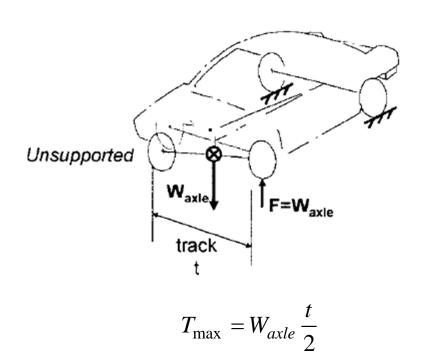
Design for Body Torsion

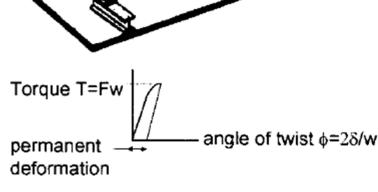
- Body torsion requirements
 - Body torsion strength
 - Body torsion stiffness
 - For midsize vehicle: K = 12000 Nm/°, T = 6250 Nm
- Internal loads during global torsion: load path analysis
- Analysis of body torsional stiffness
 - Shear strain energy
 - Effective shear stiffness
- Torsional stiffness of convertibles and framed vehicles

5.1 Body Torsion Strength Requirement

δ, F

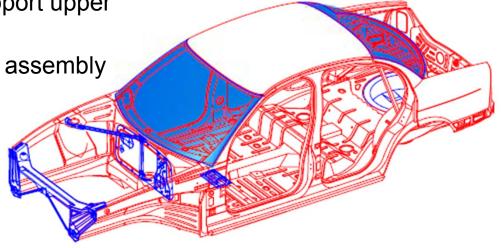
- Maximum torque to recover its shape with little deformation upon removal
- Vehicle-use condition: twist ditch maneuver
 - Input: δ , output: F (load cell)





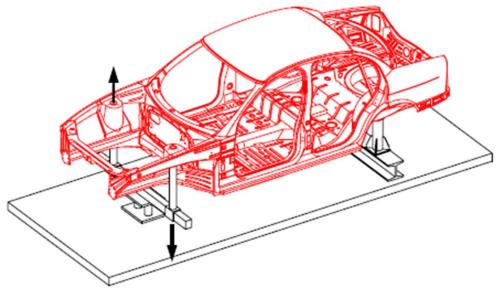
Test Configuration

- Welded body structure
- Bonded windshield and back light (aluminum panels)
- Bonded and bolted panel dash insert
- Bonded panel spare tire tub
- Bolted reinforcement panel dash brake booster
- Bolted braces radiator
- Bolted reinforcement radiator rail closeout RH/LH
- Bolted reinforcement radiator support upper
- Bolted tunnel bridge lower/upper
- Bolted brace cowl to shock tower assembly
- Holding
 - Front: at panel skirt RH/LH
 - Rear: at plate rear spring upper
- Measurement
 - 12 stadia rods along the front rails, rockers, rear rails



Static Torsion

- Constraint: two locations at the plate spring rear upper
- Load: panel skirt RH/LH by a scale beam, from M = 1000Nm to 4000Nm

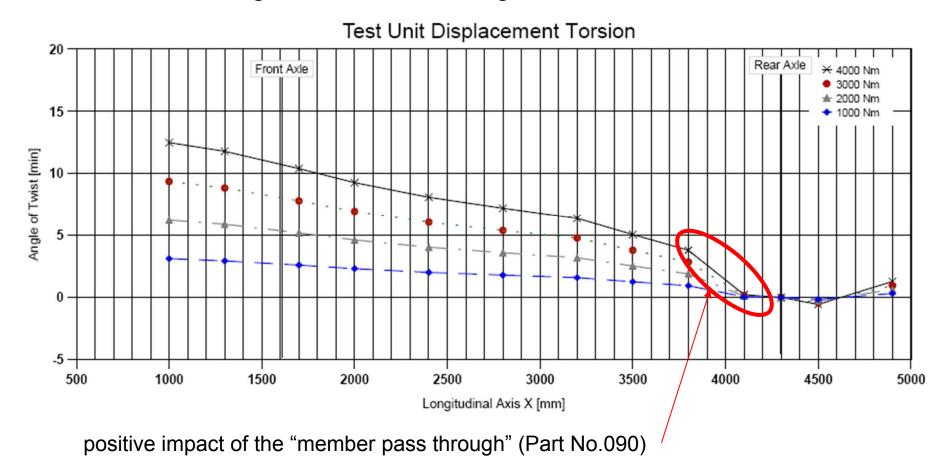




Static Torsion: Test Results

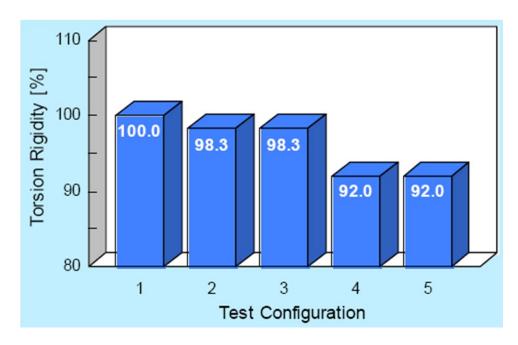
With glass: 21,620 Nm/deg

Without glass: 15,790 Nm/deg

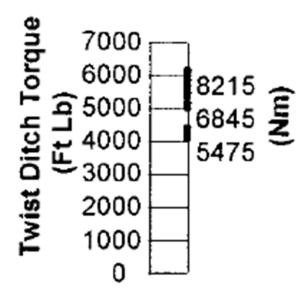


Static Torsion: impact of bonded and/or bolted parts

- 1. full configuration
- 2. as 1, but without braces radiator
- 3. as 2, but without radiator support upper
- 4. as 3, but without bolted brace cowl to shock tower assembly
- 5. as 4, but without tunnel bridge



Torsion Strength Benchmark Data



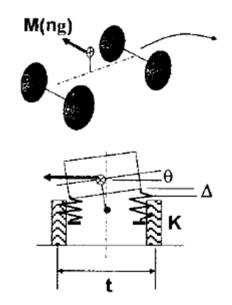
Range for 20 Cars from Small to Luxury Segments

5.2 Body Torsion Stiffness Requirement

- Body torsion test
 - Slope in the linear region of the applied couple vs. angular rotation
- Required functions for high torsional stiffness
 - Good handling property: torsionally stiff body relative to the suspension stiffness
 - Torsional stiffness: 10,000 Nm/°
 - Solid structural feel: minimize relative deformations which cause squeaks and rattles
 - Feel of solidness over road irregularities
 - Related to fundamental natural frequency of the body twisting mode: the higher, the more desirable solid feel
 - Desirable vehicle torsional frequency range: 22~25 Hz
 - Torsional stiffness (benchmarking): 12,000 Nm/°

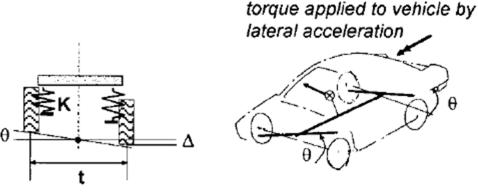
Good Handling Properties (1)

- Corner turn: roll on the suspension ride spring
- Weight transfer from the inside wheels to the outside wheels
- Affect the steering characteristics of the vehicle
- Suspension design: rigid body assumption → high torsional stiffness (much stiffer than the roll stiffness: 1000 Nm/°)



Roll Gain: Degrees of Vehicle Roll per g of Lateral Acceleration: θ/n

First order estimate of vehicle roll stiffness

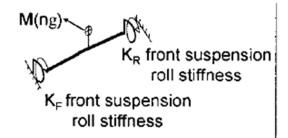


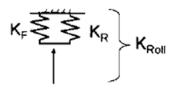
$$K_{RollVehicle} = K_{RollFront} + K_{RollRear} = \frac{t^2 K_{RideFront}}{2} + \frac{t^2 K_{RideRear}}{2}$$

$$= 1560mm$$
 $K_{Ride} = 23.4N / mm$ $\rightarrow K_{Roll} = 57,000Nm / rad = 1000Nm / deg$
Body Torsion - 9

Good Handling Properties (2)

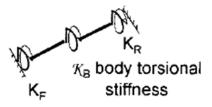
For typical passenger cars, K_{body} = 10,000 Nm/°

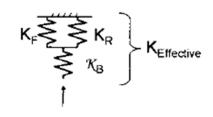




Ideally Rigid Body

Only suspension roll rate





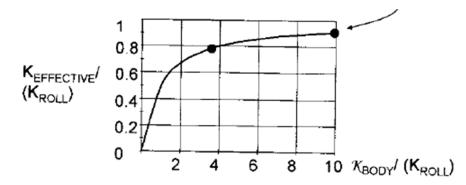
Model with Body Torsional Stiffness K_{eff} : stiffness with a torsionally flexible body

 K_{roll} : suspension stiffness with a rigid body

 K_B : body torsional stiffness

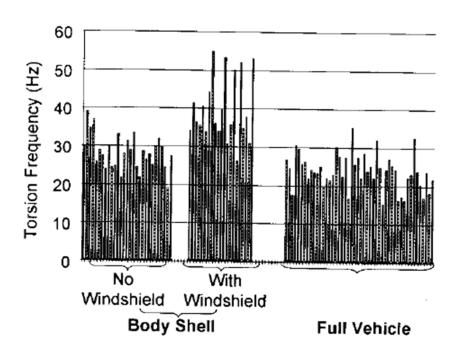
$$K_{eff} = \frac{K_{roll}K_B}{K_{roll} + K_B} \rightarrow \frac{K_{eff}}{K_{roll}} = \frac{1}{\frac{K_{roll}}{K_B} + 1} = \frac{1}{\frac{1}{\frac{K_B}{K_{roll}}} + 1}$$

$$\frac{K_{eff}}{K_{roll}} = 0.9$$
(wish to approach 1) $\rightarrow K_B = 10 K_{roll}$

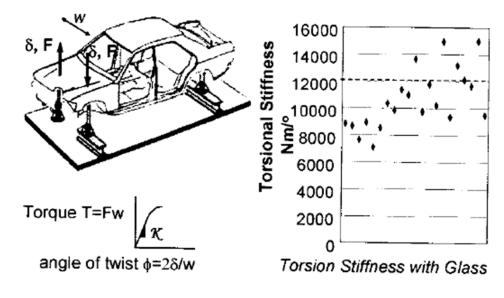


Benchmark Data

Torisional frequency



Torsional stiffness



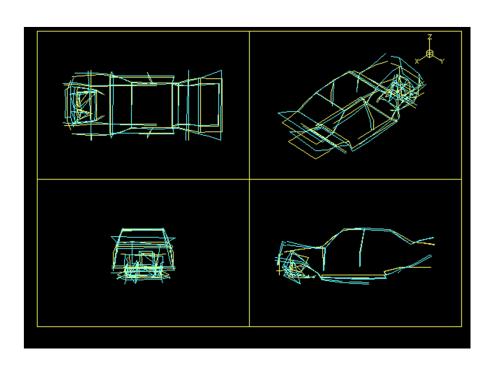
Body-In-White: TOYOTA-CAMRY

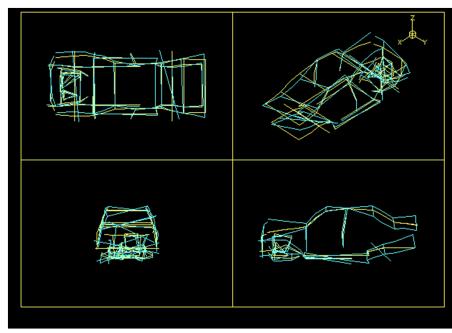
Nameplate CAMRY - Model XLE -Year 1992
 Style 4 DR , Vehicle class MID-SIZE
 Overall length (m) 4.77 , Overall width (m) 1.77 ,
 Overall height (m) 1.4 , Wheelbase (m) 2.62
 Base price (\$) 20,508 , Seating capacity 5 , Curb weight (Kg) 1493
 Body/frame UNIBODY , Body material STEEL Fuel economy (MPG) 18/24 , Engine 3.0L, V6, TRANS DOHC , Chassis layout FRONT ,
 Transmission 4 SP AUTO
 Suspension front MacPHERSON STRUT ,
 Suspension rear INDEPENDENT DUAL-LINK





Vibration: TOYOTA-CAMRY



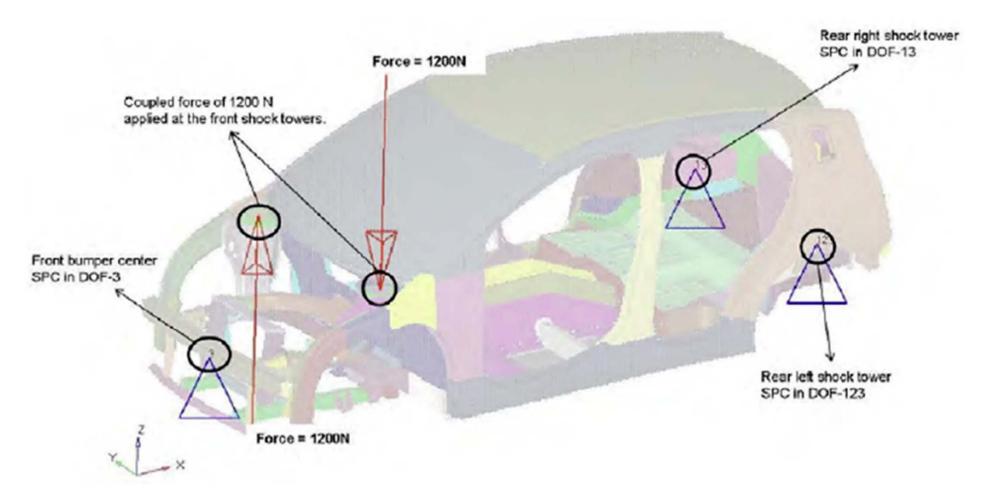


Bending

Torsion

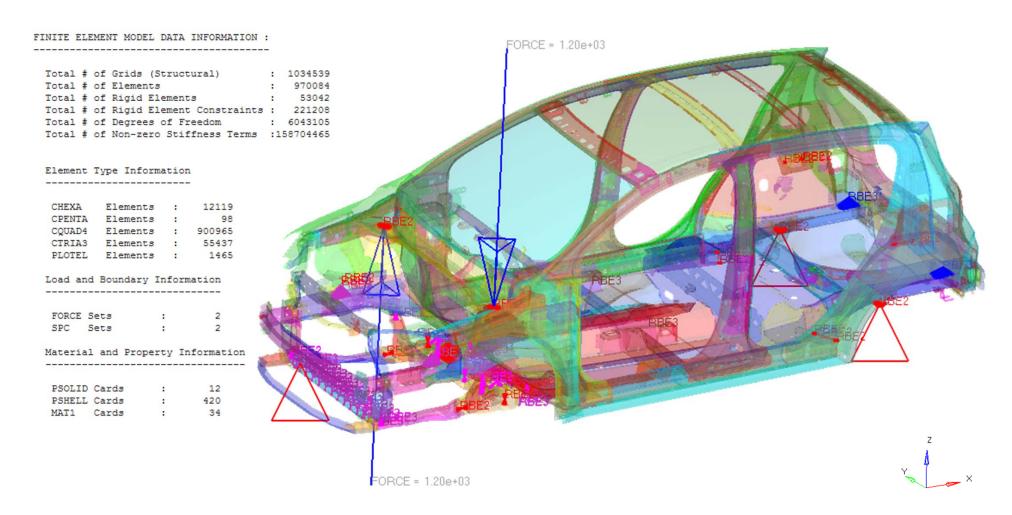
Torsion Stiffness

Constraints and Loading in FSV Report

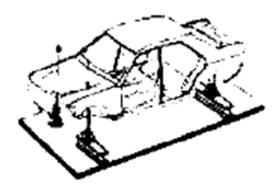


Torsion Stiffness

· Constraints and Loading in Hypermesh



Typical Torsional Requirements: Midsize Vehicle



Restraints at Suspension Attachments

Torsion Stiffness

Nominal Value
Stiffness = 12000 Nm/o

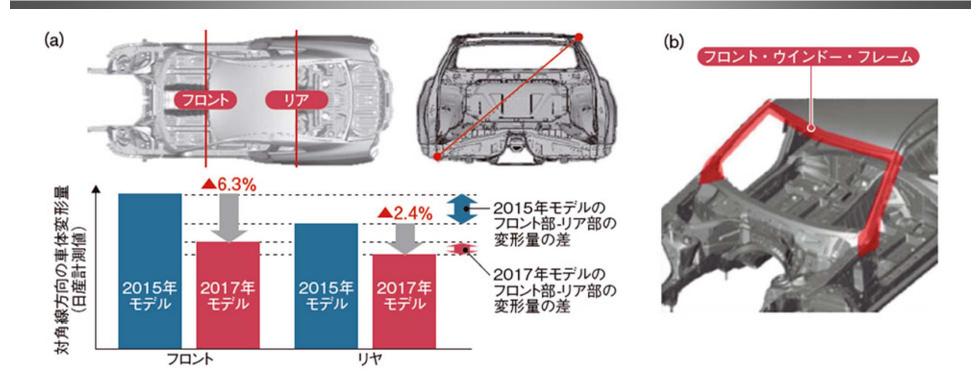
Torsion Strength

Nominal Value

T= 6250Nm

no permanent deformation

Nissan GT-T (2016.05.10)

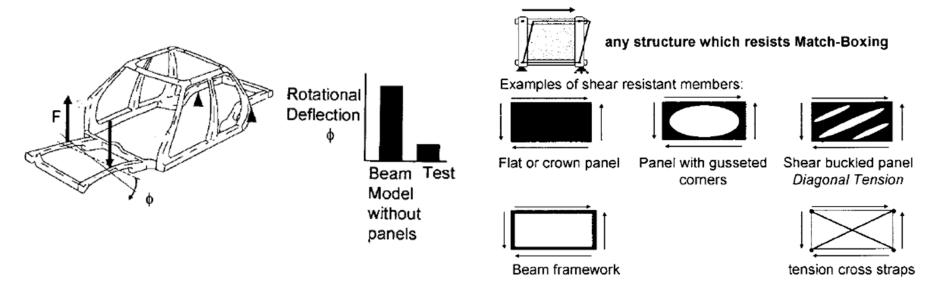






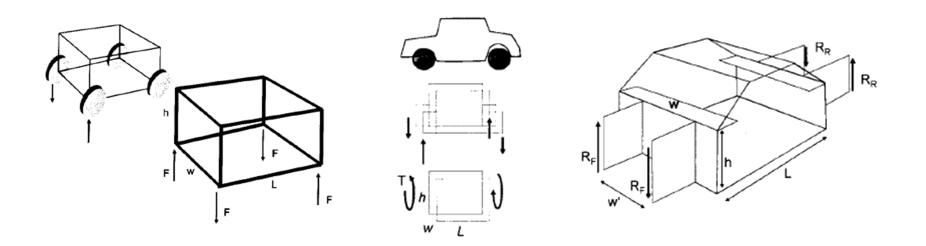
5.3 Load Path Analysis: Global Torsion

- Understand how global body requirements flow down to loads on structural elements
- Idealized structure as a framework of beams
 - Torsional stiffness: 10~30% of experimental values
- Dominant structure in reaction torsion loading
 - Surface: shear resistant members



Models in Torsion

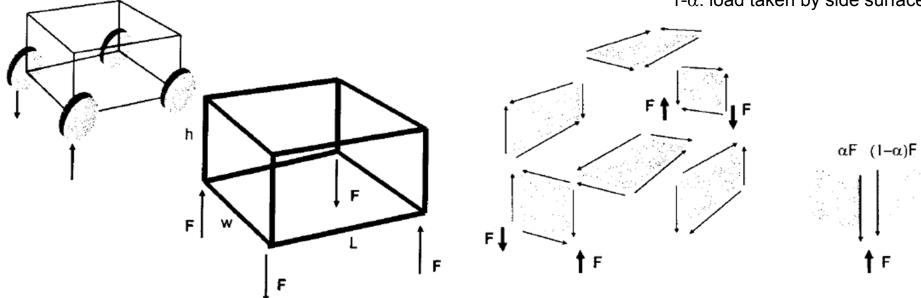
- Monocoque box model
- Passenger cabin model
- Structural surface and bar model



Simple Box Model

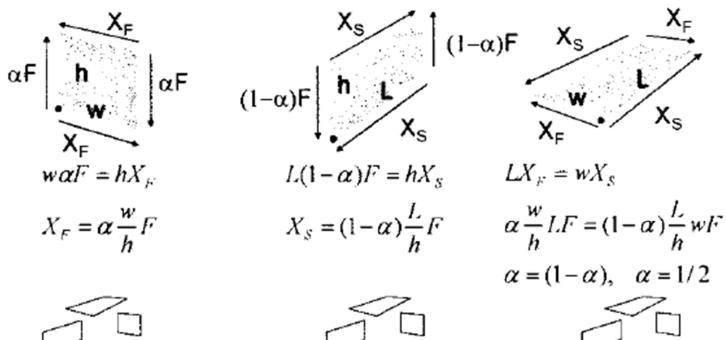
- All surfaces are loaded
- Internal loads are independent of material properties
- Each surface is necessary to react the applied torsional couple: removal of any single surface will not allow the required equilibrium and the box will collapse
- Shear flow is equal for all edges

 α : load taken by front surface 1- α : load taken by side surface

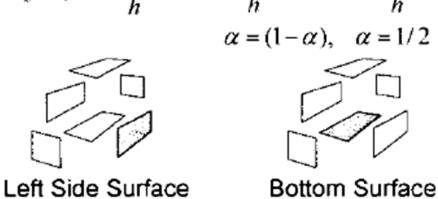


Vehicle Structure

Box Model Internal Loads

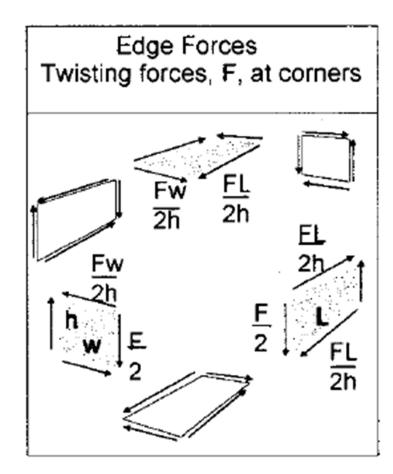


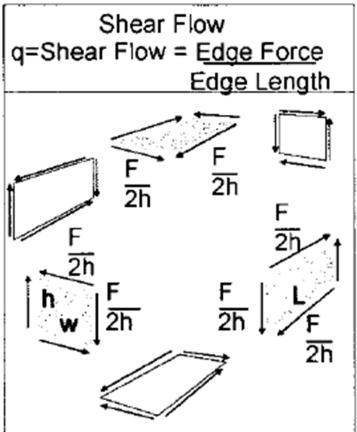
Front Surface



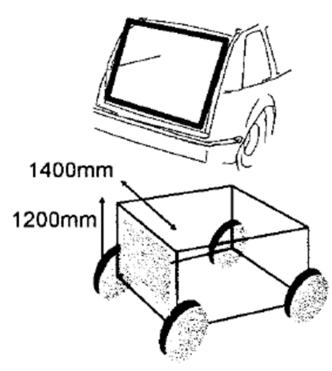
Body Torsion - 21 Vehicle Structure

Monocoque Box in Torsion





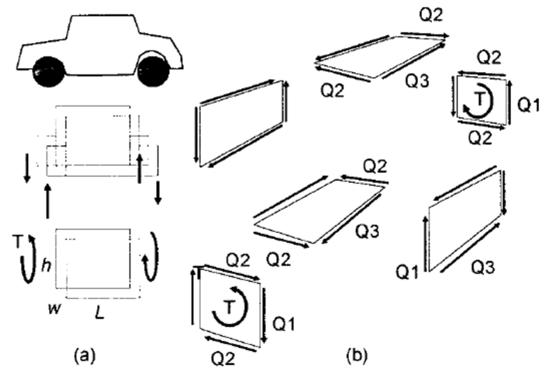
Example: Van Rear Hatch Opening



Twist Ditch Torque=7x106Nmm

 Determine shearing loads which need to be reacted by the rear hatch structure.

Passenger Cabin Internal Loads



$$+ wQ_1 + hQ_2 = T \text{ (front)}$$

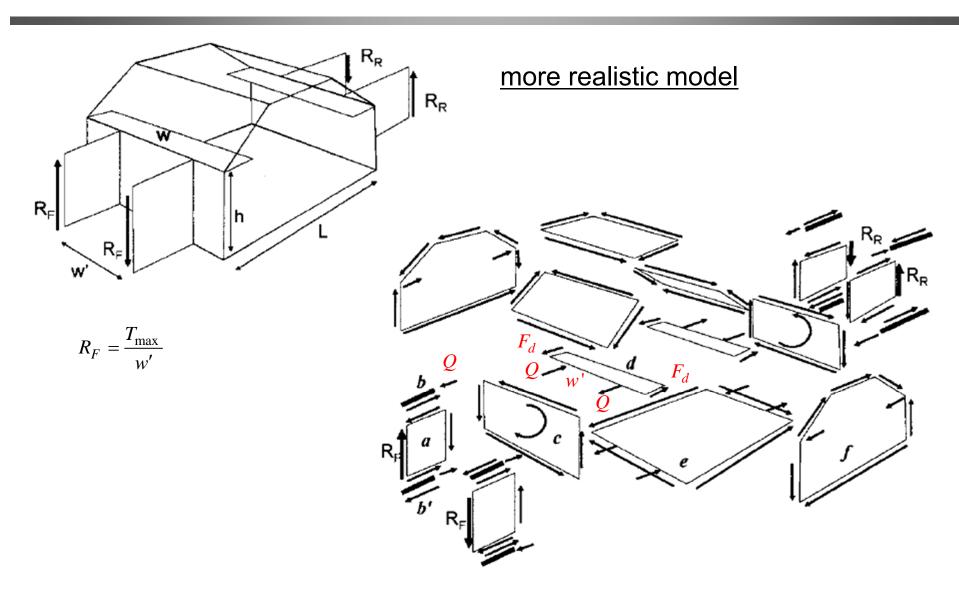
$$-LQ_2 + wQ_3 = 0 \text{ (top)}$$

$$-LQ_1 + hQ_3 = 0 \text{ (side)}$$

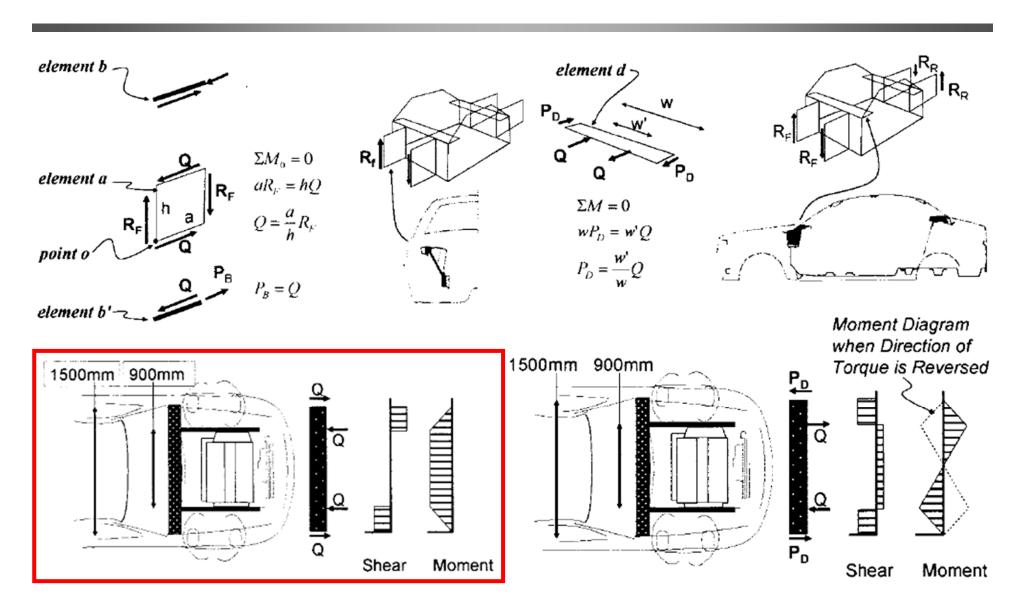
$$\rightarrow \begin{bmatrix} w & h & 0 \\ 0 & -L & w \\ -L & 0 & h \end{bmatrix} \begin{bmatrix} Q_1 \\ Q_2 \\ Q_3 \end{bmatrix} = \begin{bmatrix} T \\ 0 \\ 0 \end{bmatrix} \rightarrow \mathbf{AQ} = \mathbf{T}$$

$$\mathbf{Q} = \mathbf{A}^{-1}\mathbf{T} \to \begin{bmatrix} Q_1 \\ Q_2 \\ Q_3 \end{bmatrix} = \frac{1}{2whL} \begin{bmatrix} hL & h^2 & -hw \\ wL & -wh & w^2 \\ L^2 & Lh & Lw \end{bmatrix} \begin{bmatrix} T \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} T/2w \\ T/2h \\ TL/2wh \end{bmatrix}$$

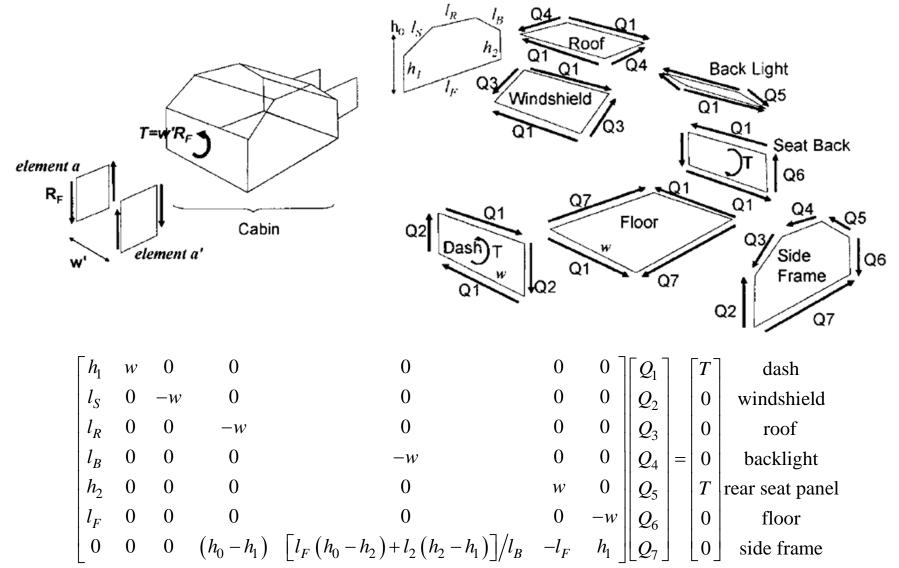
Structural Surface and Bar Model



Internal Loads



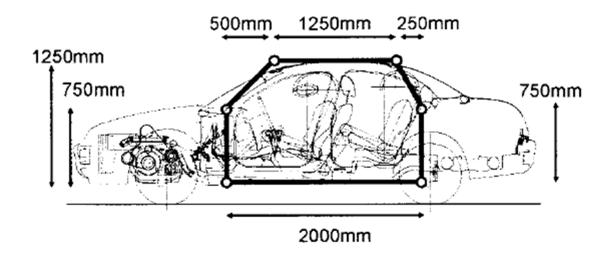
Shear Loads on Cabin Panels



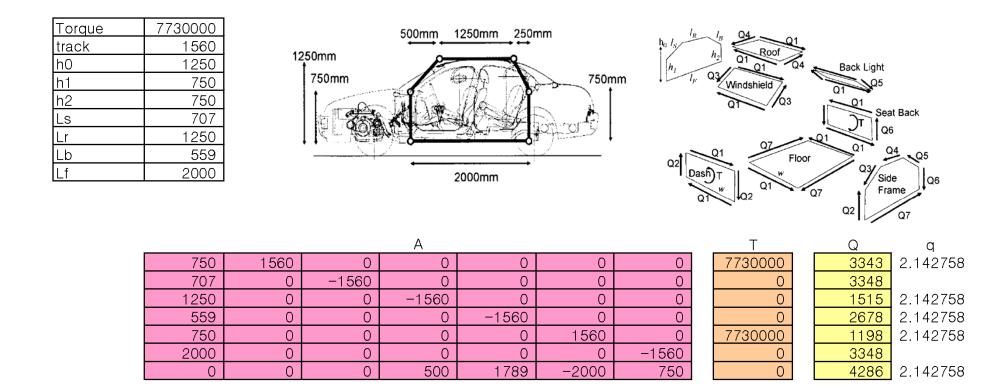
Vehicle Structure

Example: Midsize Sedan Data

- Determine internal shear loads
 - Track = 1560 mm
 - Twist ditch torque = 7,730 Nm



Example: Shear Loads



5.4 Analysis of Body Torsional Stiffness

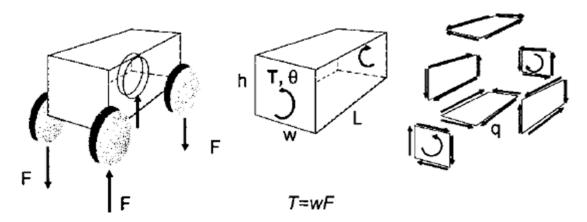
Shear strain energy of a surface

$$e = \int \frac{\tau \gamma}{2} dV = \int \frac{\tau^2}{2G} dV = \frac{(q/t)^2}{2G} (abt) = q^2 \frac{ab}{2(Gt)}$$

Energy balance for torque loaded box

$$\frac{1}{2}T\theta = \sum_{\text{all surfaces}} \frac{1}{2}q^{2} \left[\frac{ab}{(Gt)} \right]_{i} \xrightarrow{q = \frac{F}{2h} = \frac{T/w}{2h} = \frac{T}{2wh}} \xrightarrow{1} T\theta = \sum_{\text{all surfaces}} \frac{1}{2} \left(\frac{T}{2wh} \right)^{2} \left[\frac{ab}{(Gt)} \right]_{i}$$

$$\theta = T \left(\frac{1}{2wh} \right)^{2} \sum_{\text{all surfaces}} \left[\frac{ab}{(Gt)} \right]_{i} \xrightarrow{K} = \frac{T}{\theta} = (2wh)^{2} \frac{1}{2wh} \xrightarrow{\text{all surfaces}} \left[\frac{ab}{(Gt)} \right]_{i}$$



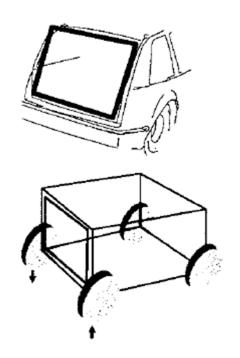
Vehicle Structure

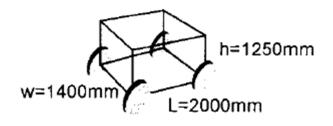
Series Spring Analogy

Consider a set of six linear springs in series

- How to increase torsional stiffness?
 - Identify which surfaces is the most flexible: lowest $\left\lfloor \frac{(Gt)}{ab} \right\rfloor$
 - Increase the stiffness of the least stiff spring

Example: Box Van





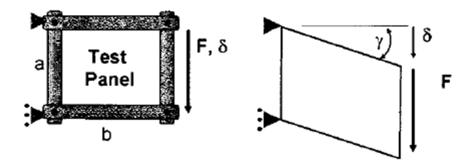
All Panels Steel G=80,000N/mm² t=1 mm

- $K = 6.95 \times 10^{10} \text{ Nm/rad} = 1,200,000 \text{ Nm/}^{\circ}$
- About 100 times stiffer than measured data
- Why?
 - Ideal flat plate assumption: surfaces remain perfectly flat during loading
 - Reality: out-of-plane shape, holes and cutouts, framework of beams with flexible joints
- Effective shear stiffness: (Gt)_{eff}

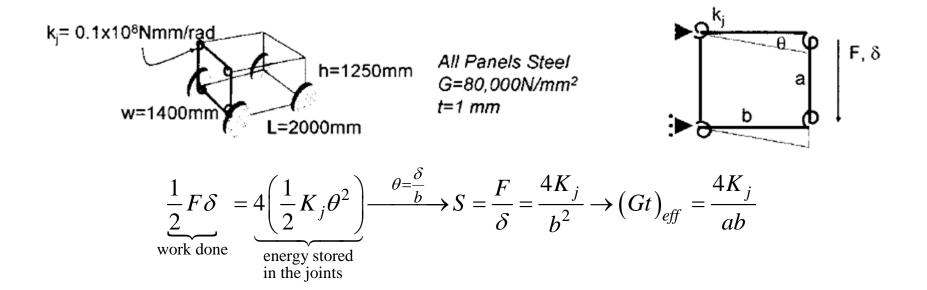
Effective Shear Stiffness

- Test panel in a pinned frame fixture
 - (Gt)_{eff}: shear stiffness for a panel
 - S: measured stiffness (slope of load vs. deflection curve)
 - Physical test / FEM
 - a: panel dimension of the side load is applied
 - b: adjacent side dimension

$$G = \frac{\tau}{\gamma} \xrightarrow{\tau = \frac{F}{at}, \ \gamma = \frac{\delta}{b}} (Gt)_{eff} =$$



Example: Van Hatch Opening (1)



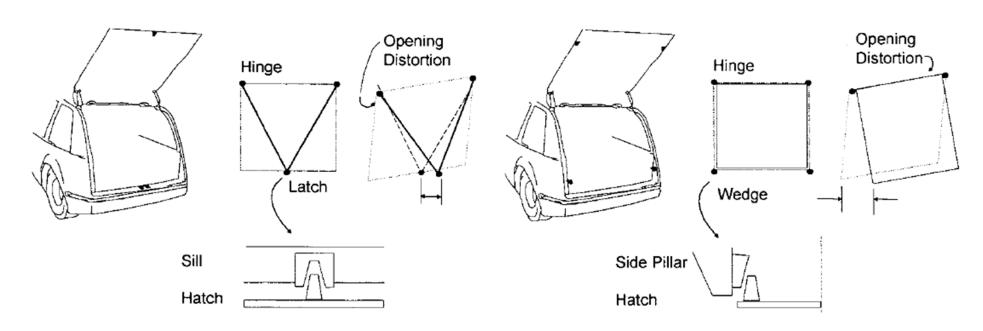
- Replace the rear panel with an open frame of rigid links with a typical joint stiffness
 - Typical joint stiffness: $K_i = 0.1x10^8 \text{ Nm/rad}$
- Much more flexible frame than the original assumption of a flat panel

Example: Van Hatch Opening (2)

- $K = 1.6x10^8 \text{ Nm/rad} = 2807 \text{ Nm/}^{\circ}$
- Influence of the hatch opening: rear surface
 - Only one surface of the closed box need be flexible to reduce the stiffness for the whole box

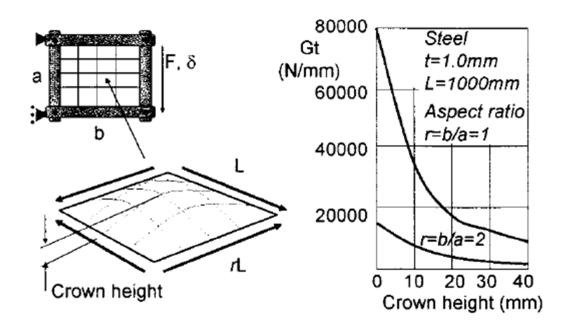
Example: Van Hatch Opening (3)

- In practice, increase the shear stiffness of the rear surface
- Typically the hinge and latch are not sufficiently stiff
- Mechanisms to wedge the door into the opening



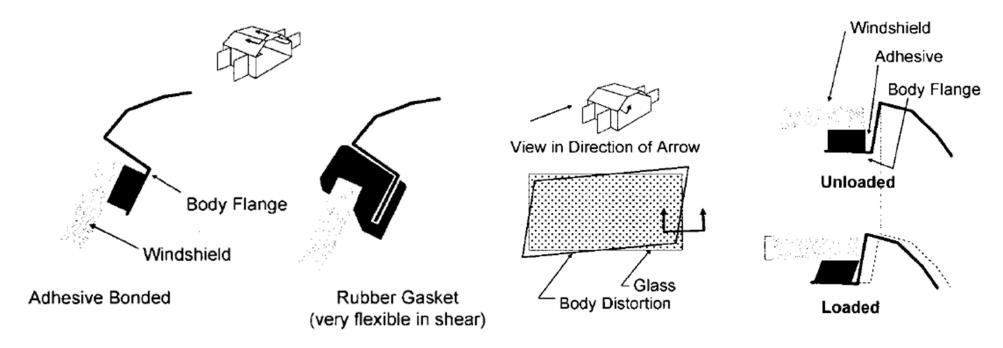
Example: Crowned Panels

- Improve panel stiffness for normal loading such as dent resistance and panel vibration
- Effective shear stiffness?
 - FEA model of the shear test fixture
 - Much smaller than a flat panel (unrealistically high)



Example: Windshield (1)

- All surfaces enclosing the cabin must act as shear resistant members
- Most effective for shear resistance: adhesive bonding

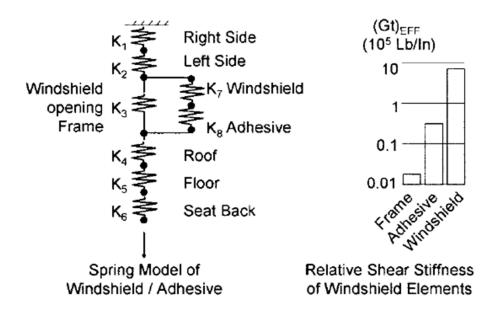


windshield retention alternatives

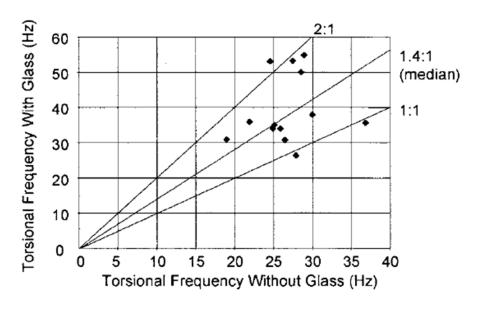
effective shear stiffness of windshield

Example: Windshield (2)

 Windshield model for torsional stiffness

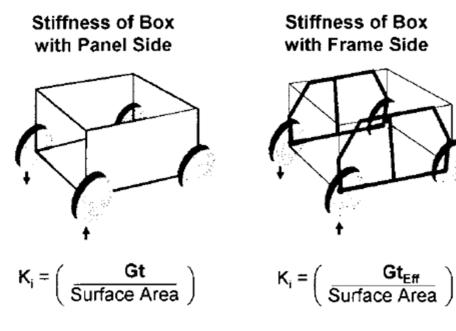


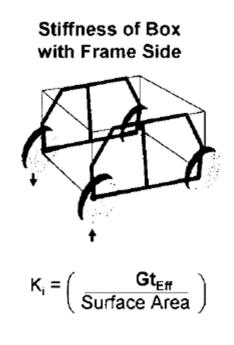
- Effect of windshield on torsional frequency
 - Increase with glass: torsionally stiffer body
 - No increase: very stiff body windshield opening perimeter

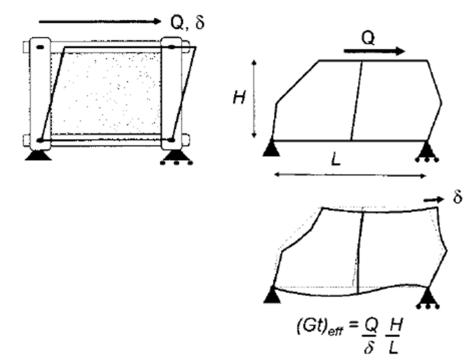


Example: Side Frame Model (1)

- Contribution to torsional stiffness
- Effective shear stiffness

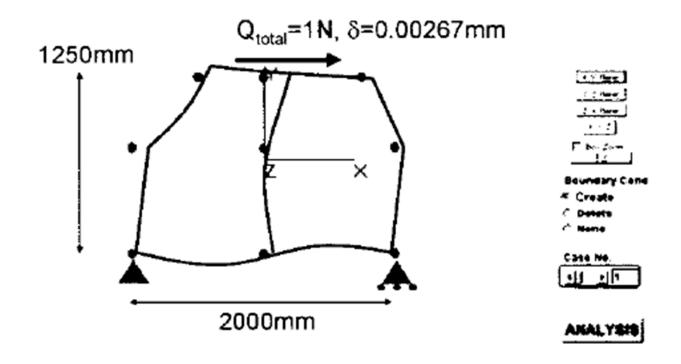






Example: Side Frame Model (2)

FEA under shear loading



$$(Gt)_{Eff} = \left(\frac{Q}{\delta}\right)\frac{H}{L} = \left(\frac{1N}{.00267mm}\right)\frac{1250mm}{2000mm} = 234N/mm$$

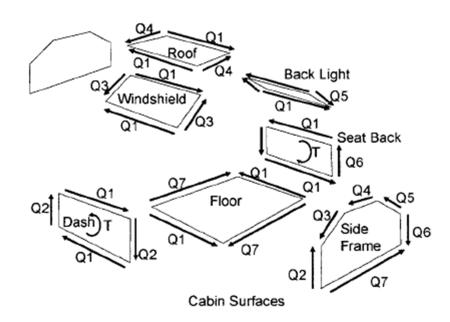
Torsional Stiffness of a Vehicle Cabin

- Solve for internal shear loads: Q = A⁻¹T
- Find the resulting shear flow on any non-loaded surface:q = Q/(side length)
- Determine the effective shear stiffness: (Gt)_{eff}
- Determine the torsional stiffness of the cabin: (q/T), (Gt)_{eff}, surface area

$$\frac{1}{2}T\theta = \sum_{\text{all surfaces}} \frac{1}{2}q^{2} \left[\frac{ab}{(Gt)}\right]_{i}$$

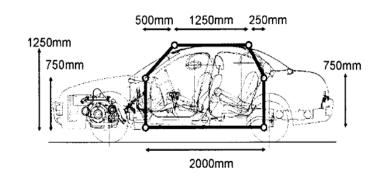
$$\frac{\theta}{T} = \left(\frac{q}{T}\right)^{2} \sum_{\text{all surfaces}} \left[\frac{\text{area of surface}}{(Gt)_{eff}}\right]_{i}$$

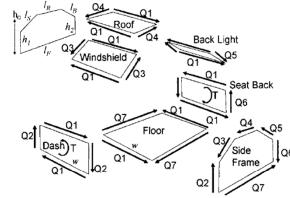
$$K = \frac{1}{\left(\frac{q}{T}\right)^{2} \sum_{\text{all surfaces}} \left[\frac{\text{area of surface}}{(Gt)_{eff}}\right]_{i}}$$



Example: Sedan

Torque	7730000
track	1560
h0	1250
h1	750
h2	750
Ls	707
Lr	1250
Lb	559
Lf	2000





			Α			
750	1560	0	0	0	0	0
707	0	-1560	0	0	0	0
1250	0	0	-1560	0	0	0
559	0	0	0	-1560	0	0
750	0	0	0	0	1560	0
2000	0	0	0	0	0	-1560
0	0	0	500	1789	-2000	750

T	_	Q
7730000		3343
0		3348
0		1515
0		2678
7730000		1198
0		3348
0		4286

panel	area	(Gt)eff	area/(Gt)eft
dash	1170000	80000	14.6
windshield	1103087	80000	13.8
roof	1950000	80000	24.4
back light	872067	80000	10.9
seat back	1170000	80000	14.6
floor	3120000	80000	39.0
side frame:L	2312500	234	9882.5
side frame:R	2312500	234	9882.5
SUM			19882.3

$$K = \frac{1}{\left(\frac{q}{T}\right)^{2} \sum_{\text{all surfaces}} \left[\frac{\text{area of surface}}{\left(Gt\right)_{eff}}\right]_{i}}$$

= 6.55E + 08Nmm/rad

=11,423Nm/°

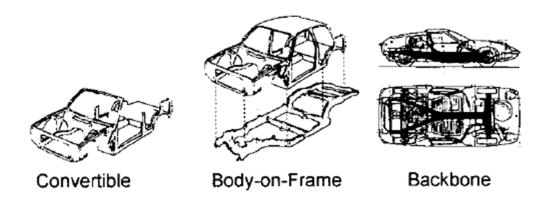
2.142758

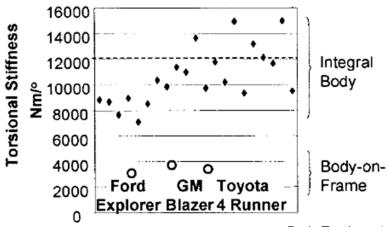
2.1427582.1427582.142758

2.142758

5.5 Torsional Stiffness of Framed Vehicle

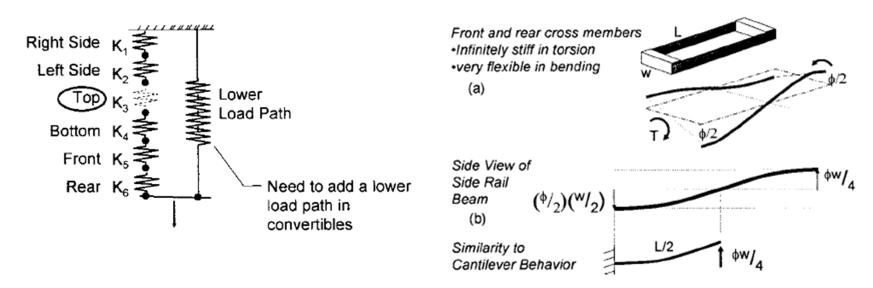
- Effective structure for torsional stiffness: large central closed section, but limited to seating arrangements
- Monocoque structure
 - efficient in reacting torsional loading
- Alternatives
 - Convertible: absence of top surface
 - Body-on-frame: common for passenger and utility vehicle
 - Backbone frame: closed thin walled sections → shear buckling





Convertibles

- Lower load path to resist torsional loads: differential bending of the rocker beams
- Lower structure: two cross members (front: dash, rear: rear seat back), two side beams
 - Cross member: infinitely rigid in torsion → zero twist along crosscar axes, flexibility in bending → side rails are not twisted down
 - Side rail: pure bending with zero slope at its ends



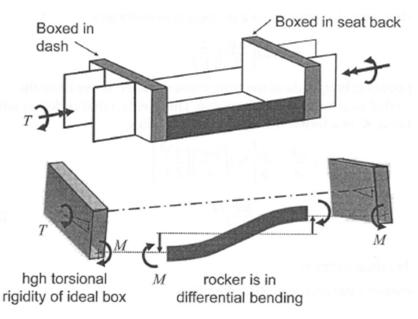
Effect of Differential Bending

 Behavior for the front half: cantilever beam of length L/2

$$\delta = \frac{Fl^3}{3EI} = \left(\frac{w}{2}\right) \left(\frac{\phi}{2}\right) \to F = 3EI \left(\frac{w\phi}{4}\right) \left(\frac{2}{L}\right)^3$$

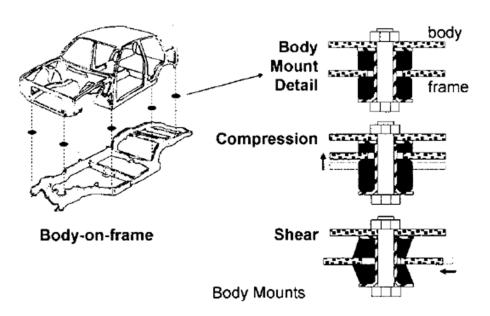
$$K = \frac{T}{\phi} = \frac{wF}{\phi} = \frac{w}{\phi} \left[3EI \left(\frac{w\phi}{4} \right) \left(\frac{2}{L} \right)^3 \right] = \frac{6w^2 EI}{L^3}$$

- In practice
 - large closed box section at dash and rear seat back
 - Difficulty: cross member to side rail joint
 - Zero slope: very large bending moment
 - Stress concentration at the joint



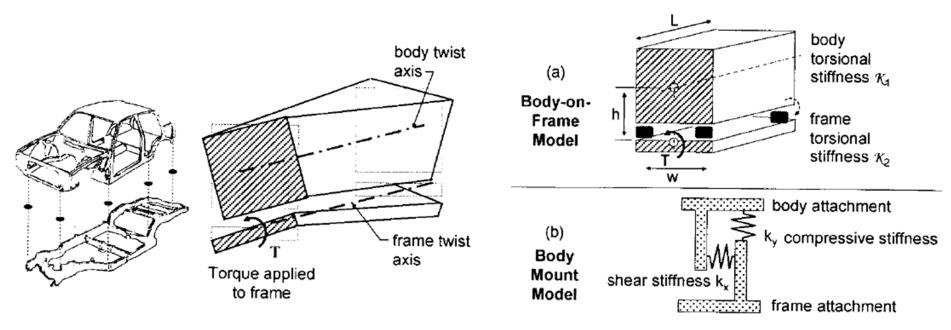
Body-on-Frame

- Body shell, ladder frame, elastomeric body mounts
- Body mounts
 - Relative motion between the frame and body both in vertical direction (compression) and in lateral direction (shear)
 - Isolation of structure borne noise and vibration from the frame into the body



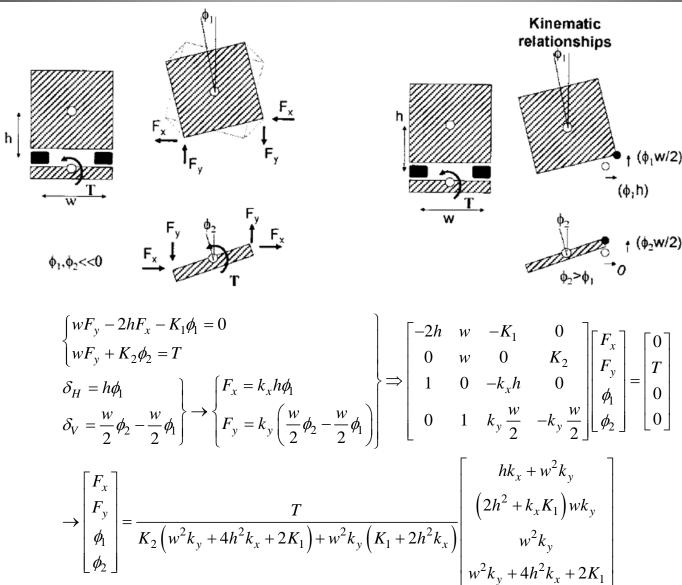
Body-on-Frame: Torsion Model

- Torque applied to the frame through the suspension
 - Twist about different longitudinal axes
 - Shearing deformation in the body mounts
 - Reduce the stiffness of the system: K < K1 + K2



Vehicle Structure

Body-on-Frame: Torsional Stiffness (1)



Body-on-Frame: Torsional Stiffness (2)

$$K_{vehicle} = \frac{T}{\phi_2} = K_2 + K_1 \psi + 2h^2 k_x \psi$$

$$\psi = \frac{1}{1 + \frac{2h^2k_x}{\left(\frac{w^2}{2}k_y\right)} + \frac{K_1}{\left(\frac{w^2}{2}k_y\right)}}$$

 K_1 , K_2 : torsional stiffness of the body and frame

 k_x , k_y : mount stiffness in the horizontal and vertical directions

h: height of the body twist axis above the plane of the frame

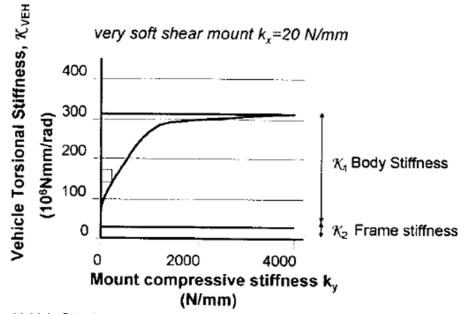
w: width between body mounts

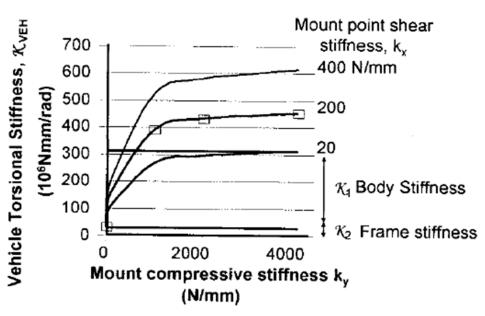
 ψ : body-frame coupling term which indicates how tightly coupled are the twisting actions of the frame and body (larger ψ , greater coupling)

Effect of Body Mount (1)

- Compressive stiffness (k_v)
 - Soft mount: body is not coupled to the twisting motion of the frame $(K_{VEH} \rightarrow K_2)$
 - Stiff mount: body and frame are highly coupled $(K_{VEH} \rightarrow K_1 + K_2)$
- Shear stiffness (k_x)

$$- k_x \uparrow \rightarrow K_{VFH} > K_1 + K_2 : why?$$

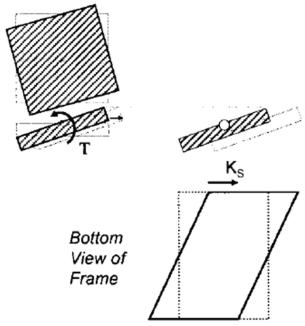




Vehicle Structure

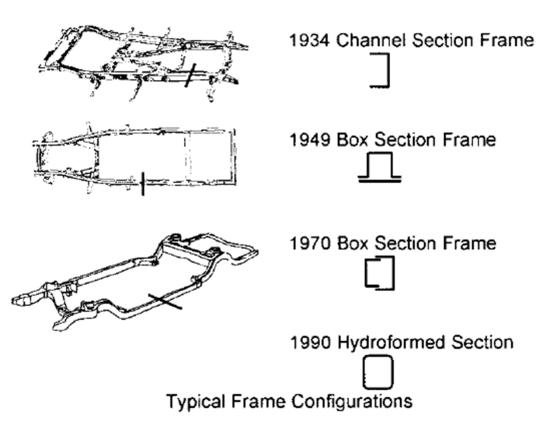
Effect of Body Mount (2)

- Body and frame have different twist axes
 - Body and frame fight against one another for the axis to twist about by increasing the mount shear stiffness
- Combined twist axis locates above the frame
 - Frame becomes a shear resistant member
 - Shear stiffness of the frame: important design consideration



Evolution of Automobile Frame

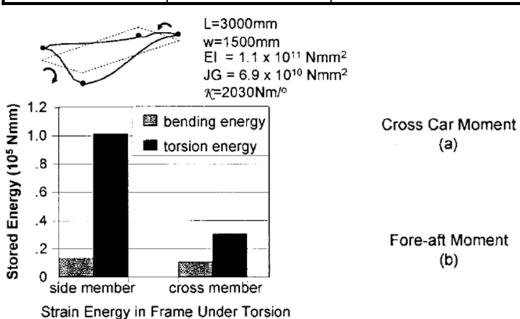
- Closed sections for both side rails and cross member
 - Improve torsional stiffness
- Improved joints at cross member to side rail
 - Improve both torsional and shear stiffness

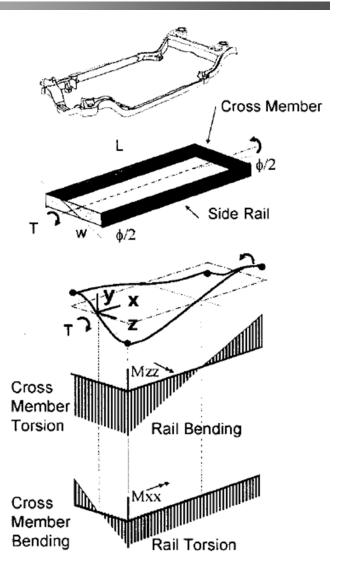


Ladder Frame

- Two limiting cases for simple frame
 - Cross member

Torsion	Bending	Torsional Stiffness
infinitely rigid	very flexible	$K = 6w^2 EI/L^3$
very flexible	infinitely rigid	$K = 2(GJ_{eff}/L)$



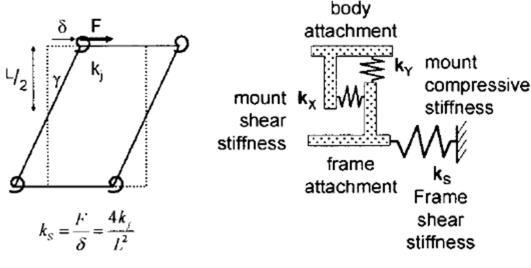


Frame: General Case

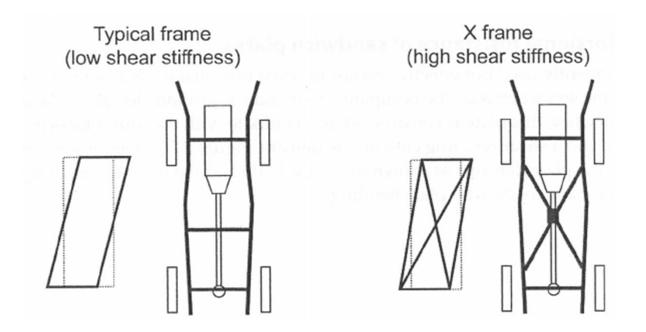
Frame Shear Stiffness

$$\frac{1}{2}F\delta = 4\left(\frac{1}{2}k_J\theta^2\right) \xrightarrow{\theta = \frac{\delta}{L}} k_S = \frac{F}{\delta} = \frac{4k_J}{L^2}$$
work done energy stored in the joints

- k_J = 1x10⁹Nmm/rad, L = 4500mm, k_S ≈ 200N/mm
- Very near the shear stiffness for a body mount
- Increase the frame shear stiffness
 - increase the joint rate with gusset, X configuration of rails



Shear Stiffness of Frame



Backbone Frame

- Large central closed section
 - Open two seat sport cars
- Large width to thickness ratio: elastic shear buckling of walls
 - Diagonal rib patterns on the backbone sides

