

JK와 함께 트램펄린운동
으로 아름다운 몸매를!



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1. Statement

2. Data and Information Collection

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1. Statement

몸무게가 100kg 나가는
김아중! 다이어트를 위

트램펄린에 달린 용수철
는 20cm라고 한다.

이 여성이 사용했을 때
하는 용수철의 최소 siz

용수철은 Helical
이다. (단, 용수철
용수철에는 같은



의 목표는 바로
을 선택하였다.

하나 당 길이 (L)

cm이하가 되도록

M 229 wire
작용하고 각

1. Statement

2. Data and Information Collection

3. Identification of design variables

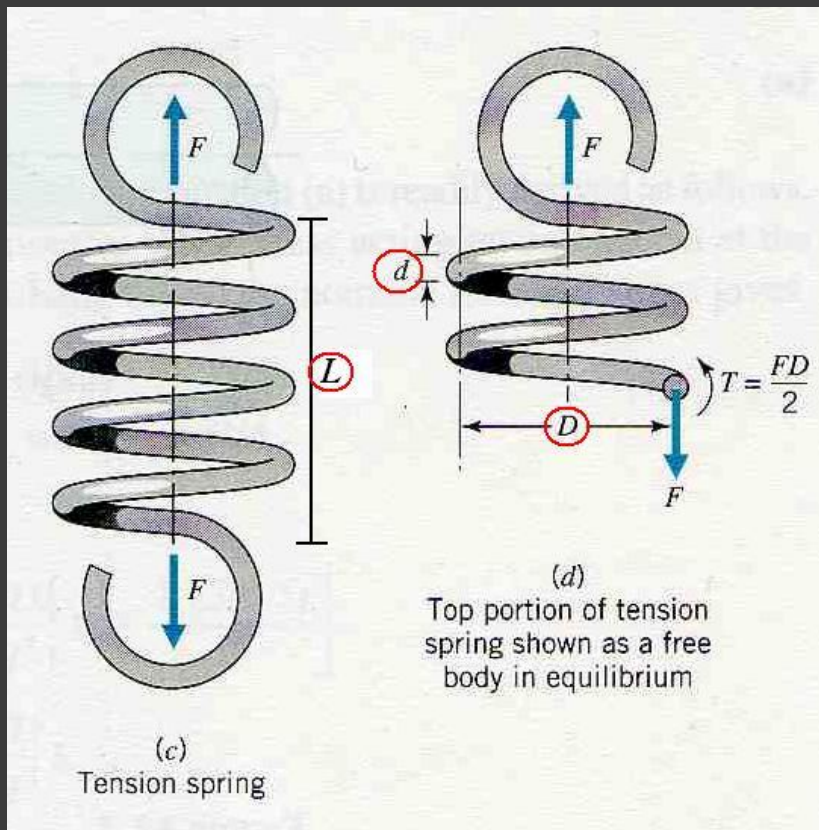
4. Identification of a Criterion to be Optimized

5. Identification of constraints

6. Simplified Solution

2. Data and Information Collection

● 스프링의 기본 형상



D : mean coil diameter

d : wire diameter

L : length (20cm)

Spring index $C = \frac{D}{d} \geq 3$

Force $F = \frac{100 \times 9.8}{20} = 49N$

2. Data and Information Collection

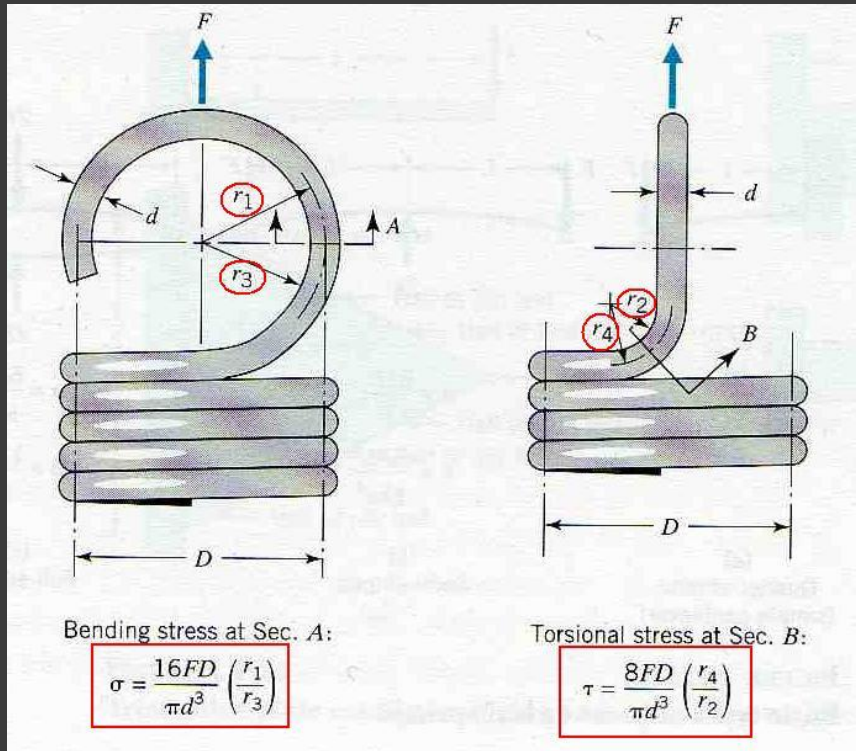
- ◉ ASTM 239 wire

$$G = 79GPa$$

$$\begin{aligned}\tau_{allow} &= 0.45S_u = 0.45 \times 225ksi \\ &= 0.45 \times 225 \times 6.89MPa \\ &= \mathbf{697.613MPa}\end{aligned}$$

$$\begin{aligned}\sigma_{allow} &= 0.5S_u = 0.5 \times 225ksi \\ &= 0.5 \times 225 \times 6.89MPa \\ &= \mathbf{775.125MPa}\end{aligned}$$

2. Data and Information Collection



$$r_1 = \frac{D}{2}, \quad r_3 = \frac{1}{2}(D - d)$$

$$r_4 = 2.5d(\text{recommended}), \quad r_2 = 2.5d - \frac{d}{2} = 2d$$

변형되는 길이

$$\delta = \frac{8FD^3 N}{d^4 G} = \frac{8FD^3 L}{d^5 G} \leq 0.1(m)$$

Spring 끝 쪽
에서 발생하는
응력

$$\sigma = \frac{16FD}{\pi d^3} \left(\frac{r_1}{r_3} \right)$$

$$\tau = \frac{8FD}{\pi d^3} \left(\frac{r_4}{r_2} \right)$$

Coil 내에
서 발생하는
응력

$$\tau = \frac{8FD}{\pi d^3} \left(1 + \frac{0.5}{C} \right) \leq \tau_{\text{initial}}$$

$$\tau_{\text{initial}} = 0.4 \frac{S_u}{C}$$

1. Statement

2. Data and Information Collection

3. Identification of design variables

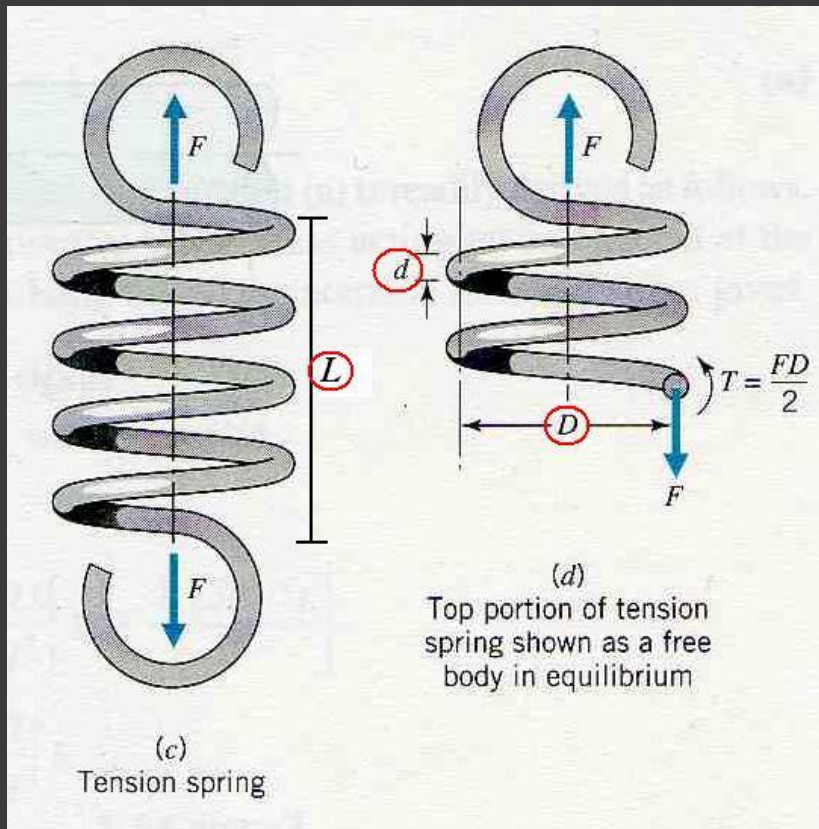
4. Identification of a Criterion to be Optimized

5. Identification of constraints

6. Simplified Solution

3. Identification of Design Variables

● 스프링의 기본 형상



D : mean coil diameter

d : wire diameter

단위: m

1. Statement

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4. Identification of a Criterion to be Optimized

● Cost function

용수철 부피 최소화(재료의 양 최소화)

$$f(D, d) = \frac{\pi}{4} d^2 \times \pi D \frac{L}{d} = \frac{\pi^2}{4} D d L$$

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5. Identification of Constraints

$$C = \frac{D}{d} \geq 3$$

$$\delta = \frac{8FD^3L}{d^5G} \leq 0.1$$

$$\sigma = \frac{16FD}{\pi d^3} \left(\frac{D}{D-d} \right) \leq \sigma_{allow}$$

$$\tau = \frac{8FD}{\pi d^3} \left(\frac{2.5d}{2d} \right) \leq \tau_{allow}$$

$$\tau = \frac{8FD}{\pi d^3} \left(1 + \frac{0.5}{C} \right) \leq \tau_{initial}$$



$$g_1 : 3d - D \leq 0$$

$$g_2 : \frac{8FD^3L}{d^5G} - 0.1 \leq 0$$

$$g_3 : \frac{16FD}{\pi d^3} \left(\frac{D}{D-d} \right) - \sigma_{allow} \leq 0$$

$$g_4 : \frac{10FD}{\pi d^3} - \tau_{allow} \leq 0$$

$$g_5 : \frac{8FD}{\pi d^3} \left(1 + \frac{0.5}{C} \right) - \tau_{initial} \leq 0$$

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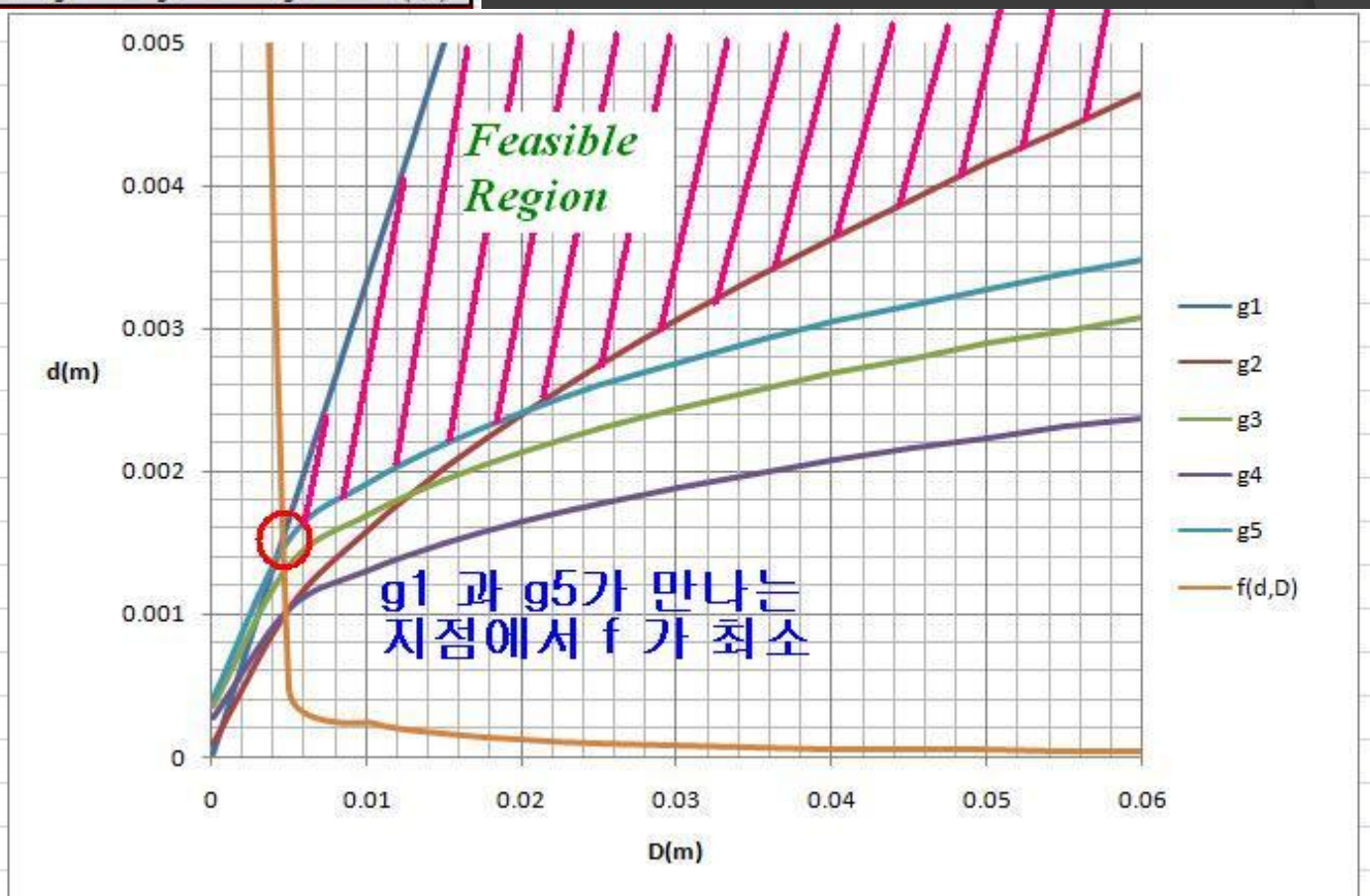
5. Identification of constraints

6. Simplified Solution

6. Simplified Solution

결과 표 & 그래프

D	g1	g2	g3	g4	g5	f(d,D)
0.0001	3.3E-05	9.98476E-05				
0.005	0.00167	0.00104404				
0.01	0.00333	0.00158247				
0.015	0.005	0.00201833				
0.02	0.00667	0.00239858				
0.025	0.00833	0.00274221				
0.03	0.01	0.00305921				
0.035	0.01167	0.00335566				
0.04	0.01333	0.00363558				
0.045	0.015	0.00390180				
0.05	0.01667	0.00415642				
0.055	0.01833	0.00440104				
0.06	0.02	0.00463690				
0.065	0.02167	0.00486503				
0.07	0.02333	0.00508623				
0.075	0.025	0.00530120				
0.08	0.02667	0.00551051				
0.085	0.02833	0.00571464				
0.09	0.03	0.00591402				
0.095	0.03167	0.00610902				
0.1	0.03333	0.00629996				
0.105	0.035	0.00648711				
0.11	0.03667	0.00667073				
0.115	0.03833	0.00685104				
0.12	0.04	0.00702823				
0.125	0.04167	0.00720250				
0.13	0.04333	0.00737401				
0.135	0.045	0.00754289				
0.14	0.04667	0.00770929				
0.145	0.04833	0.00787333				
0.15	0.05	0.00803512				



6. Simplified Solution

● Matlab Solver

```
1 %메틀랩 solve를 이용해서 g1과 g5 의 교점을 찾는다.  
2 - [D] = solve('D/3 = (8*(100*9.8/20)*D*(1+0.5/3)/(0.4*225*pi*6.89*(10^6)/3))^(1/3)')  
3 %D = .43606691333724466263061411286085e-2;  
4 %d = .14535563777908155421020470428695e-2;  
5 % D와 d 값을 위의 값으로 선택한 다음 목적함수값을 구한다.  
6 - f= ((pi^2)/4)*D*d*0.2  
7 %f = 3.1279e-006
```

$$D = 0.0043\text{m} = 4.3\text{ mm}$$

$$d = 0.0014\text{m} = 1.4\text{ mm}$$

$$f = 3.128 \cdot 10^{-6} \text{ m}^3$$

Reference

- ◉ Robert C. Juvinall and Kurt M. Marshek , WILEY, “Fundamentals of Machine Component Design 4th Edition” - Ch12
- ◉ Jasbir S. Arora, Elsevier, “ Introduction to Optimum Design”

◎ 질문 있으세요?

