

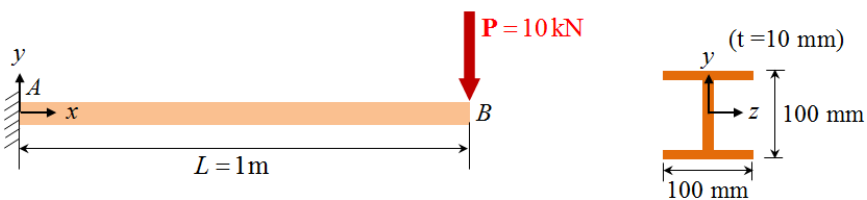
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[analysis\_result\_file] (학번)\_(문제번호)\_(요소종류) ex) 2000100100\_1\_beam

[report\_file] (학번) upload only one file for all problems.

[1-2] For the alloy steel beam and boundary condition shown, verify the following equations. Use 1-D beam element.

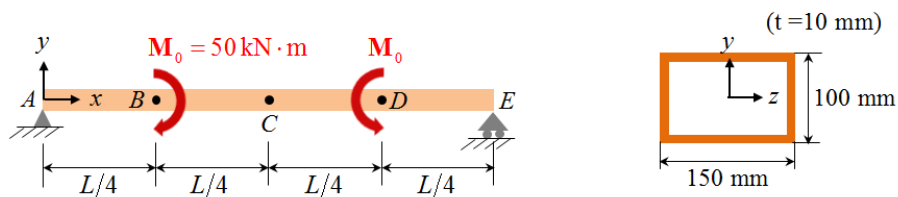
1. Cantilever beam (15 pts)



(a) the slope at the free end :  $\phi_B = \frac{PL^2}{2EI}$

(b) the deflection at the free end :  $d_B = \frac{PL^3}{3EI}$

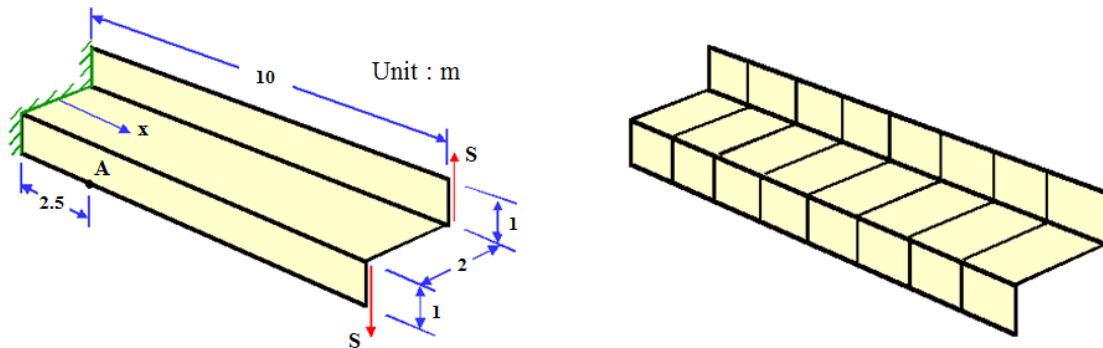
2. Simply supported beam (15 pts)



(a) the slope at end A :  $\phi_A = \frac{M_0 L}{4EI}$

(b) the deflection at the center C :  $d_C = \frac{3M_0 L^2}{32EI}$

3. A z-angle beam under torsional load is illustrated in the figure below. By using the presented boundary conditions and the element shape, find the axial (x-x) stress at the mid-surface of point A. (35 pts)



Material properties	$E = 210 \text{ GPa}$ , $\nu = 0.3$
Element type	24 shell element (thickness: 0.1 m)
Loading condition	Torque of 1.2 MNm applied at end $x=10$ by uniformly distributed edge shears, $S=0.6 \text{ MN}$ at each flange
Support conditions	Fixed conditions at edge $x=0$
Target value	-108 MPa (compression)

4. Each of the two struts consists of an alloy steel tube that has a 150-mm outer diameter and a 10-mm wall thickness. Determine the critical buckling load ( $P_{cr}$ ) for each support condition shown ( $L=1\text{m}$ ), and compare the results between 1-D and 3-D (solid) element. (35 pts)

$$\text{Analytic solution : } P_{cr} = \frac{\pi^2 EI}{L_{eff}^2}$$

