

Submit the compressed file as (ID)_(name).zip to [[ftp://cdl.hanyang.ac.kr](http://cdl.hanyang.ac.kr) → CAE/Final_Lab] folder. It should contain the final results of each problem (equations and graphs) using PowerPoint (ID.ppt) and COMSOL files (problem#-#.mph).

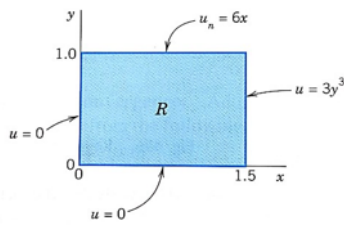
1. [PDE solving] Solve the mixed boundary value problem for a Poisson equation as follows. Plot the surface of solution 'u' and compute the solution values at the four points. (15 pts)

Mixed Boundary Value Problem for a Poisson Equation

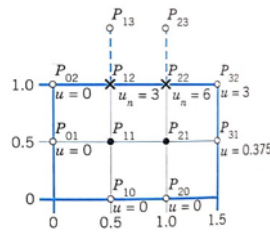
Solve the mixed boundary value problem for the Poisson equation

$$\nabla^2 u = u_{xx} + u_{yy} = f(x, y) = 12xy$$

shown in Fig. 457a.



(a) Region R and boundary values



(b) Grid ($h = 0.5$)

Fig. 457. Mixed boundary value problem in Example 1

$$u_{xx} + u_{yy} = f(x, y) = 12xy$$

Dirichlet B.C

$$u(0, y) = u(y, 0) = 0, u(1.5, y) = 3y^3$$

Neumann B.C

$$u_y(x, 1) = 6x$$

Exact sol.

$$u_{11} = 0.125, u_{12} = 1$$

$$u_{21} = 0.250, u_{22} = 2$$

Flux/Source 1

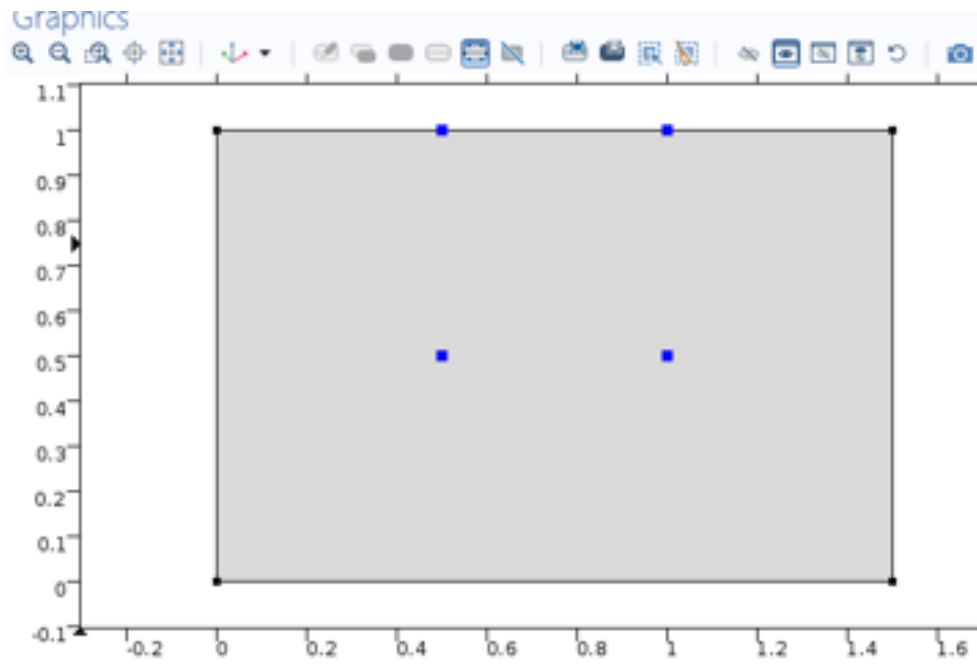
Equation

Show equation assuming:

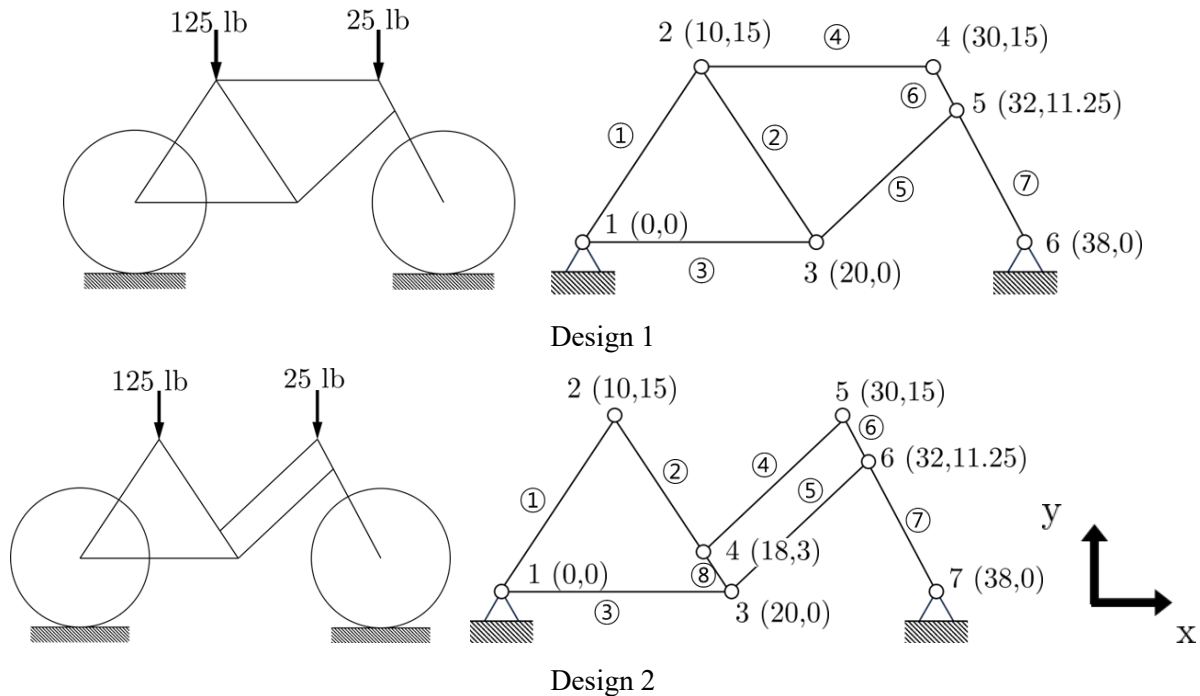
Study 1, Stationary

$$-\mathbf{n} \cdot (-c \nabla u - \alpha u + \gamma) = g - qu$$

$$\nabla = \left[\frac{\partial}{\partial x}, \frac{\partial}{\partial y} \right]$$



2. [2D Beam] Consider the following two bicycle frame models. Answer the following questions based on your analysis of these models:



[Material property]

Design 1

$$E = 30 \times 10^6 \text{ psi}$$

Design 2

$$E = 10 \times 10^6 \text{ psi}$$

[Crosssection data]

$$A_1 = 0.1 \text{ [in}^2\text{]}$$

$$A_2 = A_3 = A_4 = A_5 = 0.15 \text{ [in}^2\text{]}$$

$$A_6 = A_7 = A_8 = 0.3 \text{ [in}^2\text{]}$$

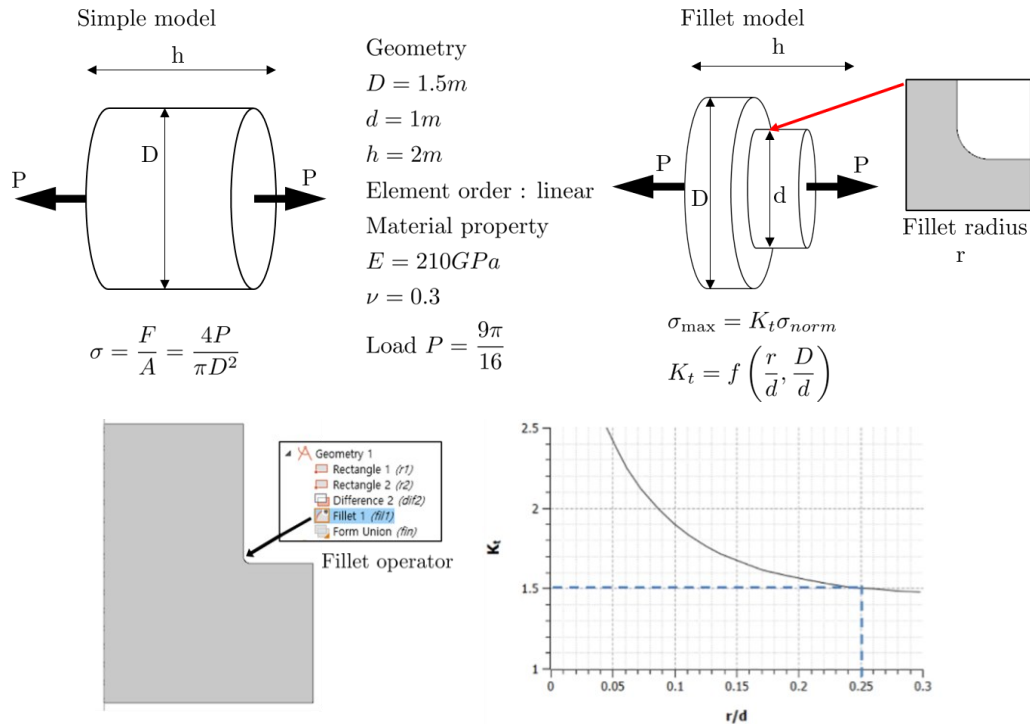
$$I_1 = 0.01 \text{ [in}^4\text{]}$$

$$I_2 = I_3 = I_4 = I_5 = 0.02 \text{ [in}^4\text{]}$$

$$I_6 = I_7 = I_8 = 0.1 \text{ [in}^4\text{]}$$

- 1) Plot the Total displacement for each model and evaluate the y-direction displacements at the node at 2. (15 pts)
- 2) Plot the von-mises stress (line type) for two bicycle frame models and determine which design is preferable based on structural stiffness, providing an explanation for your choice (10 pts)

3. [Stress concentration] The following cylinder bar with fillet (30 pts total)



- (1) Construct the full 3D model and plot the surface of the first principal stress and the Calculate norm stress (10 pts)

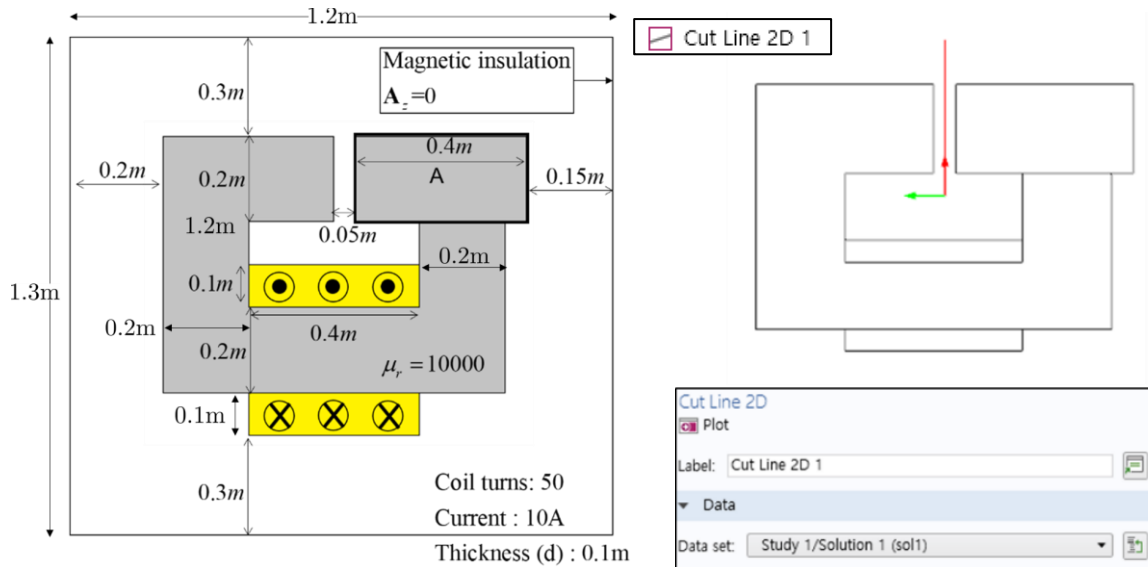
(hint: use Domain Probe 1 (dom1) average value of first principal stress "solid.sp1")




- (2) Construct the 2d axisymmetric fillet ($r=0.25$) model, Compute maximum value of the first principal stress. Check the stress by mesh dependency applying free triangle. Plot the graph as d.o.fs vs stress changing mesh size. (mesh option: extremely coarse ~ extremely fine) (10 pts)
- (3) Calculate the value of K when changing the fillet radius (0.05 ~ 0.25 m) as shown in the table. Compare the values of K between the analytic and COMSOL results and fill the table. (mesh option: normal) (10 pts)

R(m)	Analytic Kt	FEM Kt
0.05	2.4	
0.1	1.9	
0.15	1.68	
0.2	1.57	
0.25	1.5	

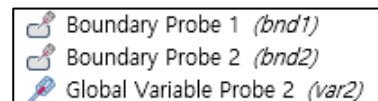
4. [Magnetic Actuator] For the actuator and boundary conditions shown, solve the Poisson equation by

 **Magnetic Fields (mf)** . (Use **Fine** discretization level.) (30 pts total)



1) Draw a Magnetic flux density norm distribution along the  **Cut Line 2D 1** by  **1D Plot Group**  **Line Graph** (15 pts total)

2) Evaluate the magnetic force using Maxwell stress tensor method by (15 pts total) Analytic solution : 1.4289 N



Hint:

Magnetic force (Maxwell Stress Tensor Method)

$$f_x = \frac{d}{\mu_0} \left[\int \frac{B_x B_x}{2} dy + \int B_x B_y dx \right]$$

d : thickness

μ_0 : vacuum permeability

B : flux density

f : force