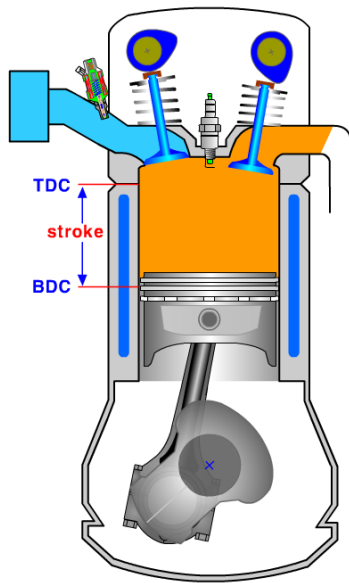


Contents

- Power Source : Engine/Motor
- Power Transfer : Clutch/Transmission
- Power Storage : Battery
- Driving Resistance
- Driver Controller

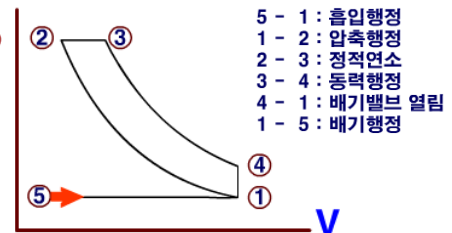
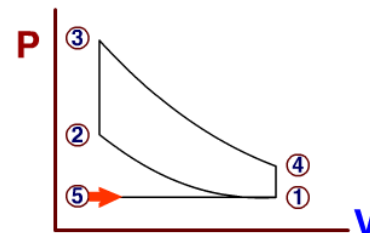
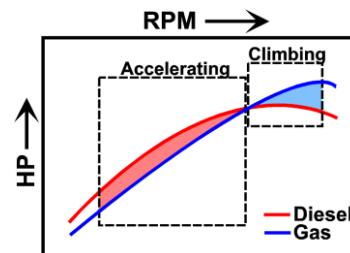
Engine

- Generation of the power to drive a vehicle
- Operating principle
 - Force generation by fuel injection and ignition in the cylinder
 - Torque generation on a crank shaft from the force through the mechanical linkage



[작동원리 Link](#)

Specification	Gasoline Engine (Otto)	Diesel Engine
Ignition Type	Spark Ignition	Compression Ignition
Compression Ratio	Between 8:1 and 12:1	Between 16:1 and 22:1
Efficiency	25-30%	36-45%
Maximum Engine Speed	7000-8250 RPM	up to 5250 RPM
Exhaust Temperature (under full load)	700-1200 Degrees Celsius	300-900 Degree Celsius



Mean Value Model

- Input : fuel mass flow rate
- Output : engine torque

1. Engine dynamic equation

$$J_e \dot{\omega}_e = T_e = T_{ind} - T_{loss}$$

J_e : engine equivalent inertia [kgm^2]

ω_e : engine angular velocity [rad/s]

T_e : engine output torque [Nm]

T_{ind} : indicated combustion torque [Nm]

T_{loss} : pumping and friction losses [Nm]

3. Pumping and friction losses

$$T_{loss} = T_{fric} + T_{pump}$$

$$T_{fric} = a_0 \omega_e^2 + a_1 \omega_e + a_2$$

$$T_{pump} = b_0 \omega_e p_{man} + b_1 p_{man}$$

a_0, a_1, a_2, b_0, b_1 : parameters dependent on specific engine

p_{man} : manifold air pressure [bar]

2. Indicated combustion torque

$$\dot{m}_f = \frac{\dot{m}_{ao}}{L_{th}} \quad T_{ind} = \frac{H_u \eta_i \dot{m}_f}{\omega_e}$$

$\dot{m}_f$: air mass flow rate [kg/s]

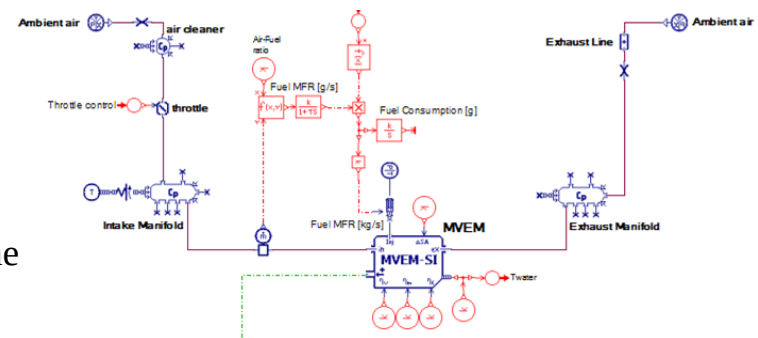
$\dot{m}_{ao}$: fuel mass flow rate into cylinder [kg/s]

L_{th} : stoichiometric air/fuel mass ratio

T_{ind} : indicated combustion torque [Nm]

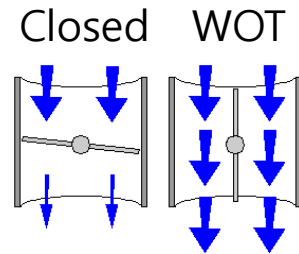
H_u : fuel energy constant [J/kg]

η_i : indicated efficiency

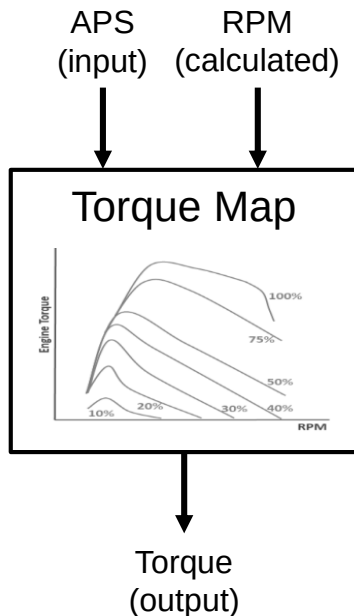


Torque Map Model

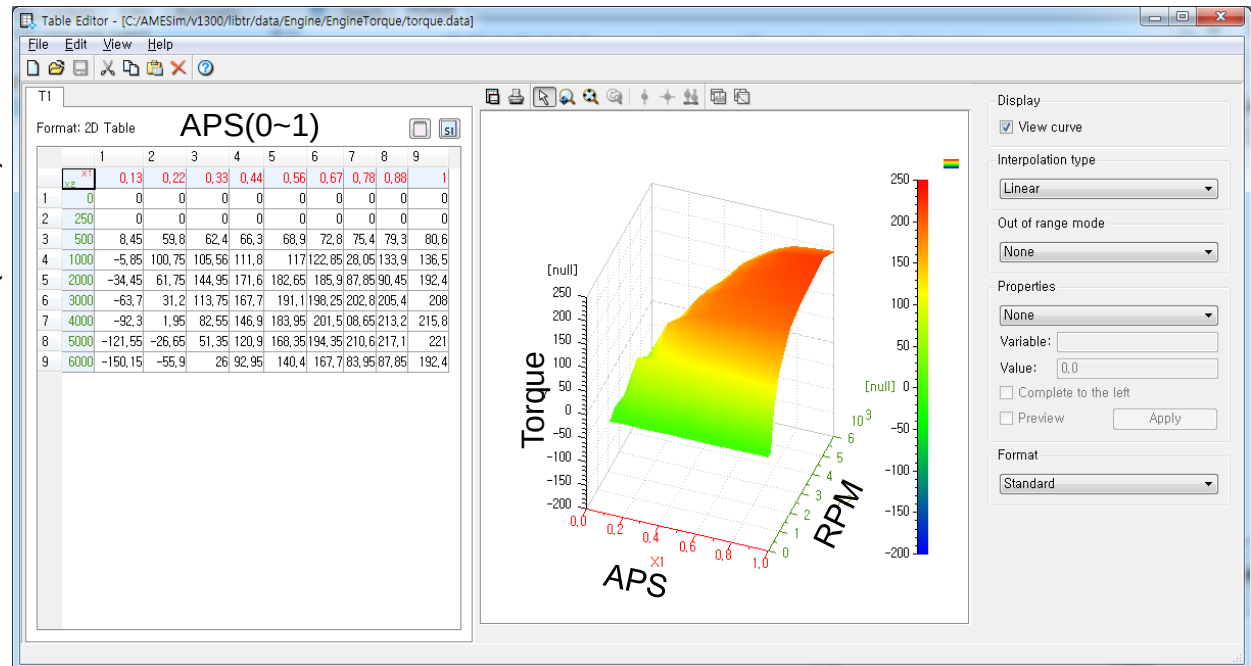
- Input : APS (accelerator pedal sensor)
- Output : engine torque
- Calculation of the engine torque from the experimental torque map



$$T_e = f(APS, RPM)$$

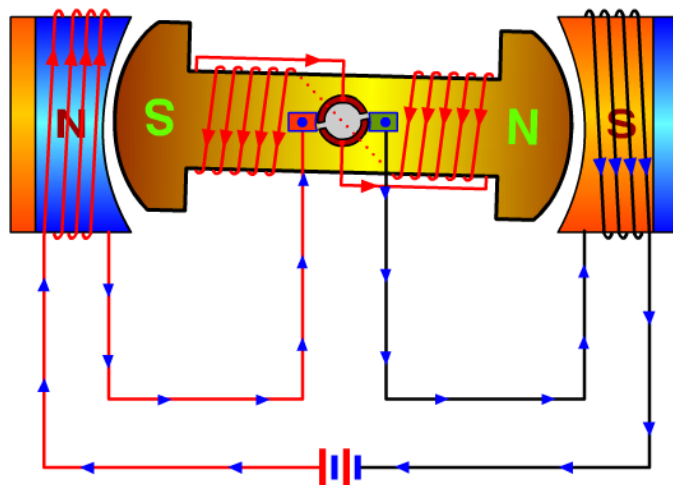


RPM (0~6000)

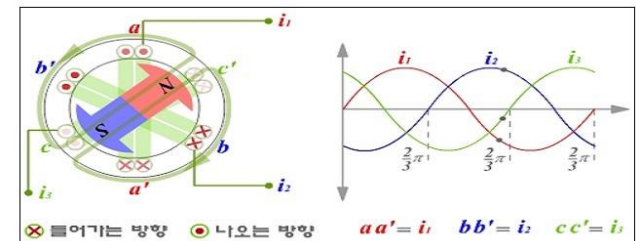
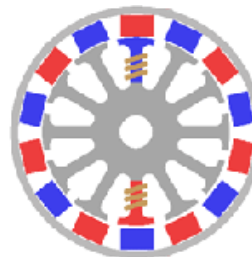
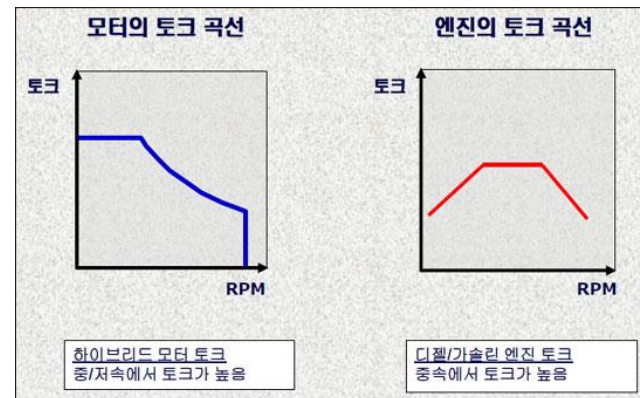


Motor

- Generation of the power to drive a vehicle
- Operating principle
 - Generation of a rotating magnetic field from an electric current
 - Mechanical torque generation on a rotating shaft from the magnetic force

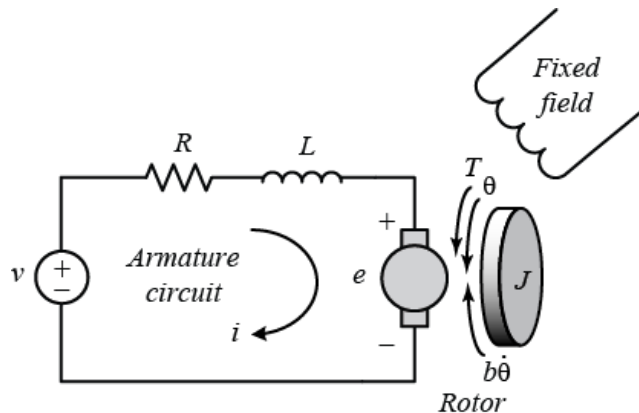


작동원리 Link



Electric Circuit Model

- Input : circuit voltage
- Output : motor torque



1. Equivalent circuit

$$V = L \frac{di}{dt} + RI + E_b$$

V : circuit voltage [V]

L : electric inductance [H]

I : electric current [A]

R : electric resistance [Ω]

E_b : back electro motive force [V]

2. Motor torque

$$E_b = K_e \omega_m$$

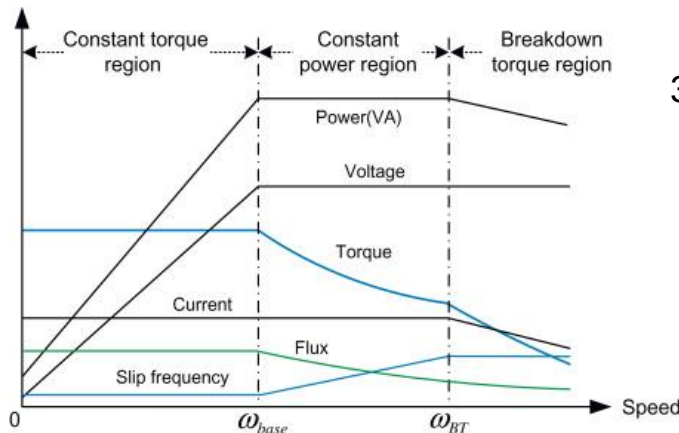
$$T_m = K_t I$$

K_e : back-EMF constant [Vs]

ω_m : motor shaft speed [rad/s]

T_m : motor torque [Nm]

K_t : torque constant [Nm/A]

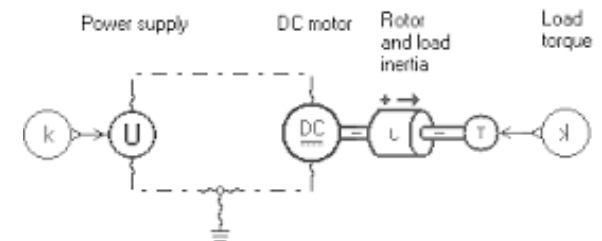


3. Motor dynamic equation

$$T_m - T_{loss} = J \dot{\omega}_m$$

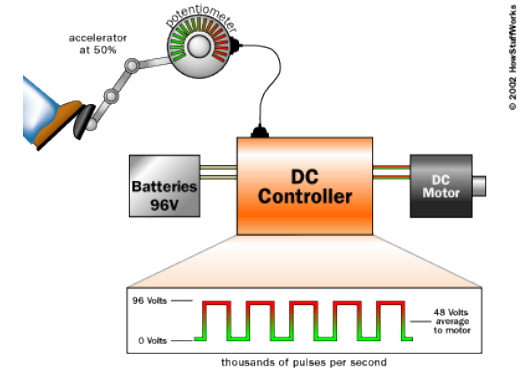
T_{loss} : total loss torque [Nm]

J : motor inertia [kgm^2]

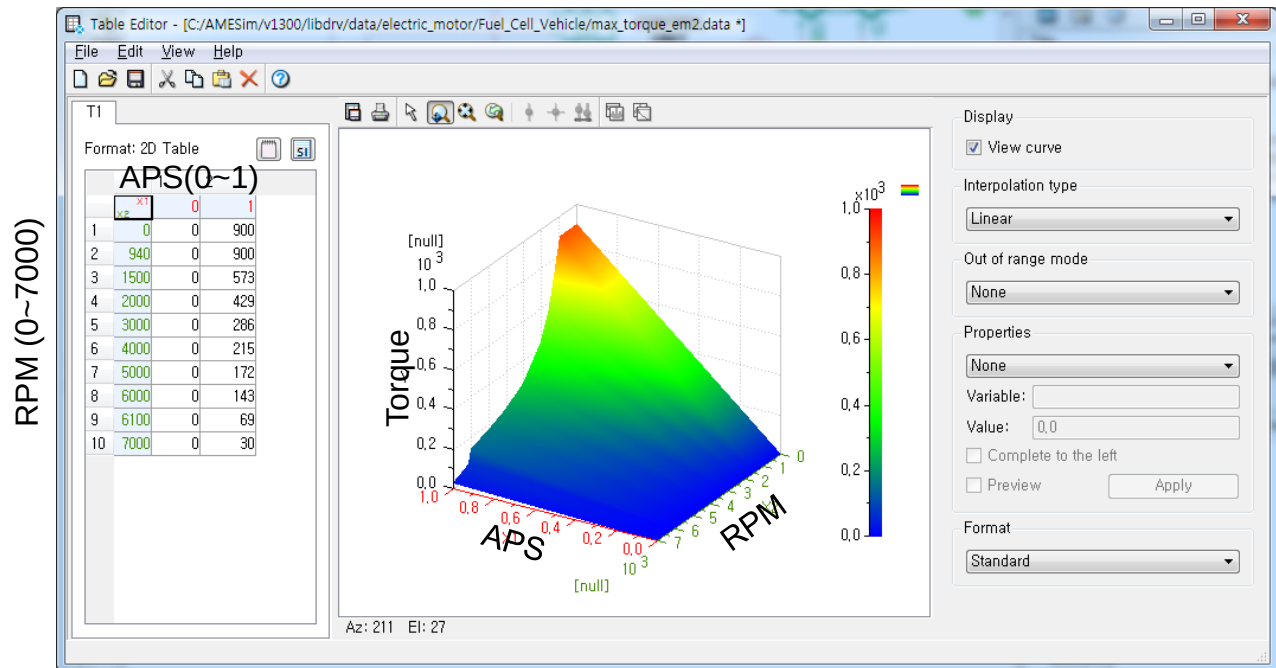
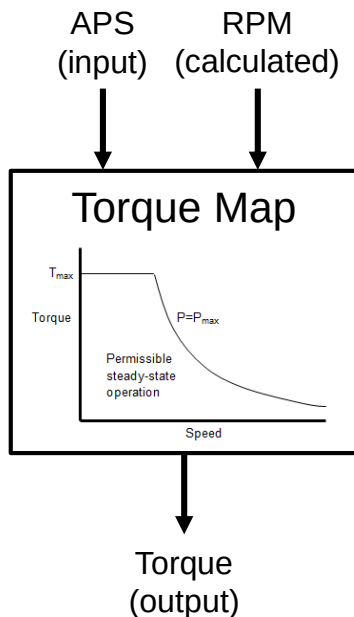


Torque Map Model

- Input : APS (accelerator pedal sensor)
- Output : motor torque
- Calculation of the motor torque from the experimental torque map

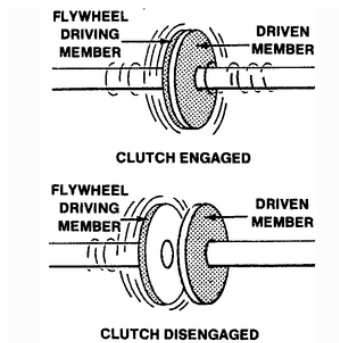
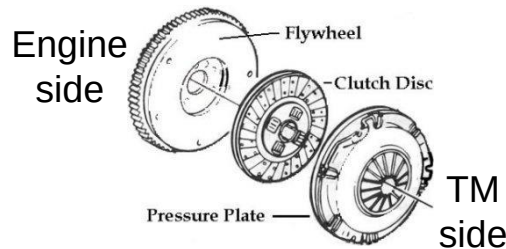


$$T_m = f(APS, RPM)$$

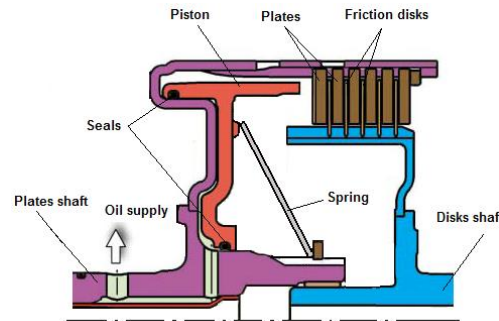


Clutch

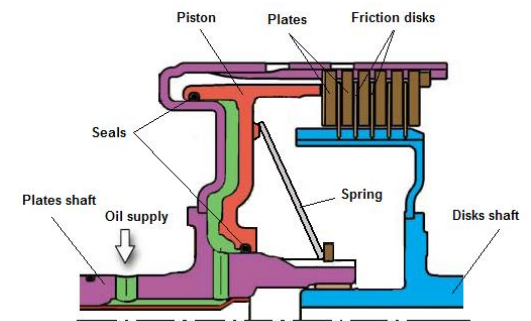
- Torque transfer or cut-off between input and output shaft
- Operating principle
 - Generation of the friction torque on a clutch disk by the clutch engaging or disengaging
 - Synchronization of both shaft speeds



< Single Disk >



Disengaged

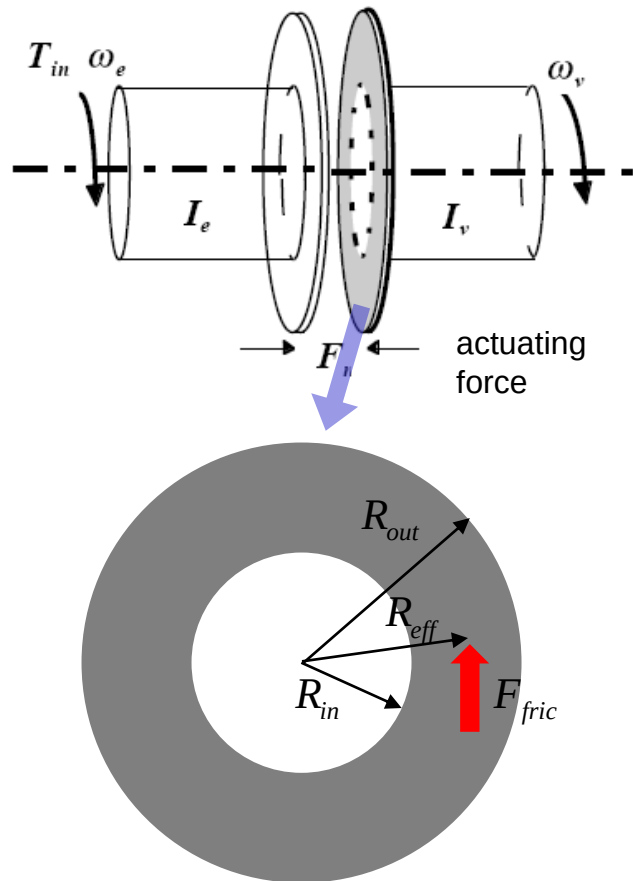


Engaged

< Multi Disk >

Friction Torque Model

- Input : clutch actuating force
- Output : output shaft torque



1. Output torque equation

$$T_{out} = \begin{cases} F_{fric} R_{eff} & (\omega_{rel} \neq 0) \\ T_{in} & (\omega_{rel} = 0) \end{cases}$$

F_{fric} : friction force [N]

R_{eff} : effective friction radius [m]

ω_{rel} : relative speed of shafts [rad/s]

2. Friction equation

$$F_{fric} = \mu_{disk} F_n$$

$$F_n = F_{act} \tanh\left(2 \frac{\omega_{rel}}{d\omega}\right)$$

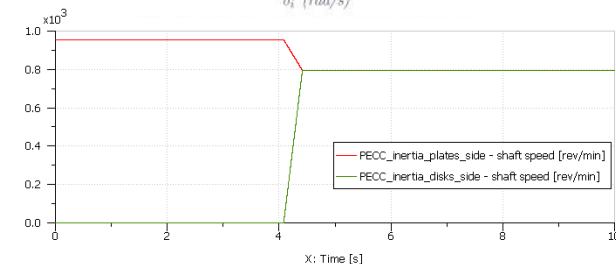
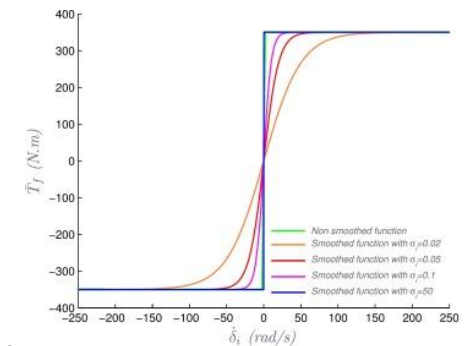
$$\omega_{rel} = \omega_e - \omega_v$$

$$R_{eff} = \frac{2(r_{out}^3 - r_{in}^3)}{3(r_{out}^2 - r_{in}^2)}$$

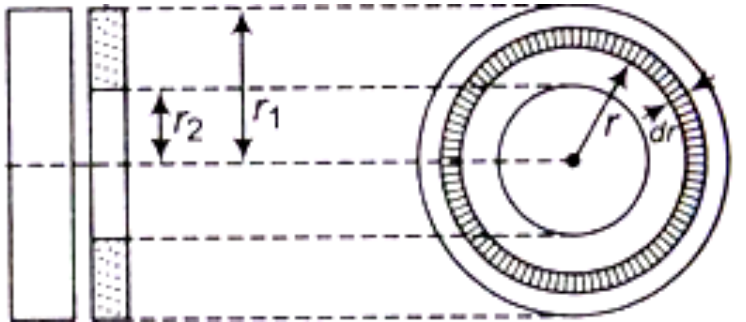
μ_{disk} : friction coefficient

F_n : normal force on disk [N]

F_{act} : clutch actuating force [N]



Effective Friction Radius



$$dA = 2\pi r \times dr$$

P : normal pressure

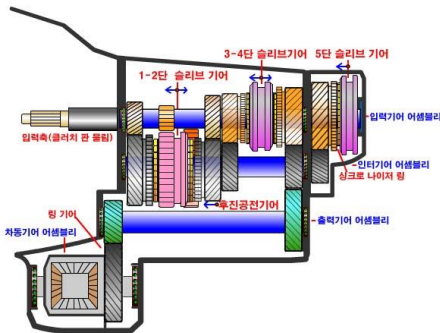
$$F_n = P \int_{r_2}^{r_1} 2\pi r \, dr \quad P = \frac{F_n}{\pi(r_1^2 - r_2^2)}$$

$$T = \mu P \int_{r_2}^{r_1} 2\pi r^2 \, dr = 2\mu\pi \frac{F_n}{\pi(r_1^2 - r_2^2)} \times \frac{r_1^3 - r_2^3}{3}$$

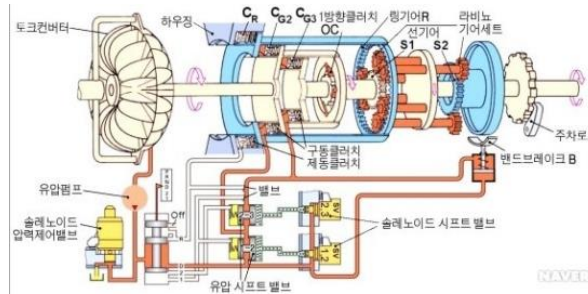
$$T = \mu F_n R_{eff} \quad \therefore R_{eff} = \frac{2(r_1^3 - r_2^3)}{3(r_1^2 - r_2^2)}$$

Transmission

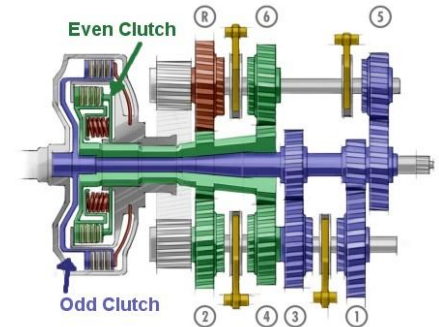
- Conversion of the torque and speed from input shaft to the proper torque and speed on output shaft
- Operating principle
 - Selection of a proper gear by operating a clutch
 - Increasing or decreasing of the torque and speed from input shaft



< Manual Transmission(MT) >

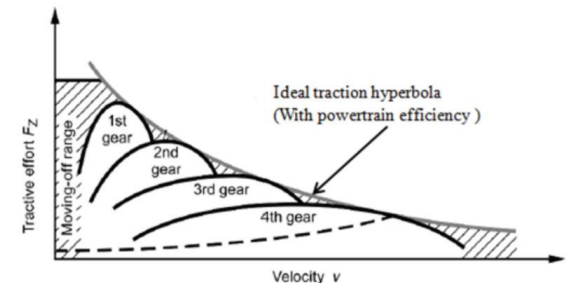
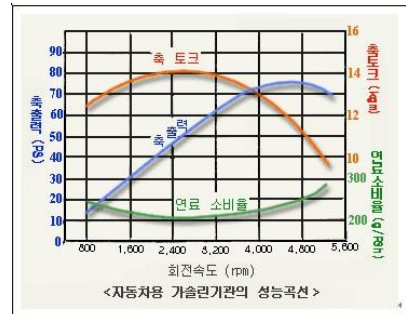


< Automatic Transmission(AT) >



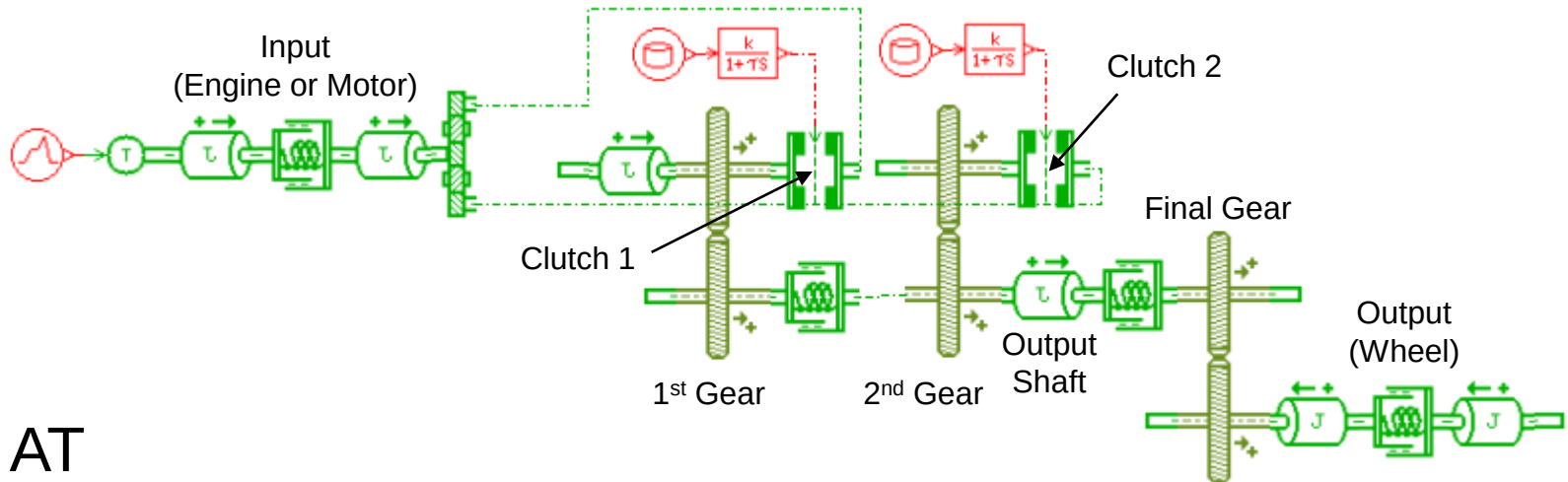
< Dual Clutch Transmission(DCT) >

구분	MT	AT	DCT
Efficiency	↑	↓	↑
Drivability	↓	↑	↑
Cost	↓	-	↑

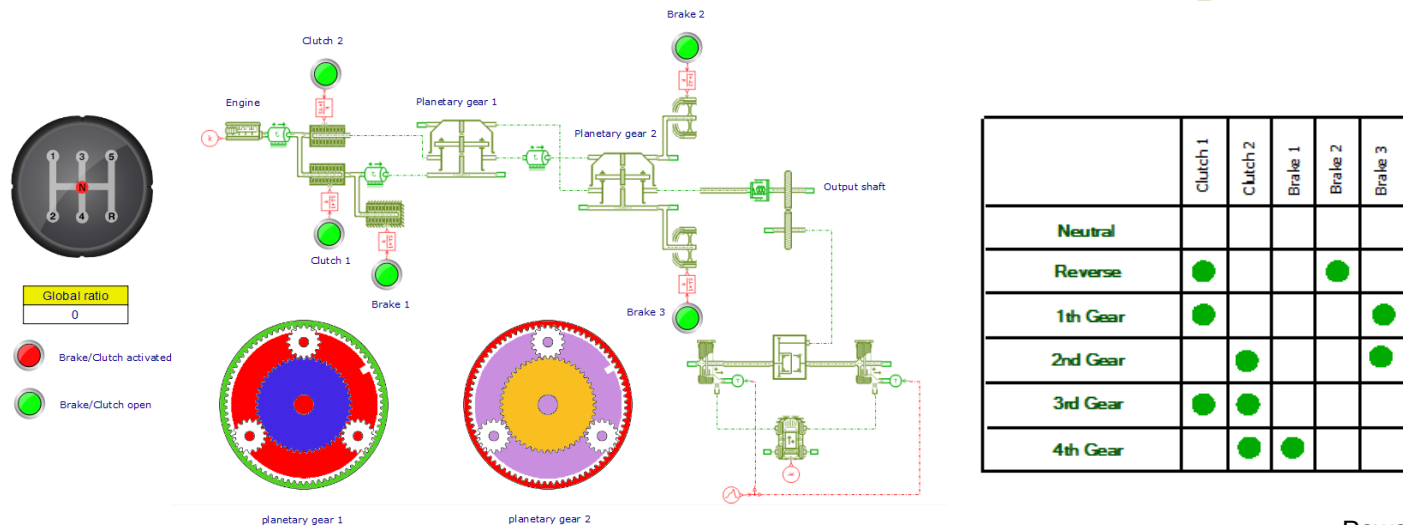


Geartrain

- MT/DCT



- AT



Parallel Gear Model (MT/DCT)

- Input : input torque/speed
- Output : output torque/speed

1. Gear ratio

$$GR = \frac{\text{\# of driven gear teeth}}{\text{\# of drive gear teeth}}$$

2. Output torque & speed

$$T_{out} = T_{in} \times GR$$

$$\omega_{out} = \frac{\omega_{in}}{GR}$$

※ Example : $T_{in} = 100 \text{ Nm}$, $\omega_{in} = 3000 \text{ RPM}$

1) $GR = 2$ (reduction)

$$T_{out} = 100 \times 2 = 200 \text{ Nm}$$

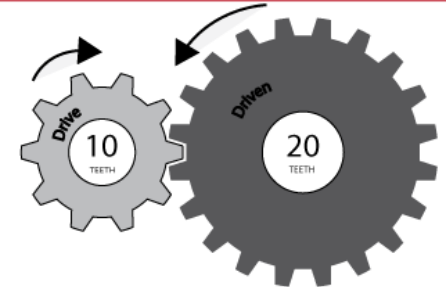
$$\omega_{out} = \frac{3000}{2} = 1500 \text{ RPM}$$

2) $GR = 0.75$ (overdrive)

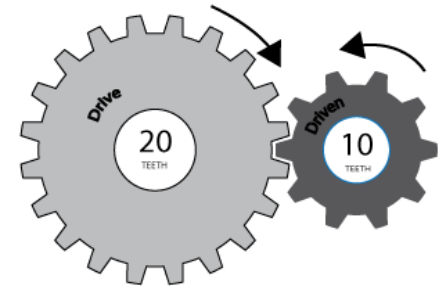
$$T_{out} = 100 \times 0.75 = 75 \text{ Nm}$$

$$\omega_{out} = \frac{3000}{0.75} = 4000 \text{ RPM}$$

Gear reduction occurs when the drive gear is smaller or has fewer teeth than the driven gear.



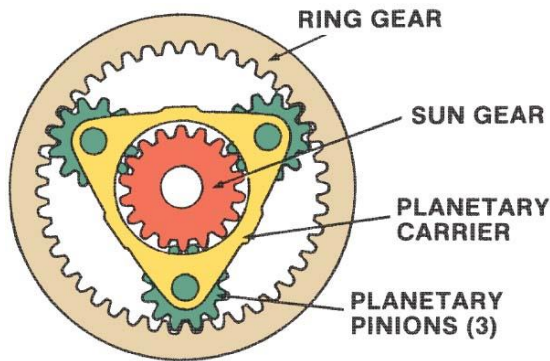
Overdrive occurs when the drive gear is larger or has more teeth than the driven gear.



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Coaxial Gear Model (AT)

- Input : input torque/speed
- Output : output torque/speed



Ring	Carrier	Sun	Gear Ratio
driven	drive	fixed	$Z_r / (Z_s + Z_r)$
drive	driven	fixed	$(Z_s + Z_r) / Z_r$
fixed	drive	driven	$Z_s / (Z_s + Z_r)$
fixed	driven	drive	$(Z_s + Z_r) / Z_s$
driven	fixed	drive	$-Z_r / Z_s$

reverse

1. Motion equation

$$\omega_s + \frac{Z_r}{Z_s} \omega_r - \frac{Z_s + Z_r}{Z_s} \omega_c = 0$$

Z_r : # of ring gear teeth

Z_s : # of ring gear teeth

$Z_s + Z_r$: # of carrier equivalent teeth

2. Output torque & speed

$$T_{out} = T_{in} \times GR$$

$$\omega_{out} = \frac{\omega_{in}}{GR}$$

※ Example : $T_{in} = 100 \text{ Nm}$, $\omega_{in} = 3000 \text{ RPM}$, $Z_r = 80$, $Z_s = 40$
ring(drive), sun(fixed)

$$GR = \frac{Z_s + Z_r}{Z_s} = \frac{40 + 80}{40} = 3$$

$$T_{out} = 100 \times 3 = 300 \text{ Nm}$$

$$\omega_{out} = \frac{3000}{3} = 1000 \text{ RPM}$$

Coaxial Gear Model (AT)

- Motion equation

각 기어 별 접촉점에서의 속도는

$$V_s = \omega_s r_s \quad V_r = \omega_r r_r \quad V_c = \omega_c r_c$$

여기서 캐리어의 속도와 반지름은

$$V_c = \frac{V_s + V_r}{2} = \omega_c r_c = \omega_c \frac{r_s + r_r}{2}$$

$$V_s = \omega_s r_s \quad \text{이고,} \quad V_r = \omega_r r_r \quad \text{이므로}$$

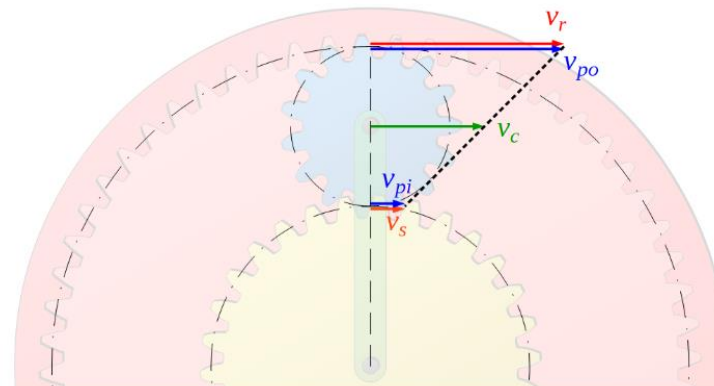
$$\frac{\omega_s r_s + \omega_r r_r}{2} = \omega_c \frac{r_s + r_r}{2}$$

정리하면

$$\omega_s r_s + \omega_r r_r - \omega_c (r_s + r_r) = 0$$

각 기어의 반지름은 잇수에 비례하므로

$$\omega_s Z_s + \omega_r Z_r - \omega_c (Z_s + Z_r) = 0$$



선기어 잇수로 나눠주면

$$\therefore \omega_s + \omega_r \frac{Z_r}{Z_s} - \omega_c \frac{Z_s + Z_r}{Z_s} = 0$$

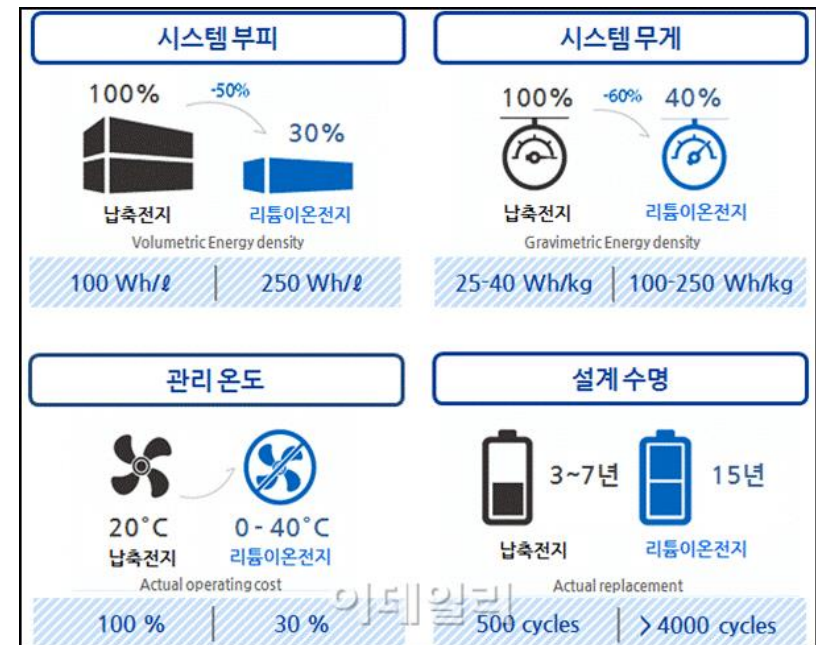
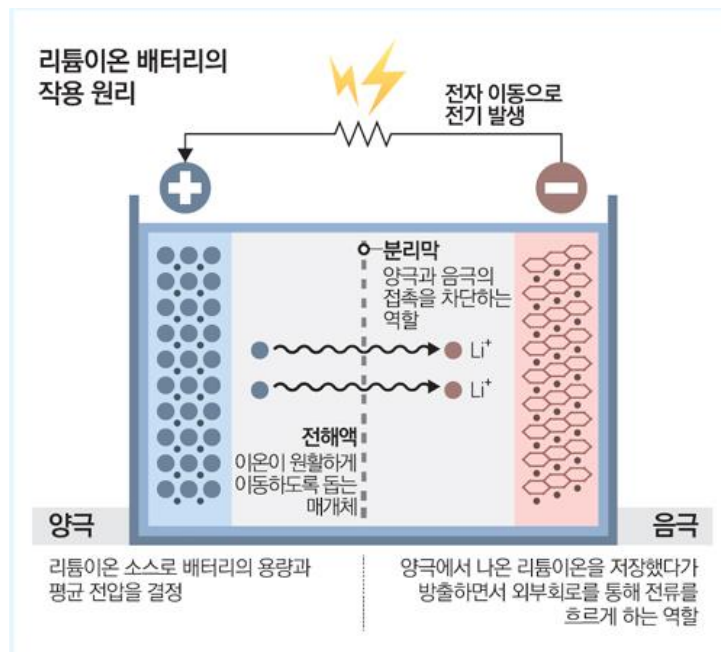
Example: Ring(driven), Carrier(drive), Sun(fixed)

$$\cancel{\omega_s} + \omega_r \frac{Z_r}{Z_s} - \omega_c \frac{Z_s + Z_r}{Z_s} = 0$$

$$GR = \frac{\omega_{in}}{\omega_{out}} = \frac{\omega_c}{\omega_r} = \frac{Z_s}{Z_s + Z_r} \frac{Z_r}{Z_s} = \frac{Z_r}{Z_s + Z_r}$$

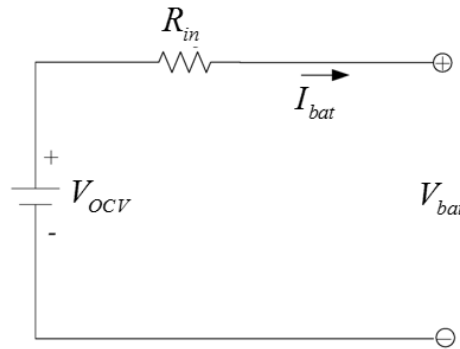
Battery

- Providing the current to generate the mechanical torque from a motor
- Operating principle
 - Conversion of the electric energy in a capacitor to the current by the battery voltage and resistance



Equivalent Circuit Model

- Input : motor power (torque and speed)
- Output : state of charge (SOC)



1. Equivalent circuit equation

$$V_{bat} = V_{OCV} - R_{in} I_{bat}$$

V_{bat} : battery volatage [V]

V_{OCV} : open circuit voltage [V]

R_{in} : equivalent internal resistance [Ω]

I_{bat} : battery current [A]

2. SOC calculation

Mechanical Power = Electrical Power

$$T_{mot} \omega_{mot} = \eta V_{bat} I_{bat} \quad (\text{discharging})$$

$$\eta T_{mot} \omega_{mot} = V_{bat} I_{bat} \quad (\text{charging})$$

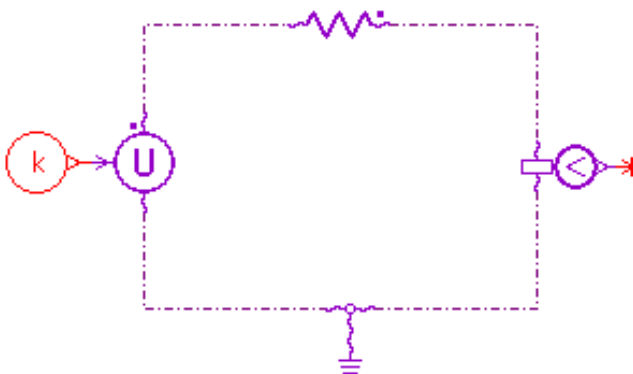
$$\frac{dSOC}{dt} = -I_{bat} \frac{100}{C_{nom}}$$

η : motor efficiency

SOC_{ini} : initial SOC [%]

C_{nom} : rated capacity [As]

$$SOC = SOC_{ini} - \frac{100}{C_{nom}} \int I_{bat} dt$$



Equivalent Circuit Model

※ Example : when $T_{mot} = 100 \text{ Nm}$, $\omega_{mot} = 955 \text{ RPM}$ (100 rad/s) during 2 min, final SOC?

$$V_{OCV} = 300 \text{ V}, R_{in} = 0.1 \Omega, \eta = 1, C_{nom} = 40,000 \text{ As}, SOC_{ini} = 50 \%$$

$$V_{bat} = V_{OCV} - R_{in} I_{bat} = 300 - 0.1 \times I_{bat}$$

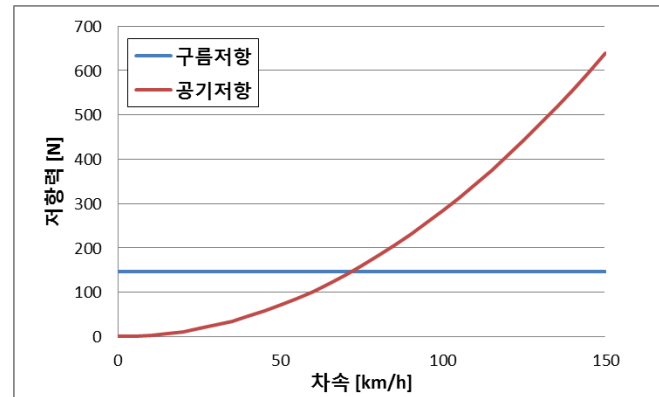
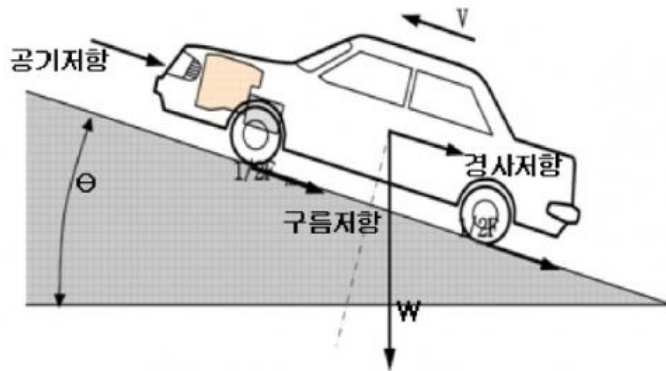
$$T_{mot} \omega_{mot} = \eta V_{bat} I_{bat} \longrightarrow 0.1 I_{bat}^2 - 300 I_{bat} + 10,000 = 0$$

$$I_{bat} = 2966 \text{ or } 33.7 \text{ A}$$

$$SOC = SOC_{ini} - \frac{100}{C_{nom}} \int I_{bat} dt = 50 - 0.084 \times 120 = 39.9 \%$$

Driving resistances

- Drag forces during the driving from the various conditions
- Air, rolling, climbing, and acceleration resistance



< Air resistance >



< Rolling resistance >



< Climbing resistance >



Resistance Calculation Model

- Input : vehicle speed, gradient
- Output : drag force

1. Air resistance

$$F_{air} = \frac{1}{2} C_d A_{fr} \rho_{air} V_{veh}^2$$

C_d : air drag coefficient

 A_{fr} : frontal area [m²] ρ_{air} : air density [kg/m³] V_{veh} : vehicle speed [m/s²]

2. Rolling resistance

$$F_{roll} = \mu_r m_b g$$

 μ_r : rolling friction coefficient m_b : body mass[kg]

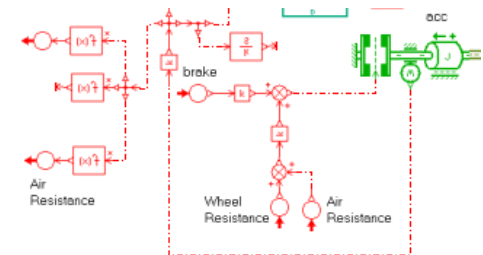
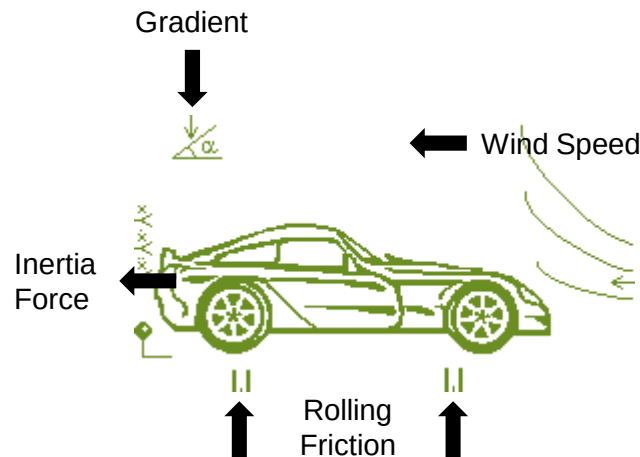
3. Climbing resistance

$$F_c = m_b g \sin \theta_{grad}$$

 θ_{grad} : gradient [rad]

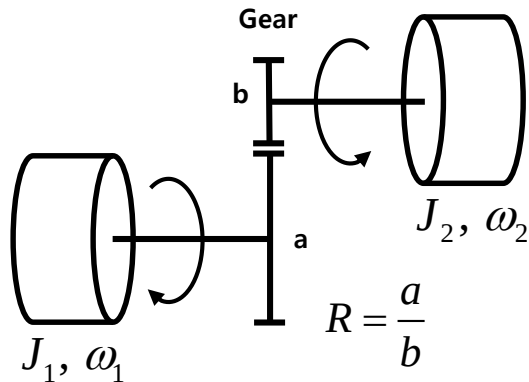
4. Acceleration resistance

$$F_{acc} = ma = J_{eq} \alpha_{whl} R_{tire}$$

 J_{eq} : vehicle equivalent inertia at wheel [kgm²] α_{whl} : wheel rotational acceleration [rad/s²] R_{tire} : effective tire radius [m]

Equivalent Inertia

- Calculation of an equivalent inertia from each inertias



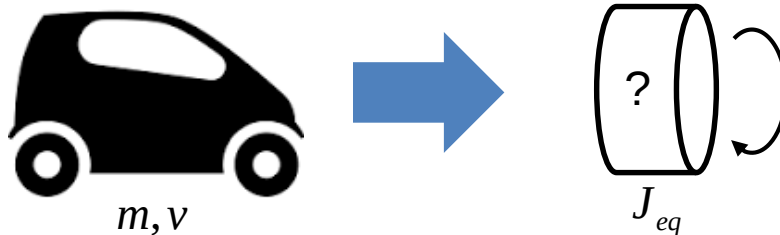
$$E_1 + E_2 = E_{eq} \quad (\text{energy conservation})$$

$$\frac{1}{2} J_1 \omega_1^2 + \frac{1}{2} J_2 \omega_2^2 = \frac{1}{2} J_{eq,1} \omega_1^2$$

$$J_1 \omega_1^2 + J_2 R^2 \omega_1^2 = J_{eq,1} \omega_1^2 \quad (\omega_2 = R \omega_1)$$

$$J_{eq,1} = J_1 + J_2 R^2 \longleftrightarrow J_{eq,2} = \frac{J_1}{R^2} + J_2$$

Equivalent inertia at wheel w.r.t vehicle mass



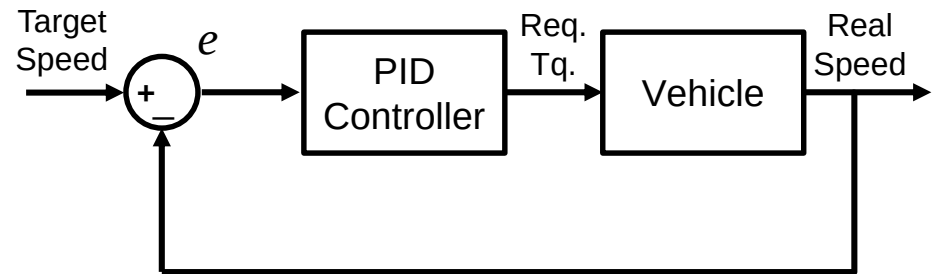
$$E_v = E_w$$

$$\frac{1}{2} m_b V_{veh}^2 = \frac{1}{2} J_{eq} \omega_{whl}^2 \quad (V_{veh} = R_{tire} \omega_{whl})$$

$$J_{eq} = m_b R_{tire}^2$$

Driver Controller

- Torque control to match a target vehicle speed from the driver request
- Operating principle
 - Reducing an error between the target speed and the real speed



$$T_{req} = K_p e(t) + K_i \int e(t) dt + K_d \frac{de(t)}{dt} \quad \begin{cases} e(t) \geq 0 : \text{accelation} \\ e(t) < 0 : \text{braking} \end{cases}$$

$$(e(t) = V_{\text{target}} - V_{\text{real}})$$

K_p : proportional gain

K_i : integral gain

K_d : differential gain

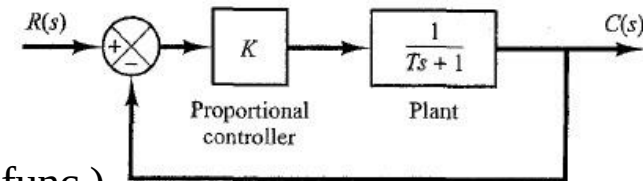
PI control

- Proportional control

$$G(s) = \frac{K}{Ts + 1} \quad \frac{E(s)}{R(s)} = \frac{R(s) - C(s)}{R(s)} = 1 - \frac{C(s)}{R(s)} = \frac{1}{1 + G(s)}$$

$$E(s) = \frac{1}{1 + G(s)} R(s) = \frac{1}{1 + \frac{K}{Ts + 1}} R(s) \quad R(s) = \frac{1}{s} \text{ (unit-step func.)}$$

$$E(s) = \frac{Ts + 1}{Ts + 1 + K} \frac{1}{s} \quad e_{ss} = \lim_{t \rightarrow \infty} e(t) = \lim_{s \rightarrow 0} sE(s) = \lim_{s \rightarrow 0} \frac{Ts + 1}{Ts + 1 + K} = \frac{1}{K + 1}$$

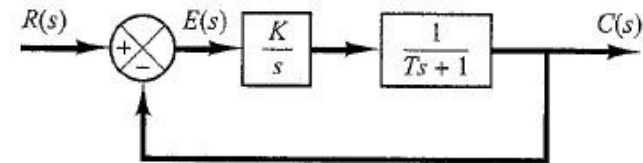


- Integral control

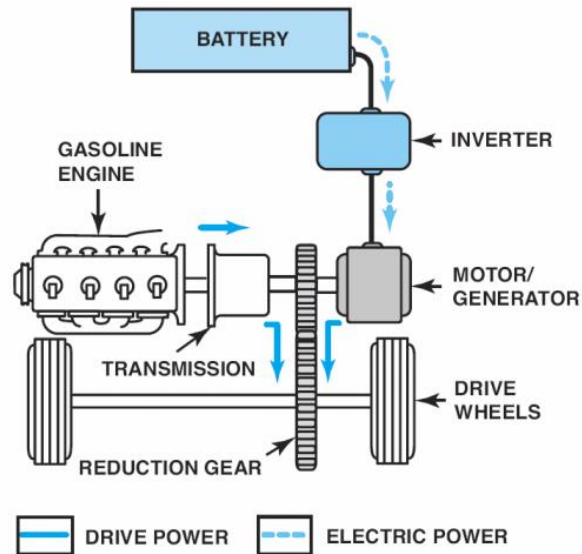
$$\frac{C(s)}{R(s)} = \frac{K}{s(Ts + 1) + K} \quad \frac{E(s)}{R(s)} = \frac{R(s) - C(s)}{R(s)} = \frac{s(Ts + 1)}{s(Ts + 1) + K}$$

$$E(s) = \frac{s(Ts + 1)}{s(Ts + 1) + K} \frac{1}{s} \quad R(s) = \frac{1}{s} \text{ (unit-step func.)}$$

$$e_{ss} = \lim_{t \rightarrow \infty} e(t) = \lim_{s \rightarrow 0} sE(s) = \lim_{s \rightarrow 0} \frac{s^2(Ts + 1)}{Ts^2 + s + K} \frac{1}{s} = 0$$



Assignment



Vehicle Parameters

$$J_{eng} = 0.2 \text{ kgm}^2, J_{motor} = 0.05 \text{ kgm}^2$$

$$GR_{TM} = 2, GR_F = 4$$

$$M_{veh} = 1500 \text{ kg}, R_{tire} = 0.3$$

$$T_{eng} = 80 \text{ Nm}, T_{mot} = 50 \text{ Nm}$$

Resistance Parameters

$$A = 2 \text{ m}^2, C_d = 0.3, \rho = 1.2 \text{ kg/m}^3, V = 15 \text{ m/s}$$

$$\mu_{roll} = 0.01, g = 9.81 \text{ m/s}^2$$

Problems

1. Equivalent inertia at wheel
2. Driving torque at wheel
3. Drag torque at wheel (air, rolling)
4. Vehicle acceleration speed

$$(\text{Driving torque} - \text{Drag torque}) = \text{Eq. Inertia} \times \text{Acceleration rotational speed}$$

$$\text{Eq. Inertia} : 148.6 \text{ [kgm}^2\text{]}$$

$$\text{Driving Torque} : 840 \text{ [Nm]}$$

$$\text{Drag Torque} : 68.44 \text{ [Nm]}$$

$$\text{Vehicle Acc.} : 1.558 \text{ [m/s}^2\text{]}$$