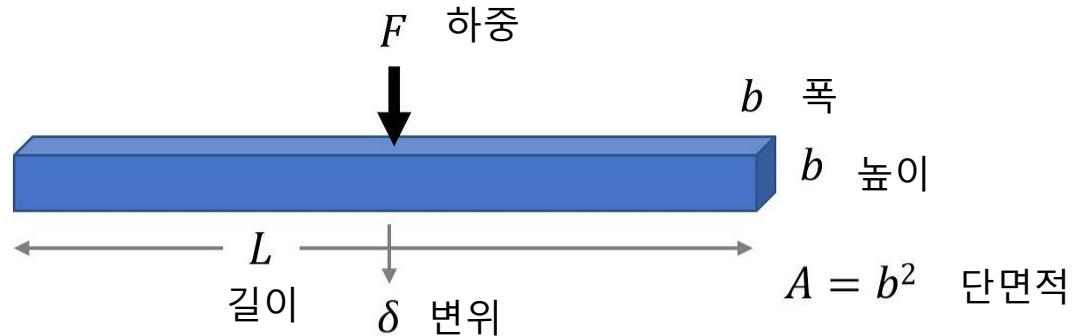


설비비:  $C_c$   
 공구비:  $C_t$   
 생산율:  $dn/dt$   
 배치사이즈:  $n$   
 원재료:  $m$   
 상각기간:  $ct$   
 할인율:  $d$   
 간접비:  $dC_{oh}/dt$   
 손실율:  $f$

# 모델링 사례: 성능 (경량보)

## 요구사항

가볍고 튼튼한 보(빔)



## 제약조건

- 길이  $L$ 은 고정
- 굽힘강성  $> S^*$
- 면적  $A$ 에 관한 제약식

$$S = \frac{F}{\delta} = \frac{CEI}{L^3} = \frac{CEA^2}{12L^3}$$

## 목적함수

질량  $m$ 을 최소화  $m = AL\rho$

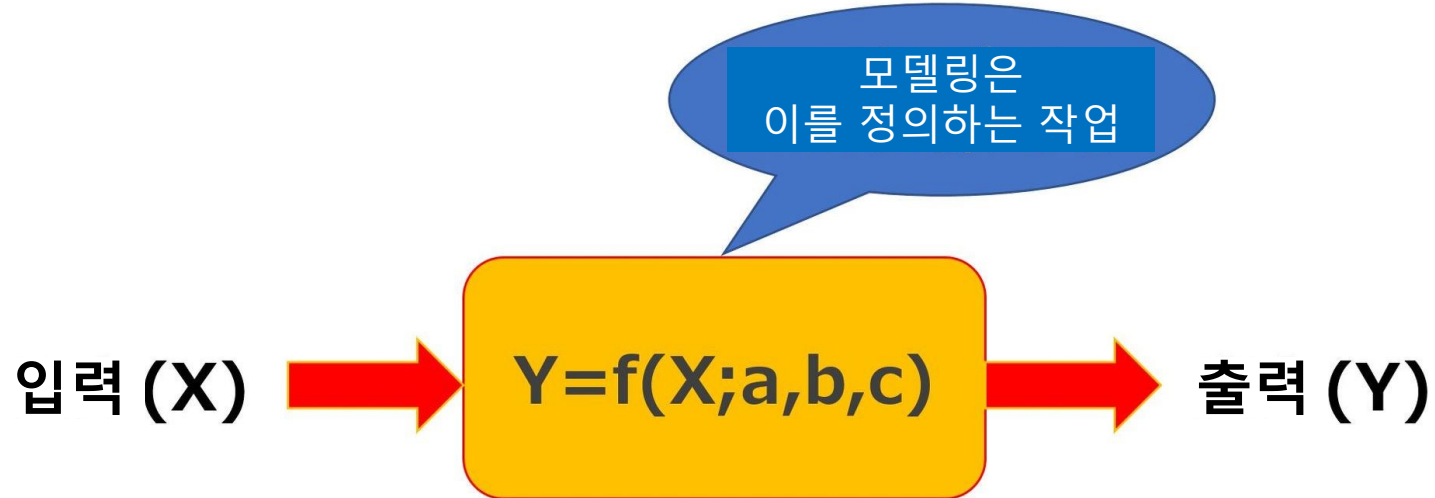
굽힘강성:  $S$   
 밀도:  $\rho$   
 경계조건에 따른 정수:  $C$   
 (종)탄성계수:  $E$   
 단면2차모멘트:  $I$

## 성능지표

$$m = \left[ \frac{12L^5 S^*}{C} \right]^{1/2} \left[ \frac{\rho}{E^{1/2}} \right] \rightarrow M = \left[ \frac{E^{1/2}}{\rho} \right] \text{ 설계지표: 이 값이 큰 재료를 선정}$$

# 모델링이란?

- 알고 싶은 것(예: 부품 각 요소의 가치, 부품 한개당 비용, 설계지표)을 지배하는 지표를 명확히 하여 알고 있는 정보로부터 알고 싶은 것을 예측하는 행위



모델파라미터 : a, b, c

**모델링 = 설계 (디자인)**

# Engineering Model (1)

- Model
  - Abstract description of the real world giving an approximate representation of more complex functions of physical systems
  - Increase our understanding of how a system works
  - Physical: scale model, prototype
  - Symbolic: drawings, verbalization, logic, mathematics
- Mathematical model
  - A model that represents a system by mathematical expressions of relevant natural laws, experience, and geometry
  - May contain many alternative designs, so criteria must be introduced in the model
  - Best, or optimum, design can be identified with the aid of mathematical methods

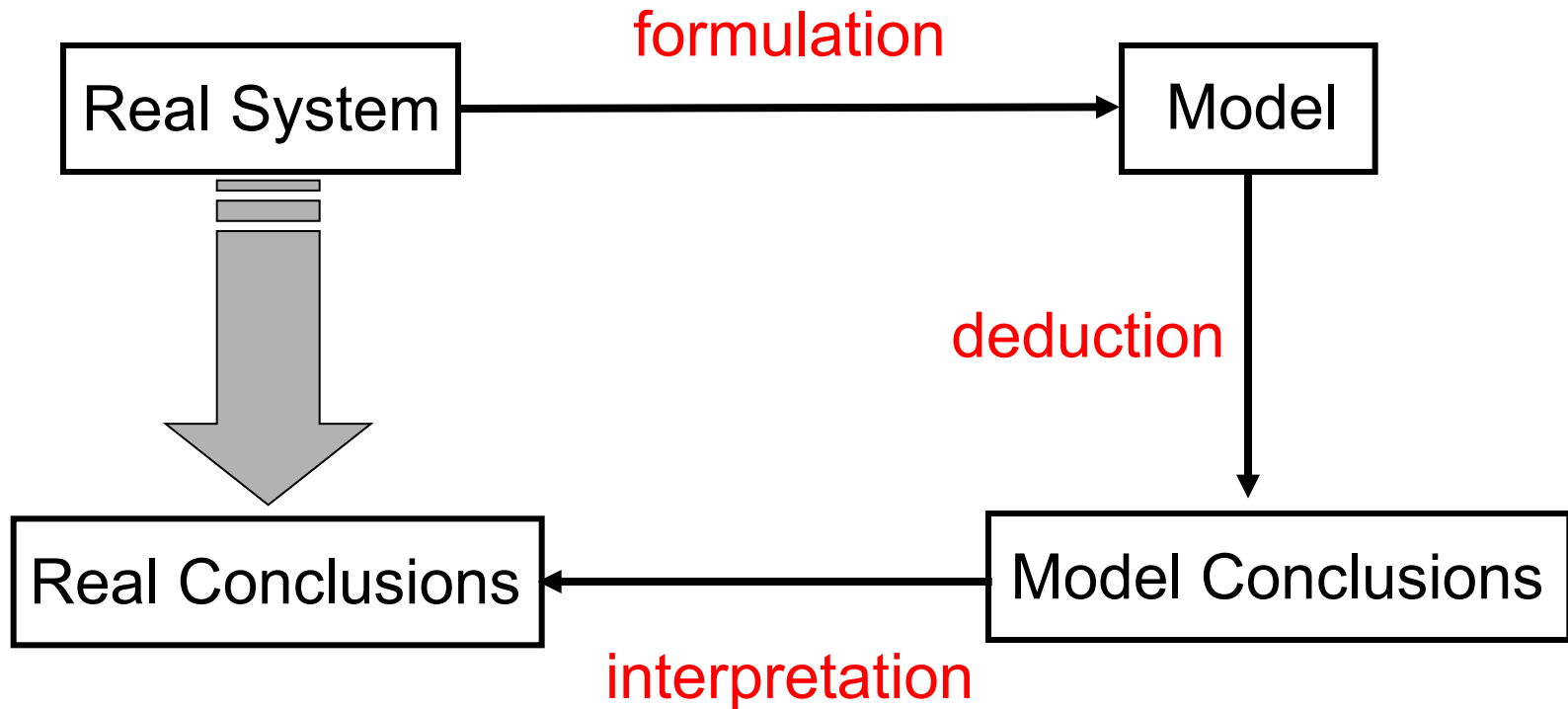
# Engineering Model (2)

- Real-life engineering design problem
  - very unstructured
- Most difficult and challenging part
- Depends on experience as well as skill
- Thorough understanding of the first principles and fundamentals of engineering
- Describes the physical behavior of the system ► mathematical model

# Engineering Model (3)

- Elements of models
  - Variables / Parameters / Constants / Mathematical relations
- Hierarchical levels
  - Every system is analyzed at a particular level of complexity
  - System → Subsystems → Components
  - “cut across” the links with environment, input/output characterization: free-body diagram, control volume

# Modeling Process (1)



# Modeling Process (2)

- Formulation
  - Often considered to be an art
  - What aspects of the real system should be included, which can be ignored?
  - What assumptions can and should be made?
- Deduction
  - Involves techniques that depend on the nature of the model
  - May involve solving equations, running a computer program, expressing a sequence of logical statements – whatever it takes to solve the problem of interest relative to the model
  - It should not be subject to differences of opinion, provided that the assumptions are clearly stated and identified
- Interpretation
  - Again involves a large amount of human judgment
  - The model conclusions must be translated to the real world conclusions, in full cognizance of possible discrepancies between the model and its real world



# Analysis vs. Design

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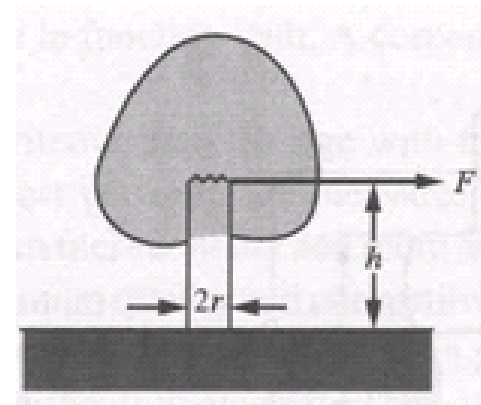
- Engineering analysis
  - To determine the behavior of an existing system
  - Sizes and configurations are given
- Engineering design
  - To calculate sizes and shapes of various parts to meet performance requirements
- ► estimate a design and analyze it to see if it performs according to the specifications

# Analysis and Design Model

- Analysis model
  - Based on the principles of engineering science
    - Maximum wind force the tree can withstand before it breaks ( $F$ ) if we take the tree as given ( $\sigma_{max}$ ,  $h$ ,  $r$  : parameters)
- Design model
  - Constructed from the analysis models for specific prediction tasks
    - Protect the tree from high winds by appropriately trimming the foliage to decrease  $F$  and  $h$  (variables)

Trunk of a tree subject to a wind force  $F$  at a height  $h$

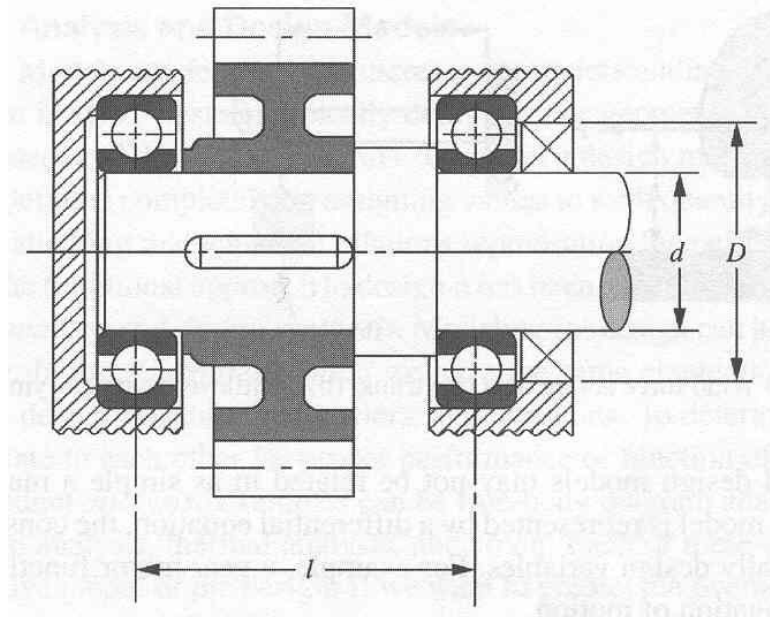
$$\sigma = \frac{My}{I} \xrightarrow{I = \frac{\pi r^4}{4}} \sigma_{\max} = \frac{4Fh}{\pi r^3}$$



# Example: Shaft Design

- Influence of a given viewpoint on the design model

	$d$	$l$	<i>materials</i>
Shaft designer	variable	parameter	parameter
Housing designer	variable	variable	parameter
Project manager	variable	variable	variable



# Decision Making

- Criterion: evaluating alternatives and choosing the “best” one
  - Not unique, influenced by many factors
    - Design application, timing, point of view, judgment of the designer
  - May change with time
    - Automobile design: maximum power and comfort → fuel economy
- Decision-making (Optimization) model
  - A design model that includes an evaluation criterion (*objective*)
- Shaft design example

Criterion	
Weight	
Rigidity	Best meshing of the attached gear
Material and manufacturing costs	Shop manager, ease of manufacturing
Cost	Project or plant manager

# Design Optimization

- Goal of engineering
  - To improve the design so as to achieve the best way of satisfying the original need within the available means
- Elements in the design process
  - Recognition of need / act of creation / selection of alternatives
- Design optimization: selection of the “best” alternative
  - How do we describe different designs ? (design model)
  - What is our criterion for “best” design ? (objective)
  - What are the “available means” ? (set of requirements)

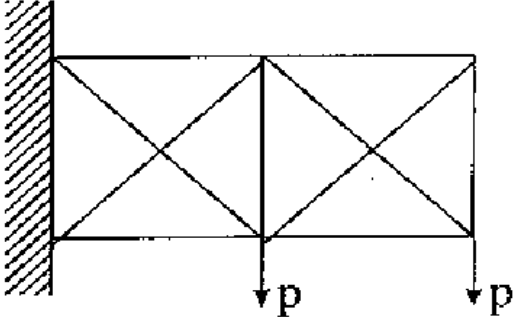
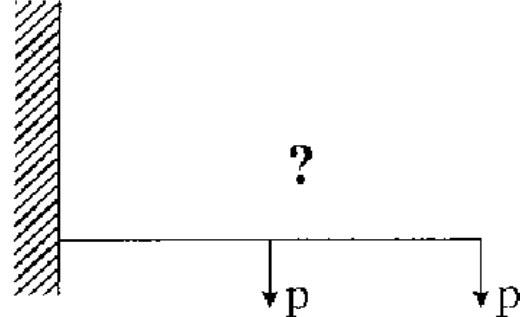
# Optimum Design

- Undesirable effects
  - Stress, deflection, vibration, space occupancy, weight, cost
  - Dependent of the application (degree of significance)
  - Tolerable limit
- Desirable effects
  - Power transmission/ energy absorption/ momentary overload/ speed capacity, usable length of life, factor of safety
- Optimum design
  - Best possible one from the standpoint of the most significant effect
  - Minimize/Maximize the most significant undesirable/desirable effect

# Problem Formulation Steps

- Identification of *design variables*
  - Parameter chosen to describe the design
  - Independent of each other, minimum number
- Identification of an *objective (cost) functions*
  - Criterion to compare various designs
  - as a function of the design variables
  - Single/Multi-objective
- Identification of all *design constraints*
  - All restrictions placed on a design
  - Explicit/Implicit, Linear/Nonlinear, Equality/Inequality
  - Feasible/Infeasible

# 10 Bar Truss Design

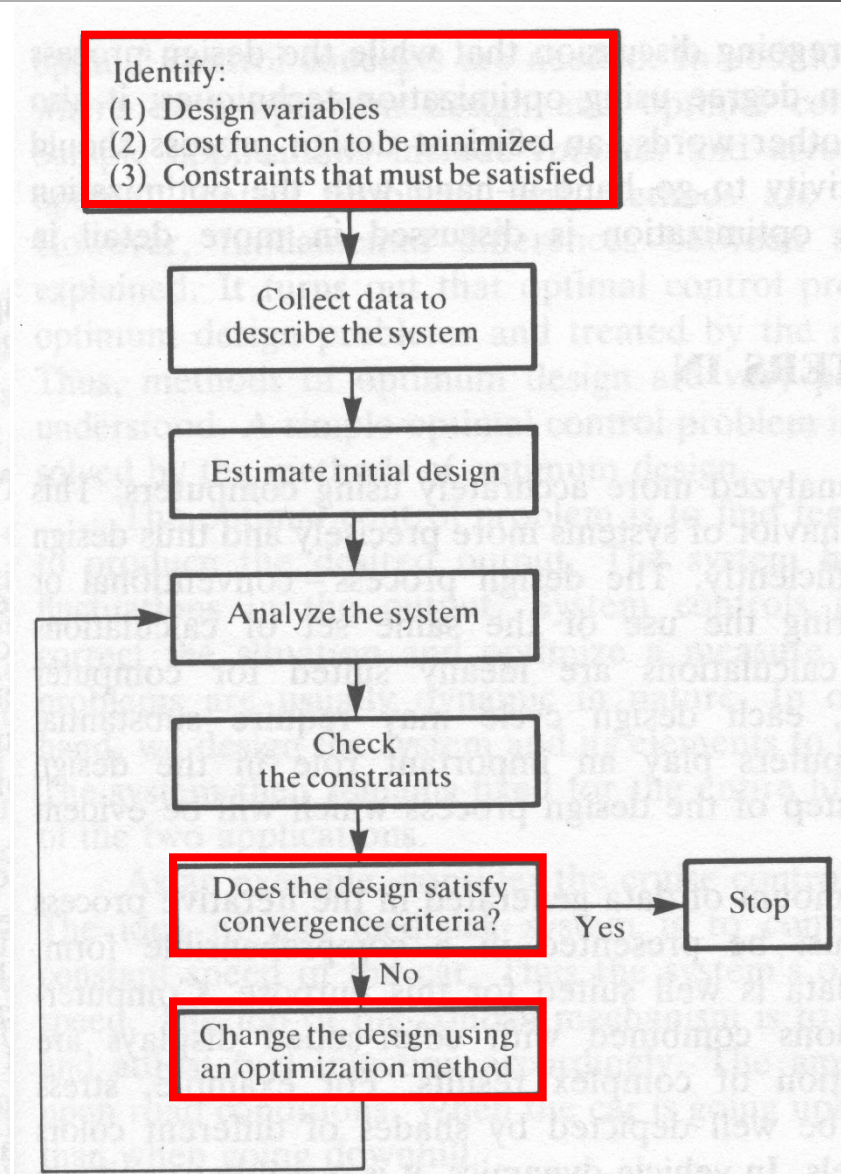
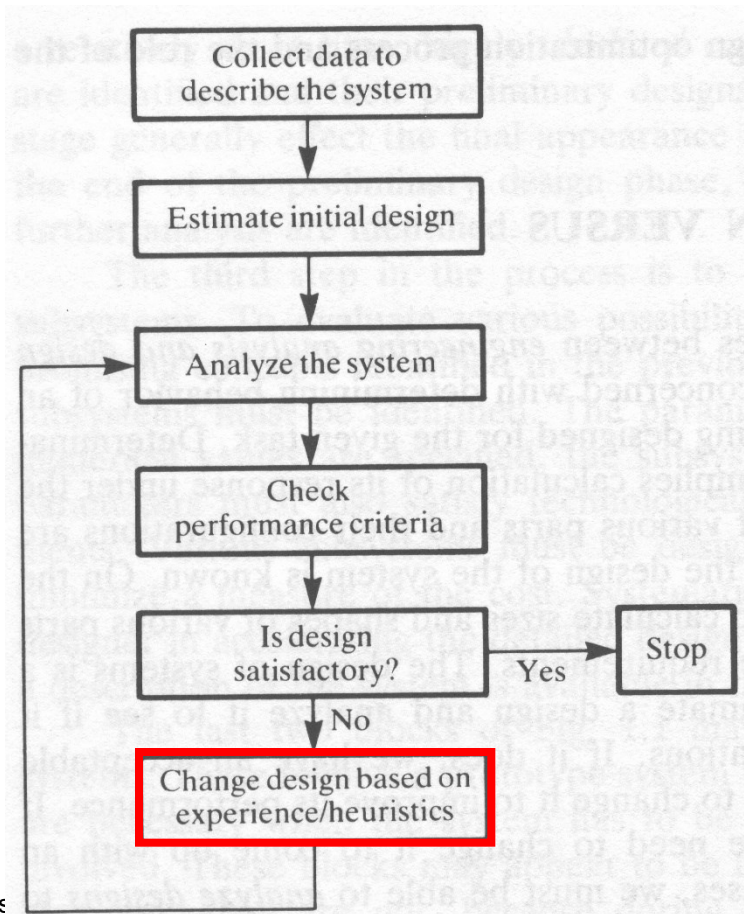
해석 (Analysis)	설계 (Design)
	
$\delta = ?$ $\sigma = ?$	$\delta \leq \delta_{allow}$ $\sigma \leq \sigma_{allow}$
<ul style="list-style-type: none"> <li>• to obtain the response of a given system</li> <li>• # of unknown = # of equations</li> </ul>	<ul style="list-style-type: none"> <li>• to determine specifications of the system satisfying requirements</li> <li>• # of unknown &gt; # of equations</li> </ul>



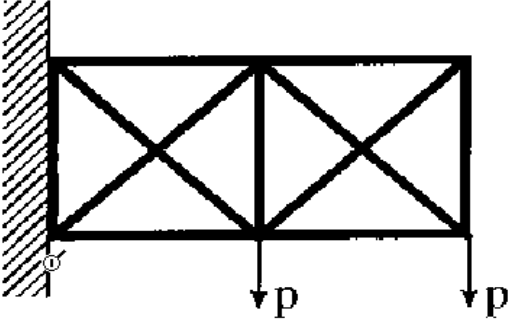
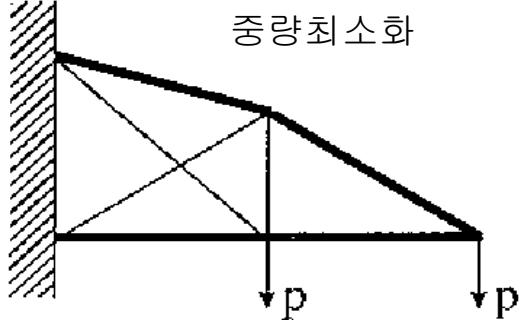
# Conventional vs. Optimum (1)

- Conventional design
  - Depends on designer's intuition, experience, and skill
  - Merits in making conceptual changes/additional specs
  - Difficulties in detailed design (complex constraints)
  - Less formal, no objective function/trend information
- Optimum design
  - Identify explicitly a set of design variables, cost function to be minimized, and constraint functions
  - More organized using trend information

# Conventional vs. Optimum (2)



# Conventional vs. Optimum (3)

Conventional Design	Optimum Design
	
$\delta \leq \delta_{allow}$ $\sigma \leq \sigma_{allow}$	$\delta \leq \delta_{allow}$ $\sigma \leq \sigma_{allow}$

# Optimization Problems in Engineering (1)

- Design aircraft for minimum weight and maximum strength
- Optimal trajectories of space vehicles
- Design civil engineering structures for minimum cost
- Design water-resource projects like dams to mitigate flood damage while yielding maximum hydropower
- Predict structural behavior by minimizing potential energy
- Material-cutting strategy for minimum cost
- Design pump and heat transfer equipment for maximum efficiency
- Maximize power output of electrical networks and machinery while minimizing heat generation
- Shortest route of salesperson visiting various cities during one sales trip
- Optimal planning and scheduling

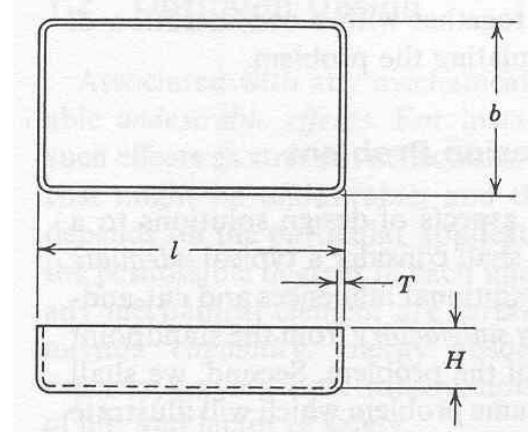
# Optimization Problems in Engineering (2)

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- Statistical analysis and models with minimum error
- Optimal pipeline networks
- Inventory control
- Maintenance planning to minimize cost
- Minimize waiting and idling times
- Design waste treatment systems to meet water-quality standards at least cost

# Plastic Tray Design (1)

- Basic design problem
  - Design a plastic tray capable of holding a specified volume of liquid,  $V$ , such that the liquid has a specified depth  $H$ , and the wall thickness of the tray is to be a specified thickness,  $T$ . The tray is to be manufactured in large quantities.
- Adequate design solution
  - Geometry
    - Intuition: rectangular ?
    - Infinite number of possible solutions
  - Material: experience?
    - Possible manufacturing techniques: vacuum forming
    - Possible chemical reactions w/ liquid: acrylic thermoplastic sheet



# Plastic Tray Design (2)

- Optimum design solution
  - “manufactured in large quantities”: cost (most significant undesirable effect)
  - Primary design equation:  $C = \underbrace{C_o}_{\text{overhead}} + \underbrace{C_t}_{\text{tooling}} + \underbrace{C_l}_{\text{labor}} + \underbrace{C_m}_{\text{material}}$
  - $C_o, C_t, C_l$  : independent of
    - Reasonable geometrical shapes / Feasible plastic materials
  - Objective: minimize cost  $C_m$ 
    - selecting the best feasible material and the best values for  $b$  and  $l$

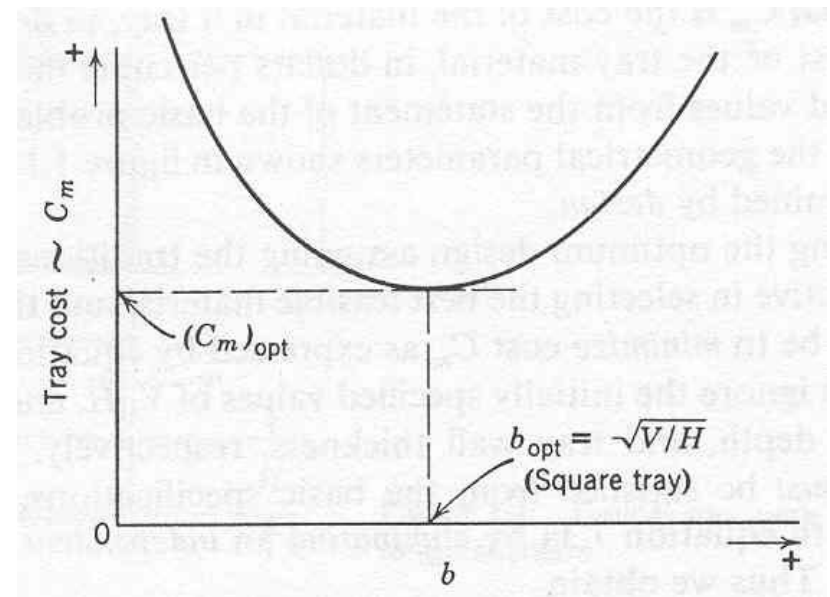
$c$  : unit volume cost of the tray material

- Optimum feasible material
  - $c$ : polystyrene

	$c$	
	\$/in <sup>3</sup>	\$/m <sup>3</sup>
Acrylic	0.030	1831
Polystyrene	0.012	732

# Plastic Tray Design (3)

- Optimum geometry for the rectangular tray



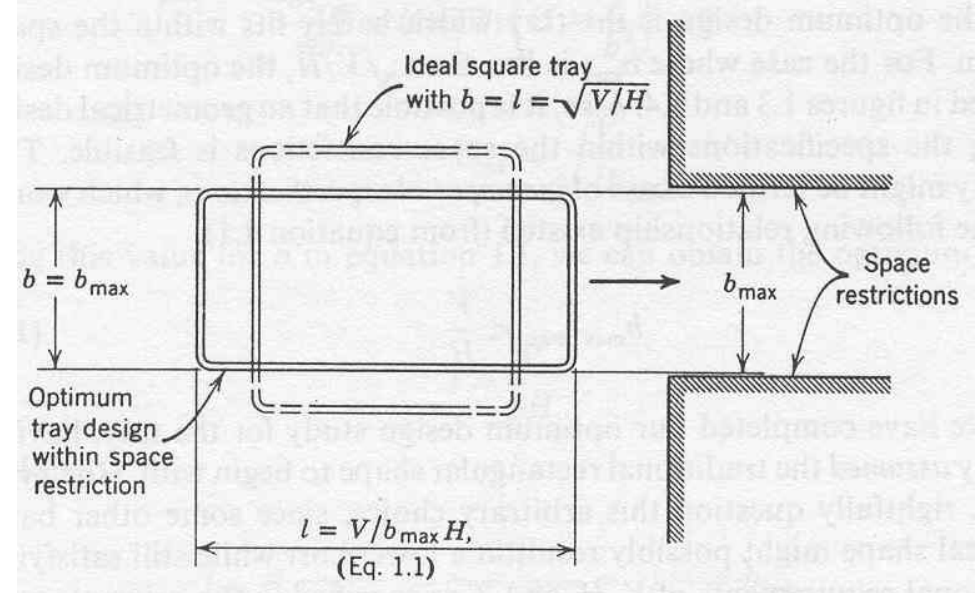
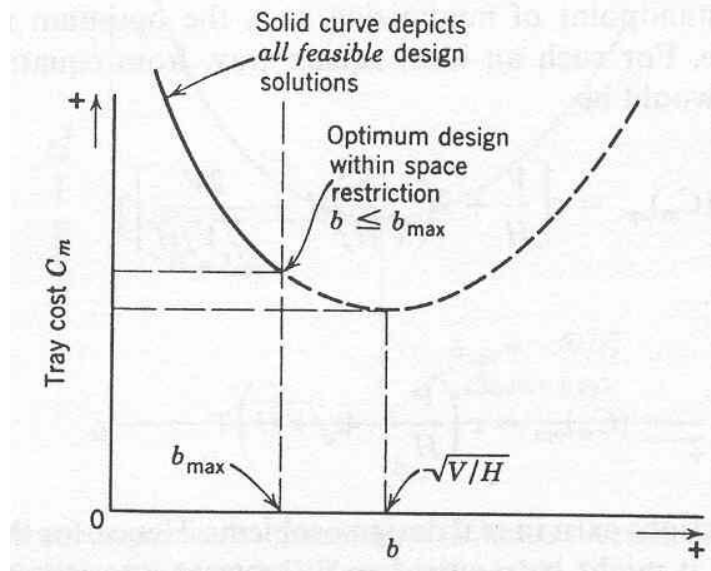


# Plastic Tray Design (4)

- Space restrictions:  $b \leq b_{\max}$ ,  $l \leq l_{\max}$

$b_{\max} \geq \sqrt{V/H}$  and  $l_{\max} \geq \sqrt{V/H}$  : ideal square tray is still the optimum design  
 $b_{\max} < \sqrt{V/H}$  or  $l_{\max} < \sqrt{V/H}$  : the tray which barely fits within the space restriction

incompatible specifications :  $b_{\max} l_{\max} < \frac{V}{H}$



# Plastic Tray Design (5)

- Other basic geometrical shape ?
  - Circle: lowest  $C_m$  from the calculus of variations

