

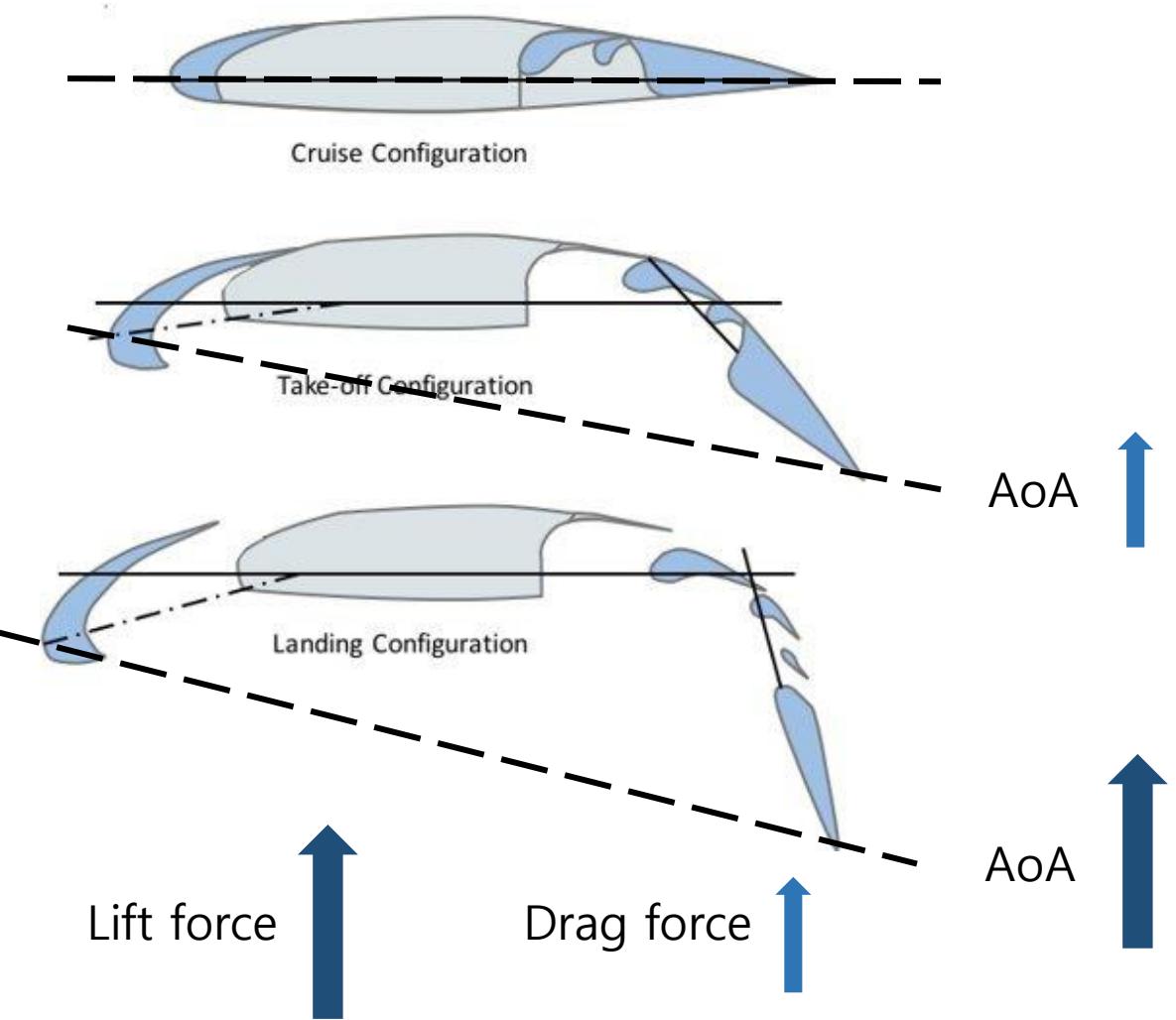
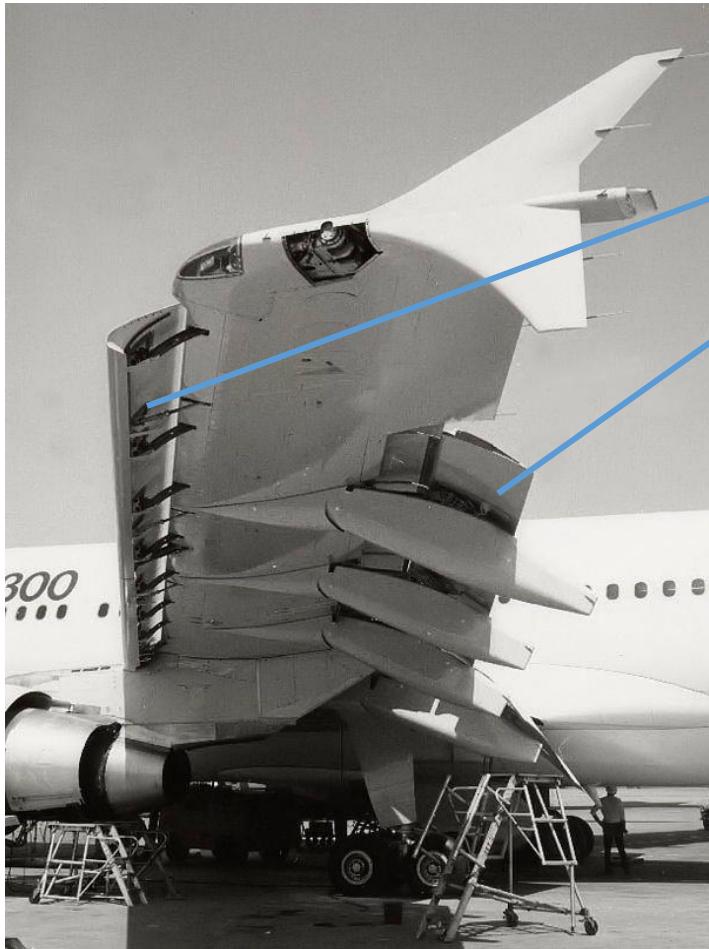
Slat & Flap 작동에 따른

Boeing 737-500 이륙 상황 분석

2018016044 여준성
2021081121 송기원

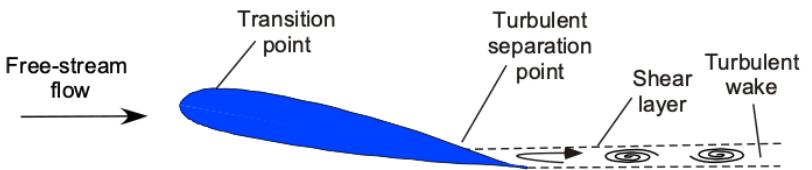
주제 소개

Slat & Flap

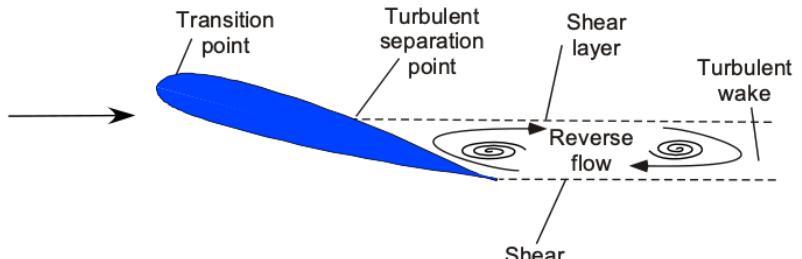


Stall

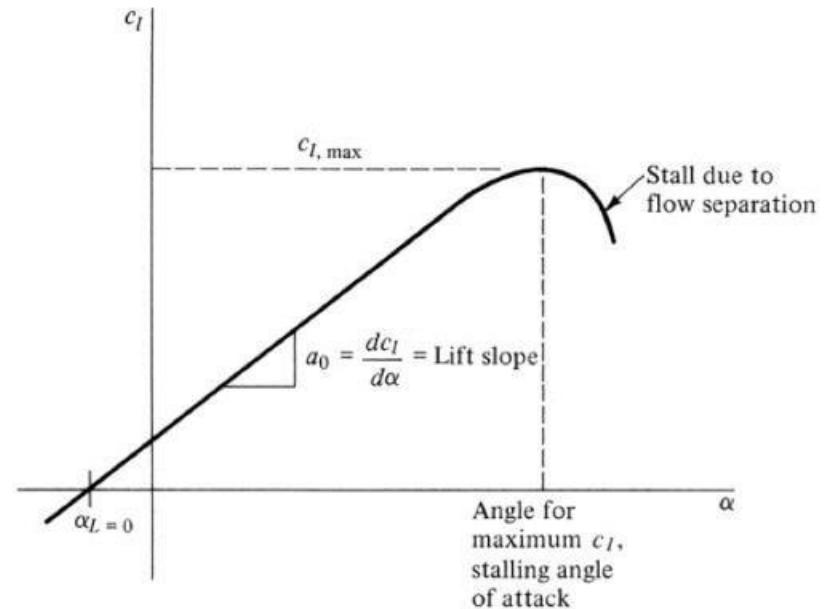
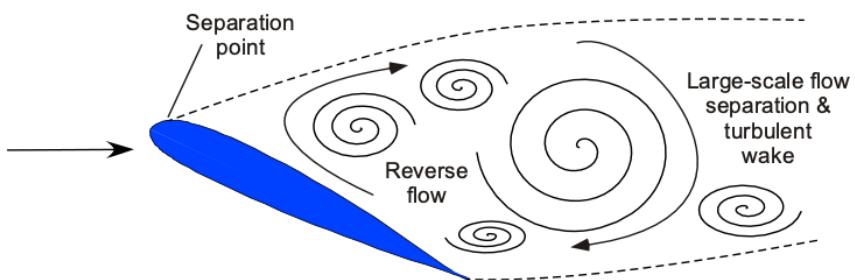
(a) Lower angle of attack



(b) Higher angle of attack

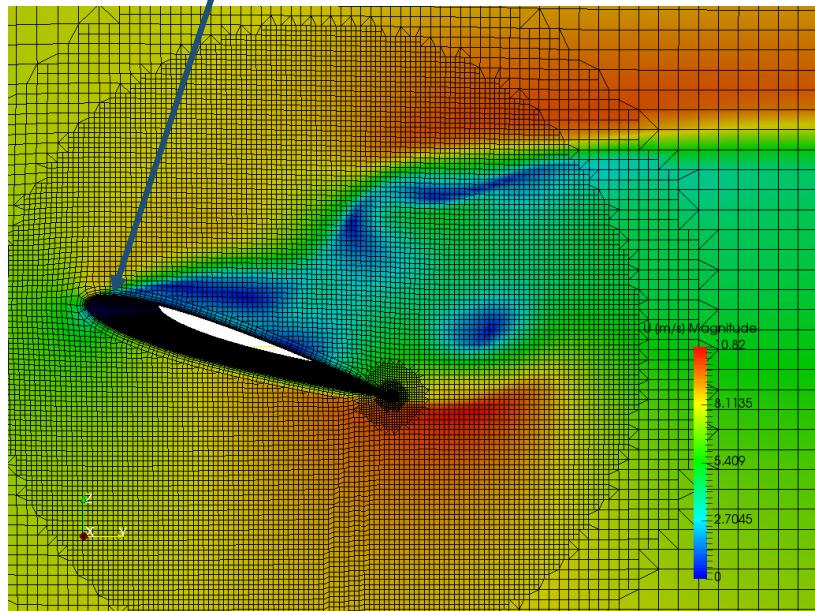


(c) Stalled flow conditions

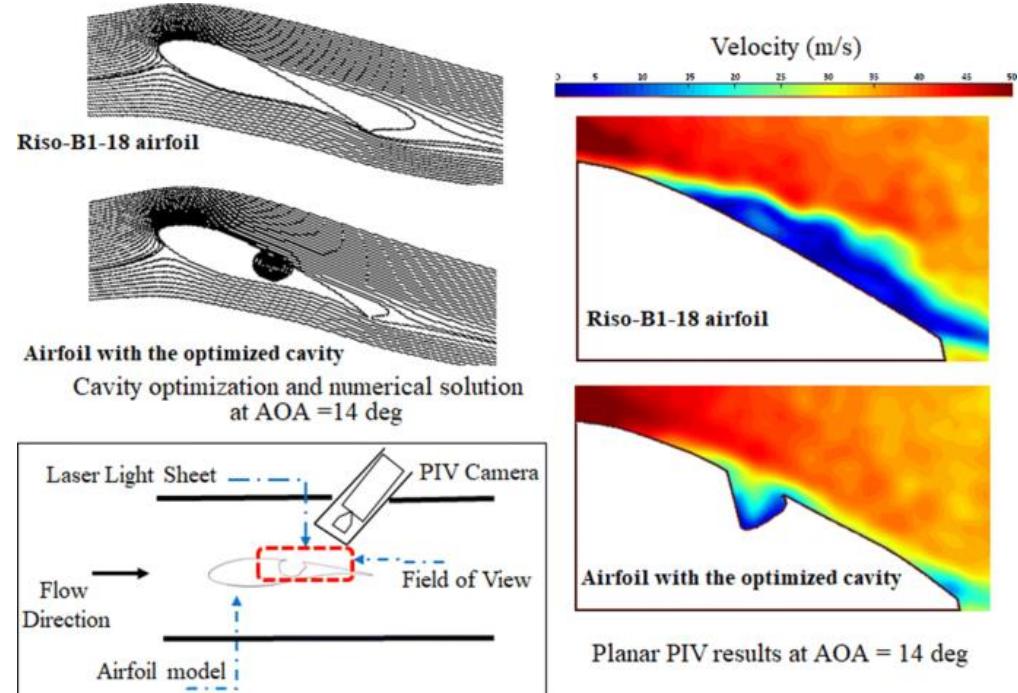


Stall

Solution : Separation point를 최대한 뒤로 이동시킨다.



1.



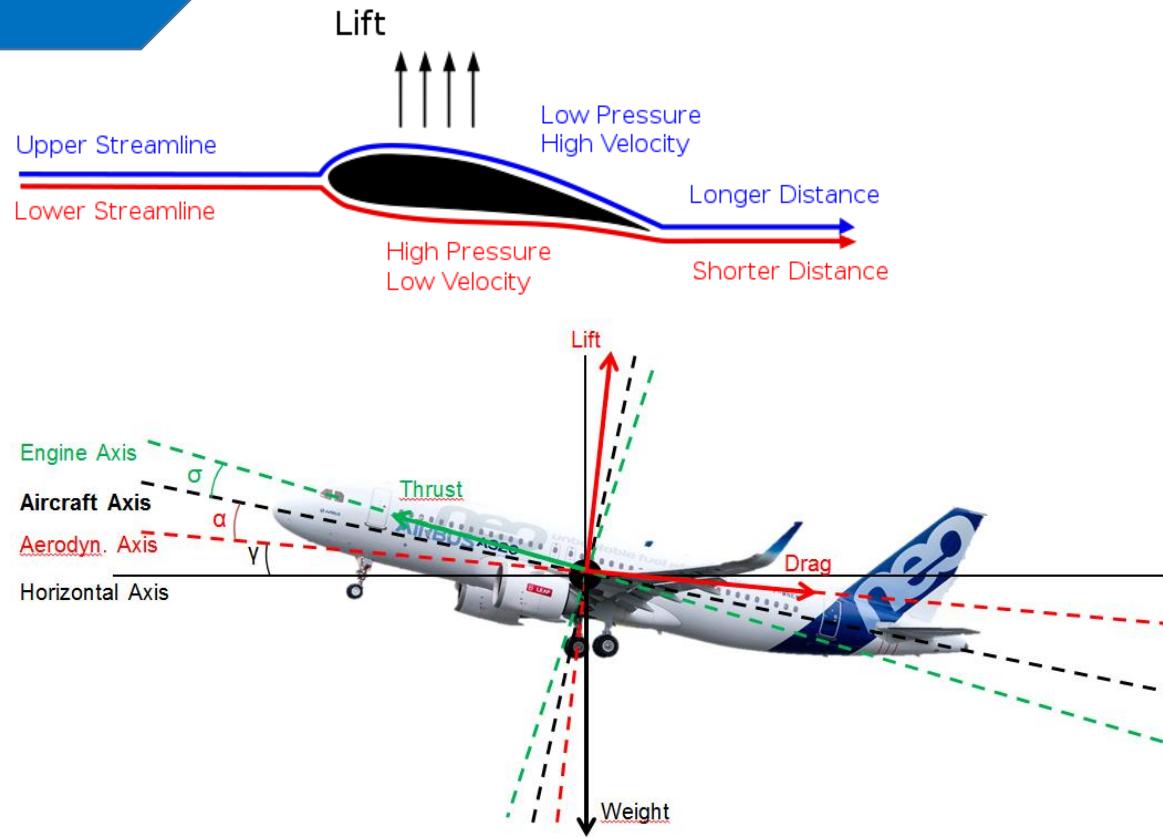
2.



Lift & Drag

$$F_{Lift} = \frac{1}{2} \cdot C_L \cdot \rho \cdot A \cdot v^2$$

$$F_{Drag} = \frac{1}{2} \cdot C_D \cdot \rho \cdot A \cdot v^2$$



For convenience, we will use $\frac{1}{2} \cdot C_L \cdot \rho \cdot A$ instead of C_L to calculate force versus velocity

Also, we will neglect Aerodynamic Axis \gg No nose up or down situation

Airfoil – Boeing 737



Airfoil Tools

Search 1638 airfoils G+ X Post 좋아요 1.5천개

You have 0 airfoils loaded.
Your Reynold number range is 50,000 to 1,000,000. ([Edit](#))

ENHANCED BY Google Search

Applications

- Airfoil database search
- My airfoils
- Airfoil plotter
- Airfoil comparison
- Reynolds number calc
- NACA 4 digit generator
- NACA 5 digit generator

Information

- Airfoil data
- Lift/drag polars
- Generated airfoil shapes

Searches

- Symmetrical airfoils
- NACA 4 digit airfoils
- NACA 5 digit airfoils
- NACA 6 series airfoils

Airfoils A to Z

- A a18 to avistar (88)
- B b29root to bw3 (22)
- C c141a to curtisc72 (40)
- D dae11 to du861372 (28)
- E e1098 to esa40 (209)
- F falcon to fxs21158 (121)
- G gemini to gu255118 (419)
- H hh02 to ht23 (63)
- I isa571 to isa962 (4)
- J j5012 to joukowsk0021 (7)
- K k1 to kenmar (11)
- L l1003 to lwk80150k25 (24)
- M m1 to mue139 (95)
- N n0009sm to nplx (174)

BOEING 737 ROOT AIRFOIL (b737a-il)

BOEING 737 ROOT AIRFOIL - Boeing Commercial Airplane Company model 737 airfoils

Details

(b737a-il) BOEING 737 ROOT AIRFOIL
Boeing Commercial Airplane Company model 737 airfoils
Max thickness 15.4% at 19.6% chord.
Max camber 0.2% at 5% chord
[Source UIUC Airfoil Coordinates Database](#)
[Source dat file](#)
The dat file is in Lednicer format

Dat file

```
BOEING 737 ROOT AIRFOIL
23.      23.
0.000000  0.017700
0.002300  0.030900
0.005000  0.037200
```

Parser

No parser warnings

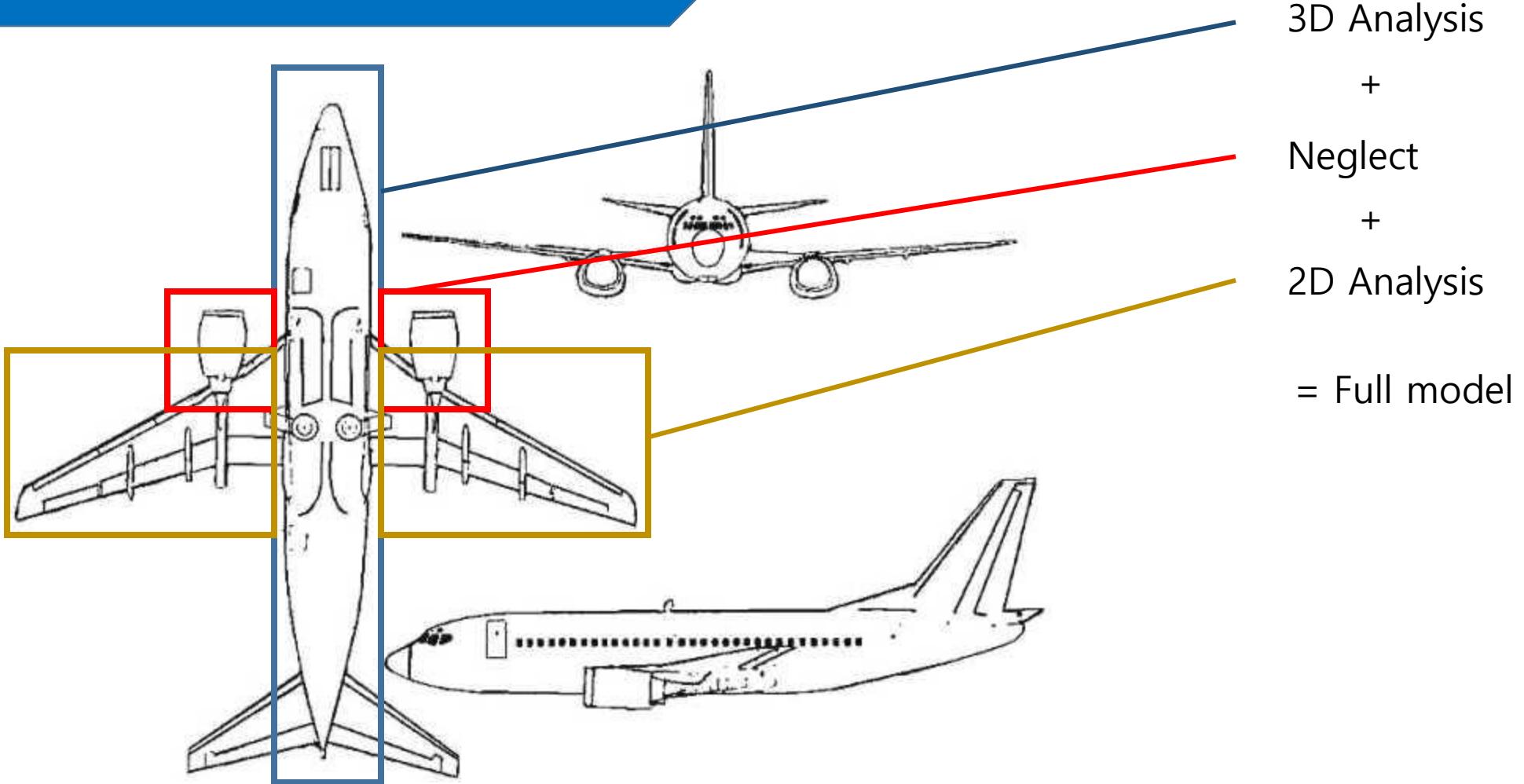
[Send to airfoil plotter](#)
[Add to comparison](#)
[Lednicer format dat file](#)
[Selig format dat file](#)

Data – Boeing 737

Powerplant:	JT8D	JT8D	CFM56-3	CFM56-3	CFM56-3
Model	JT8D	JT8D	CFM56-3	CFM56-3	CFM56-3
Type	-7	-15A	-B2	C-1	-B1
Static Thrust (kN)	64.4	71.2	88.9	104.5	82.3
Static Thrust (Lb)	14,000	16,000	20,000	23,500	18,500
Bypass Ratio	1.1	0.99	5.0	4.9	5.0
EGT Margin (C)			50	45	90
Fan tip diameter (in)	54	54	60	60	60
Max Nacelle Width (m)	1.50	1.50	2.00	2.00	2.00

Wing:					
Span (m)	28.35	28.35	28.88	28.88	28.88
Gross Area (m ²)	102.0	102.0	105.4	105.4	105.4
Aspect Ratio	8.83	8.83	9.16	9.16	9.16
Taper Ratio	0.266	0.266	0.240	0.240	0.240
Root Chord (m)	7.32	7.32	7.32	7.32	7.32
Tip Chord (m)	1.60	1.60	1.62	1.62	1.62
M.A.C.(m)	3.80	3.80	3.41	3.41	3.41
Dihedral (°)	6	6	6	6	6
¼ Chord Sweep (°)	25.00	25.00	25.00	25.00	25.00
Wing High Lift Devices:					
Flap Span/Wing Span	0.740	0.740	0.720	0.720	0.720
Flap Area/Wing Area	0.290	0.290	0.290	0.290	0.290

Full model

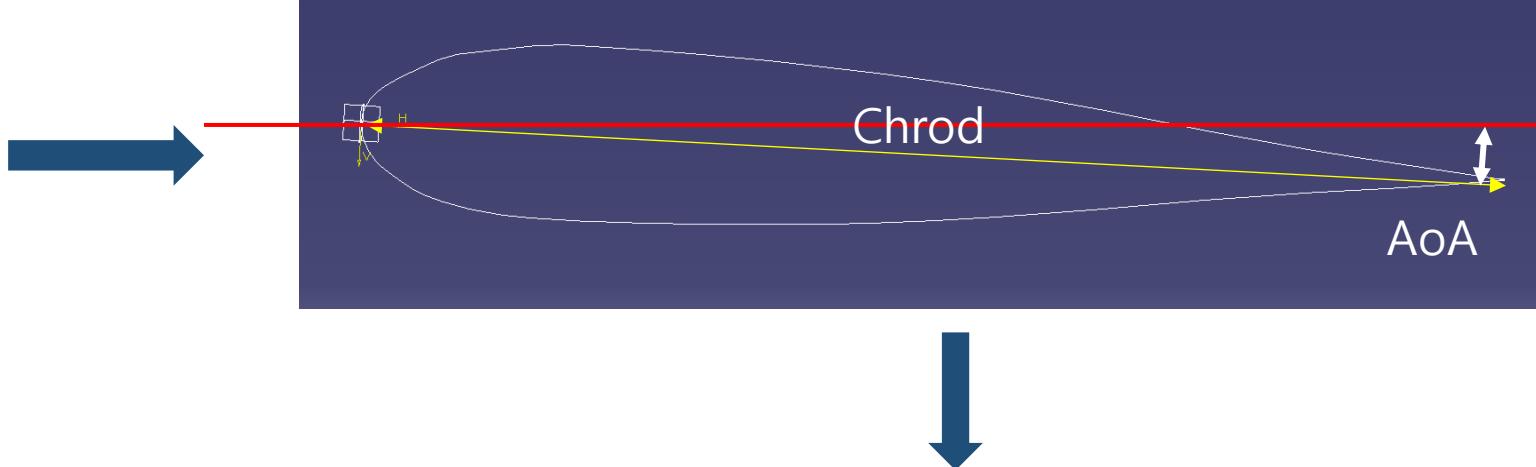


Wing Analysis - Comsol

AoA 6deg 2D CFD

AoA 6deg 2D Model

A	B	C	D
1 StartLoft			
2 StartCurve			
3 0	0.0177	0	
4 0.0023	0.0309	0	
5 0.005	0.0372	0	
6 0.0076	0.0415	0	
7 0.0143	0.0499	0	
8 0.0249	0.0582	0	
9 0.0495	0.073	0	
10 0.074	0.0814	0	
11 0.099	0.0886	0	
12 0.153	0.0907	0	
13 0.1961	0.0905	0	
14 0.2504	0.0887	0	
15 0.3094	0.0858	0	
16 0.352	0.0833	0	
17 0.3919	0.0804	0	
18 0.4477	0.0756	0	
19 0.5034	0.0696	0	
20 0.5593	0.0626	0	
21 0.5965	0.0575	0	
22 0.6488	0.0498	0	
23 0.8351	0.0224	0	
24 0.9109	0.0132	0	
25 1	0.0003	0	
26 EndCurve		0	
27 EndLoft			
28 0	0.0177	0	
29 0.0022	0.0038	0	
30 0.0049	-0.0018	0	
31 0.0072	-0.0053	0	
32 0.0119	-0.0106	0	
33 0.0243	-0.0204	0	
34 0.0486	-0.0342	0	
35 0.0716	-0.0457	0	
36 0.0979	-0.0516	0	
37 0.1488	-0.0807	0	
38 0.1953	-0.0832	0	
39 0.2501	-0.0832	0	
40 0.2945	-0.0826	0	
41 0.3579	-0.061	0	
42 0.3965	-0.0595	0	
43 0.4543	-0.0563	0	
44 0.505	-0.0527	0	
45 0.5556	-0.0482	0	
46 0.6063	-0.0427	0	
47 0.6485	-0.0375	0	
48 0.8317	-0.0149	0	
49 0.941	-0.0053	0	
50 1	-0.0003	0	
51 EndCurve			
52 EndLoft			
53 End			
54			
55			
56			



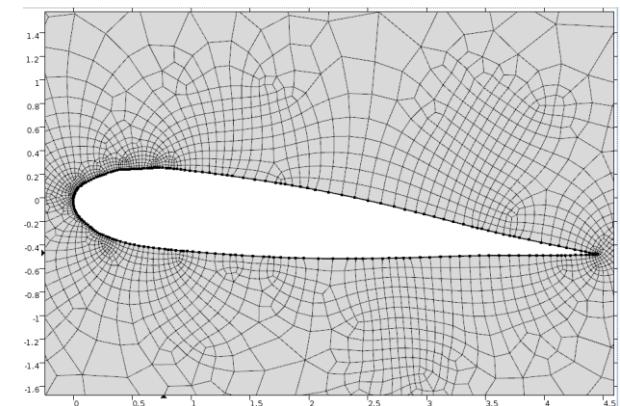
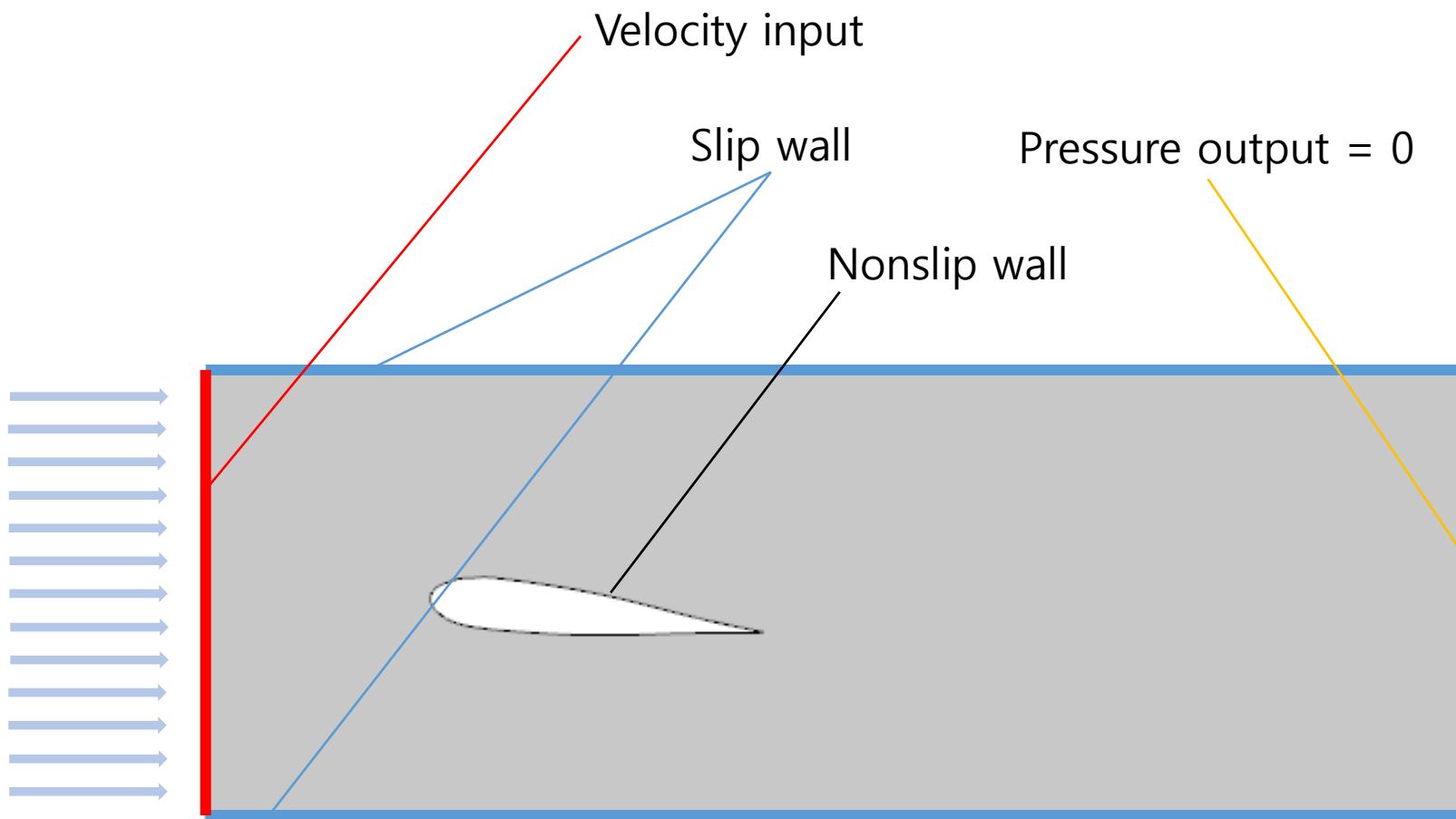
Root Chord (m)	7.32	7.32	7.32	7.32	7.32
Tip Chord (m)	1.60	1.60	1.62	1.62	1.62

$$\frac{(7.32 + 1.62)}{2} = 4.47 \text{ m : Chord Length}$$

Dihedral (°)	6	6	6	6	6
--------------	---	---	---	---	---

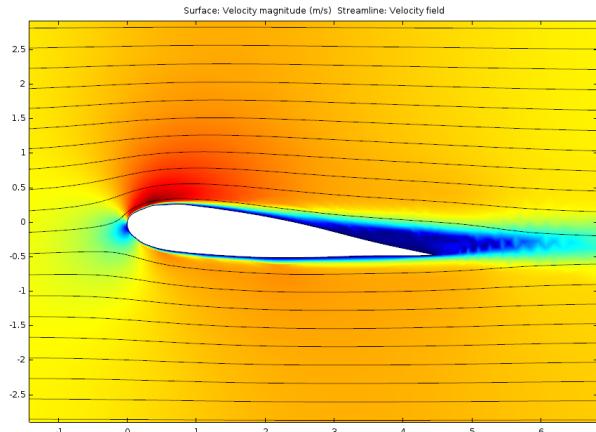
6 ° : Attack of Angle

AoA 6deg 2D Model

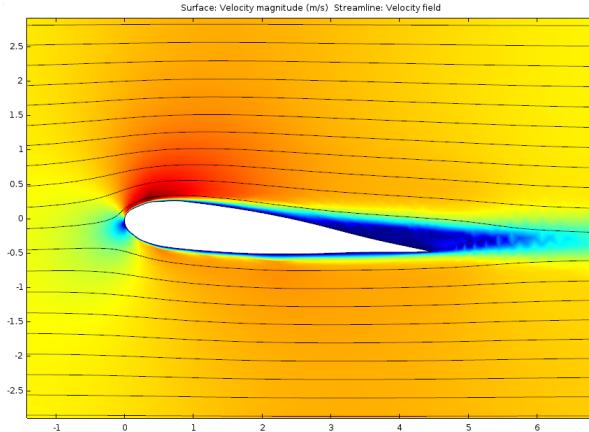


Altitude = Sea level
Temperature = 293.15 K
Air density(ρ) = 1.22 kg/m³

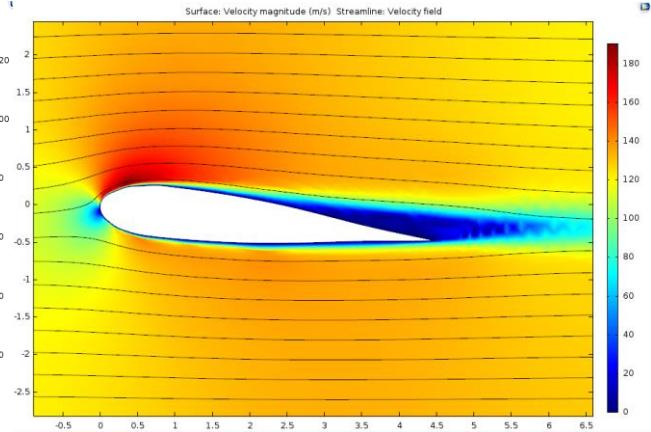
AoA 6deg 2D CFD



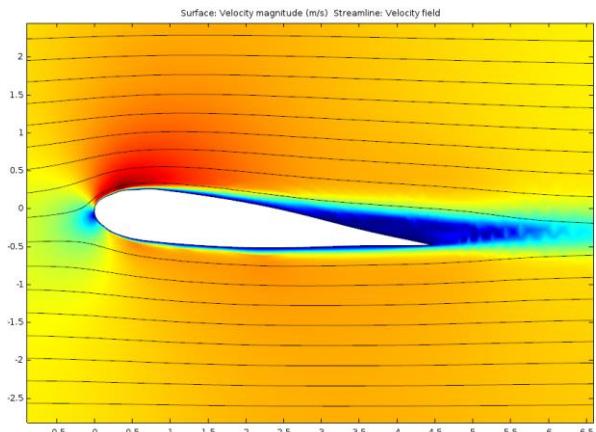
40m/s



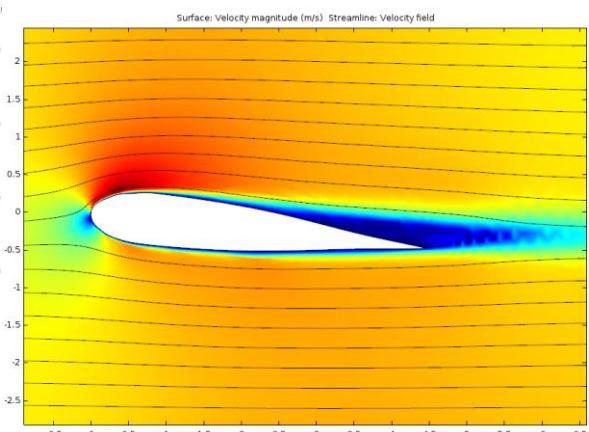
80m/s



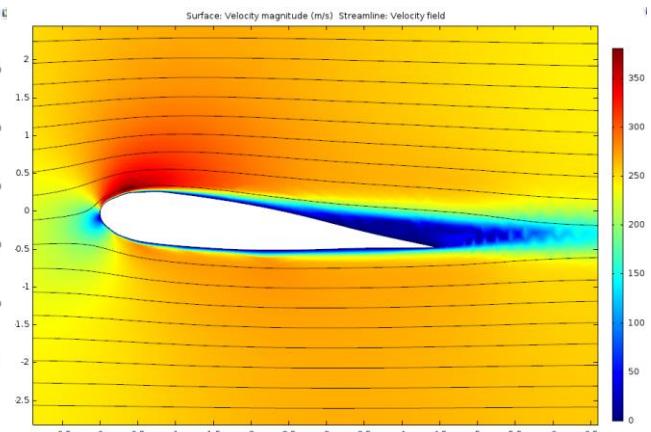
120m/s



160m/s

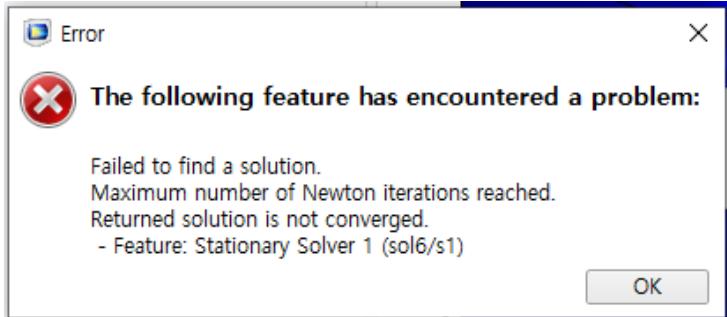


200m/s



240m/s

Stationary vs Time Dependent



September 19, 2005, 01:50 Re: What are the reasons for solution instability?

Mani Guest Posts: n/a

You may have to define your problem a little clearer. There will not be any simple and general answer to the question why numerical solutions blow up, because of a quite complex interaction of possible causes, such as numerical instability of the main algorithm, ill-posedness of the physical/numerical problem, instability of the boundary conditions (maybe related to ill-posedness), unresolved physical instability... and so on. I think that you are focusing on the stability of your numerical algorithm, but I wasn't quite clear from your post. Stability analysis is not a new field, you are surely familiar with the linear Von-Neumann analysis, for example. If you're interested in nonlinear stability analysis, I am not sure there is a lot you can do for the general case, but I would say that the stability issues you mentioned in your post are understood within the framework of linear stability. In order to get feedback on your new idea, you probably need to be more specific.

September 19, 2005, 04:19 Re: What are the reasons for solution instability?

diaw Guest Posts: n/a

Thanks Mani... always a good comment... 😊

Try this little experiment:

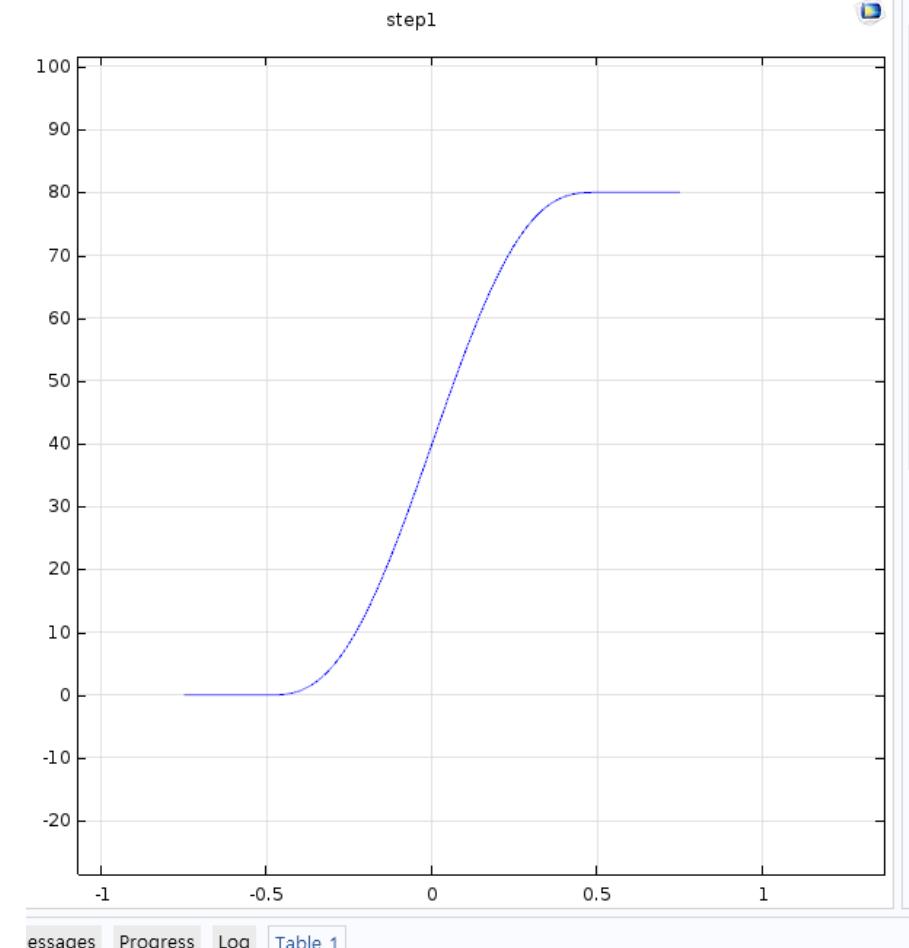
1. Create rectangular domain - $dx=4$; $dy=1$.
2. Discretise into coarse structured elements - say 0.5×0.5 .
3. Set upper & lower faces to $u,v=0$.
4. Apply input velocity at central node on left edge (the inlet).
5. Without using flow-field stabilisation, begin with velocity $u=1$ m/s & gradually raise the velocity until a reasonable Reynolds is reached.
6. Fluid properties: density = 1, viscosity = 1.

Observe the total-velocity & pressure fringe plots & tell what you see. At what velocity does the solution blow up - !!!without flow stabilisation!!!

Interesting results on my end in FEM... at low Reynolds numbers...

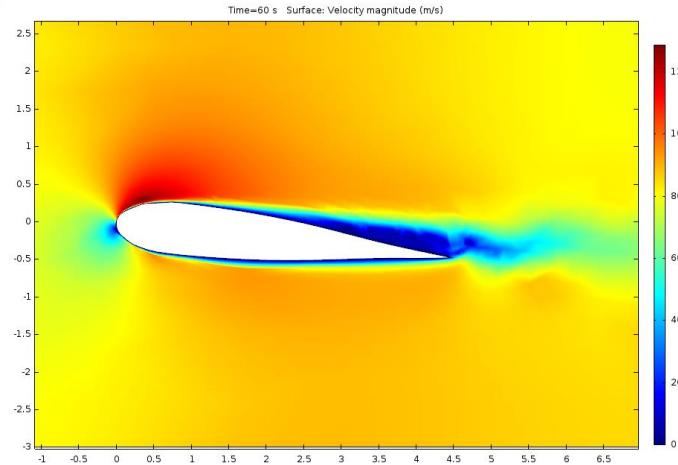
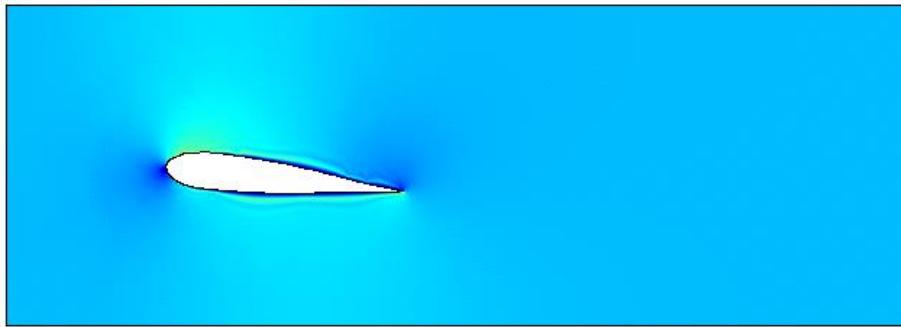
This experiment was constructed in order to challenge a new 'singularity theory' I have been dabbling with on the sidelines for a few months... I can show the mathematical reasoning rather clearly.

diaw...



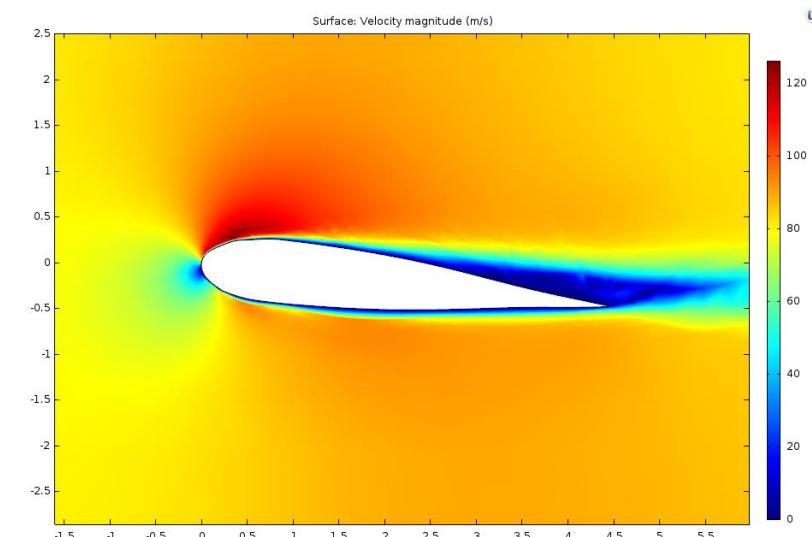
Stationary vs Time Dependent

Step function * 80 m/s



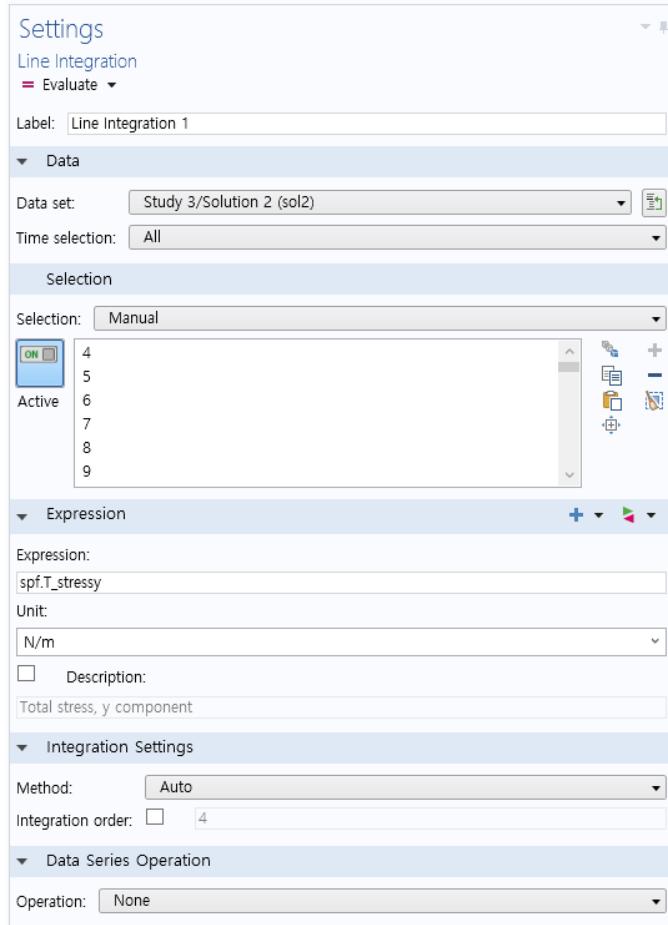
VS

Stationary 80 m/s



Average of reasonable data \approx Stationary result

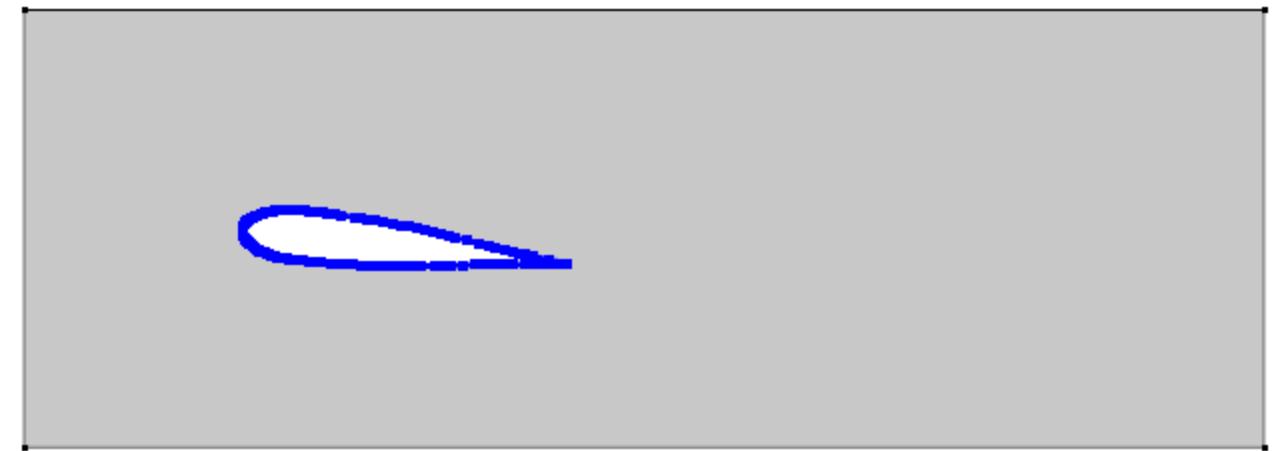
Calculating Lift & Drag Force



Momentum Equations

$$\rho \frac{D\vec{V}}{Dt} = -\nabla p + \rho \vec{g} + \mu \nabla^2 \vec{V}$$

↑ Total derivative ↑ Pressure gradient ↗ Body force term ↗ Diffusion term



Lift force per unit length Drag force per unit length

Total stress, y component (N/m)	Total stress, x component (N/m)
-5748.0	-725.65

→ Why minus?

: This calculates reaction force from airfoil boundary

AoA 6deg Lift & Drag

Velocity (m/s)	Lift force (N/m)	Drag force(N/m)
40	1066	183.6
80	5748	725.65
120	9598.2	1651.2
160	17064	2935
200	26669	4585.8
240	38388.7	6603.9



L*wing span	D*wing span	L/v^2	D/v^2
26650	4590	0.66625	0.11475
143700	18141.25	0.898125	0.113383
239955	41280	0.666542	0.114667
426600	73375	0.666563	0.114648
666725	114645	0.666725	0.114645
959717.5	165097.5	0.66647	0.114651

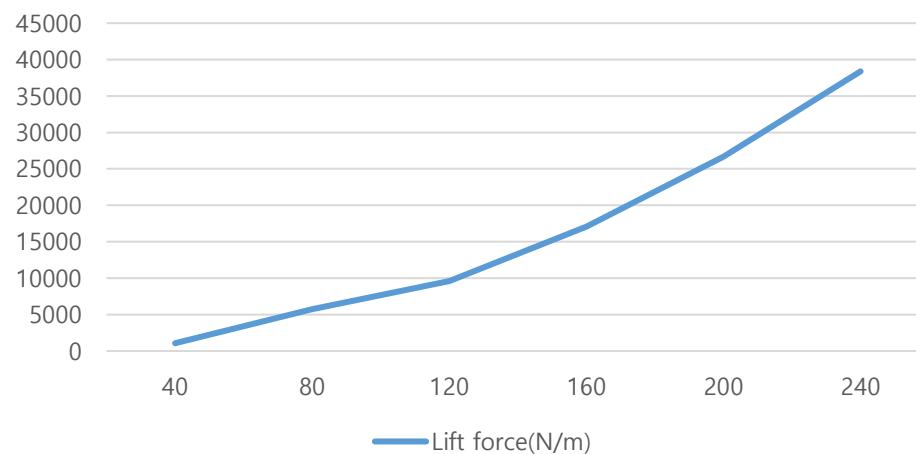


$$\frac{1}{2} \cdot C_L \cdot \rho \cdot A = 0.705 / \text{span}$$

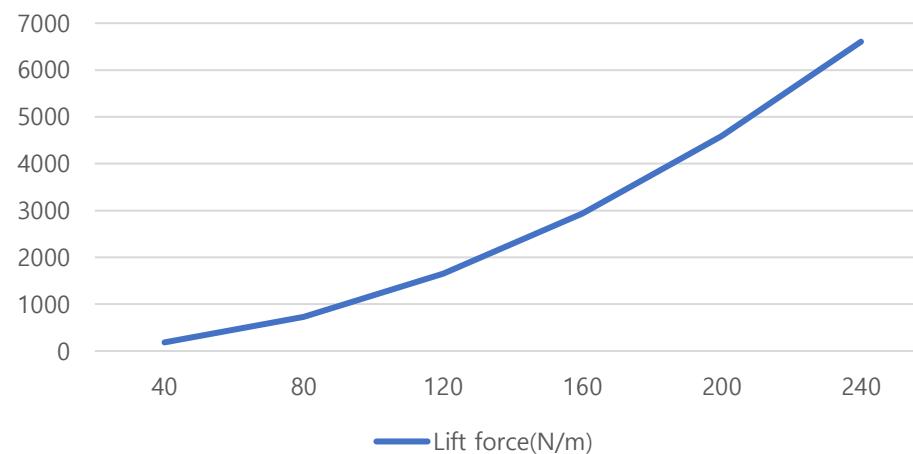
$$\frac{1}{2} \cdot C_D \cdot \rho \cdot A = 0.114 / \text{span}$$

$$C_L/C_D = 6.184$$

Lift force(N/m)

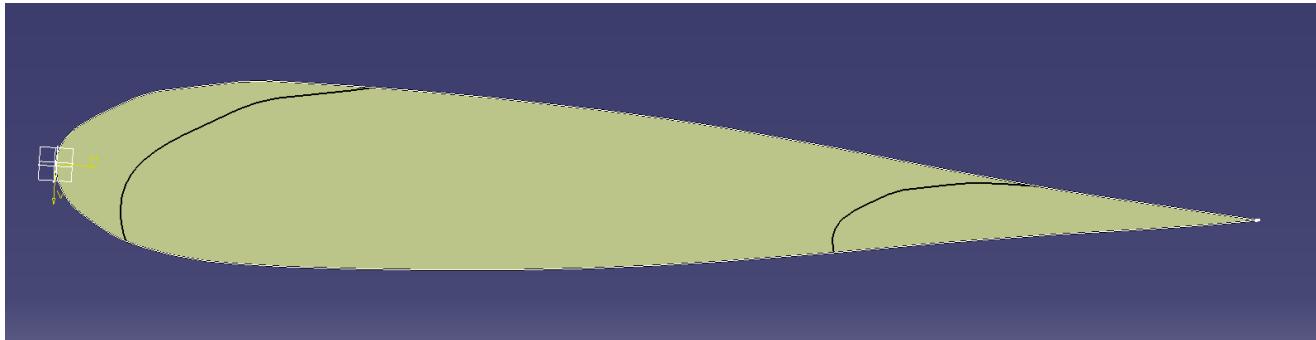


Drag force(N/m)

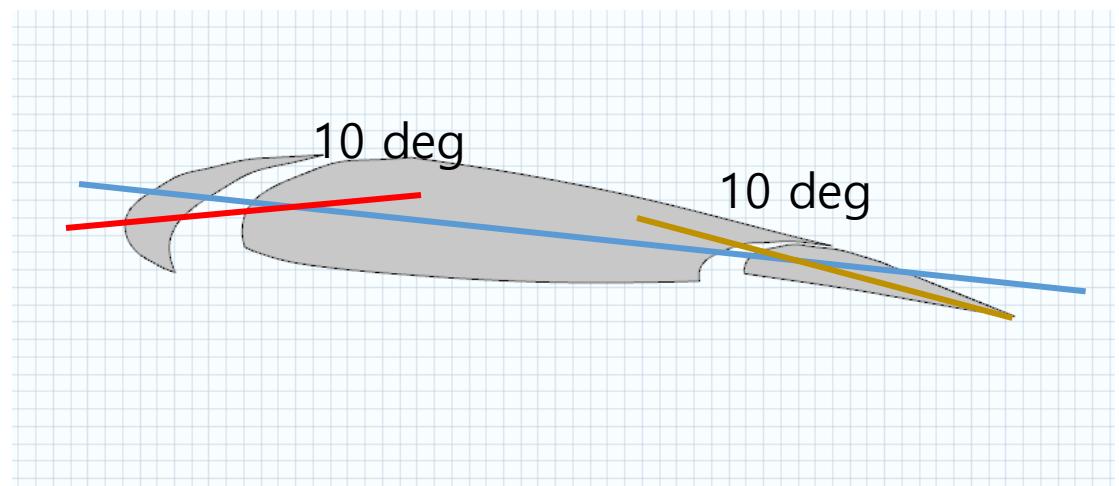


Slat & Flap 2D CFD

Slat & Flap 2D Model

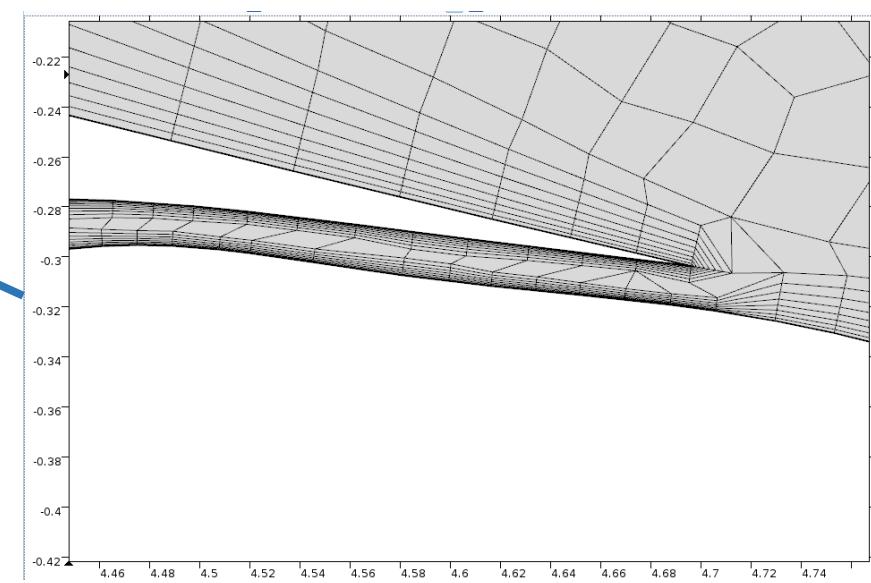
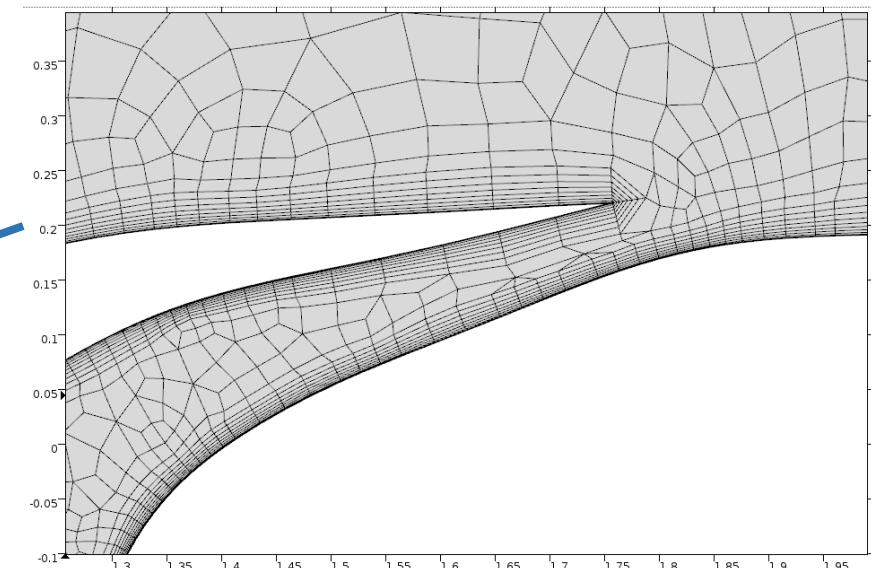
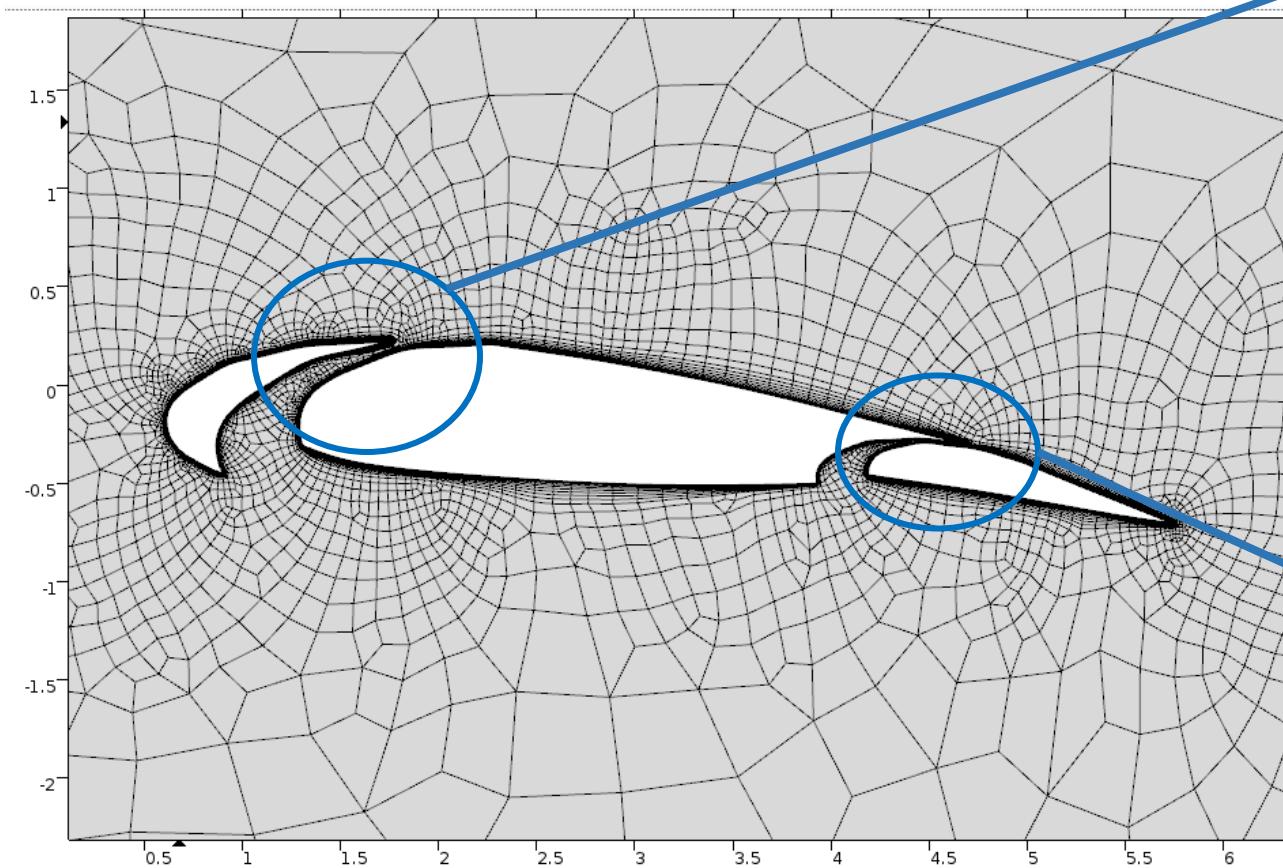


- ▲ Geometry 1
 - ☛ Import 1 (imp1)
 - ☛ Import 2 (imp2)
 - ☛ Import 3 (imp3)
 - ☛ Scale 1 (sca1)
 - ☛ Rotate 1 (rot1)
 - ☛ Rotate 2 (rot2)
 - ☛ Rotate 3 (rot3)
 - ☛ Move 1 (mov1)
 - ☛ Move 2 (mov2)
 - ☛ Move 3 (mov3)
 - ☛ Rectangle 1 (r1)
 - ☛ Difference 1 (dif1)
 - ☛ Move 4 (mov4)
 - ☛ Form Union (fin)



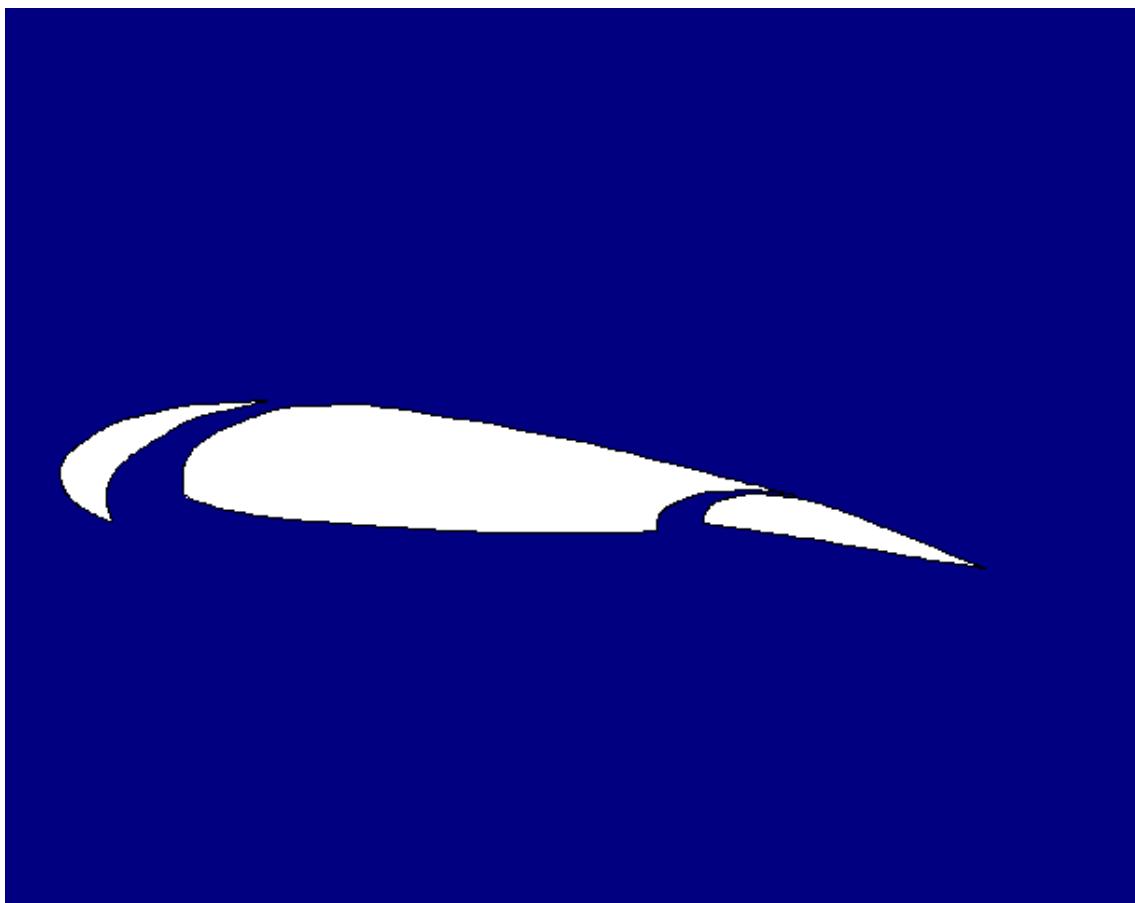
Slat & Flap 2D Mesh

Boundary Layer for Mesh Quality

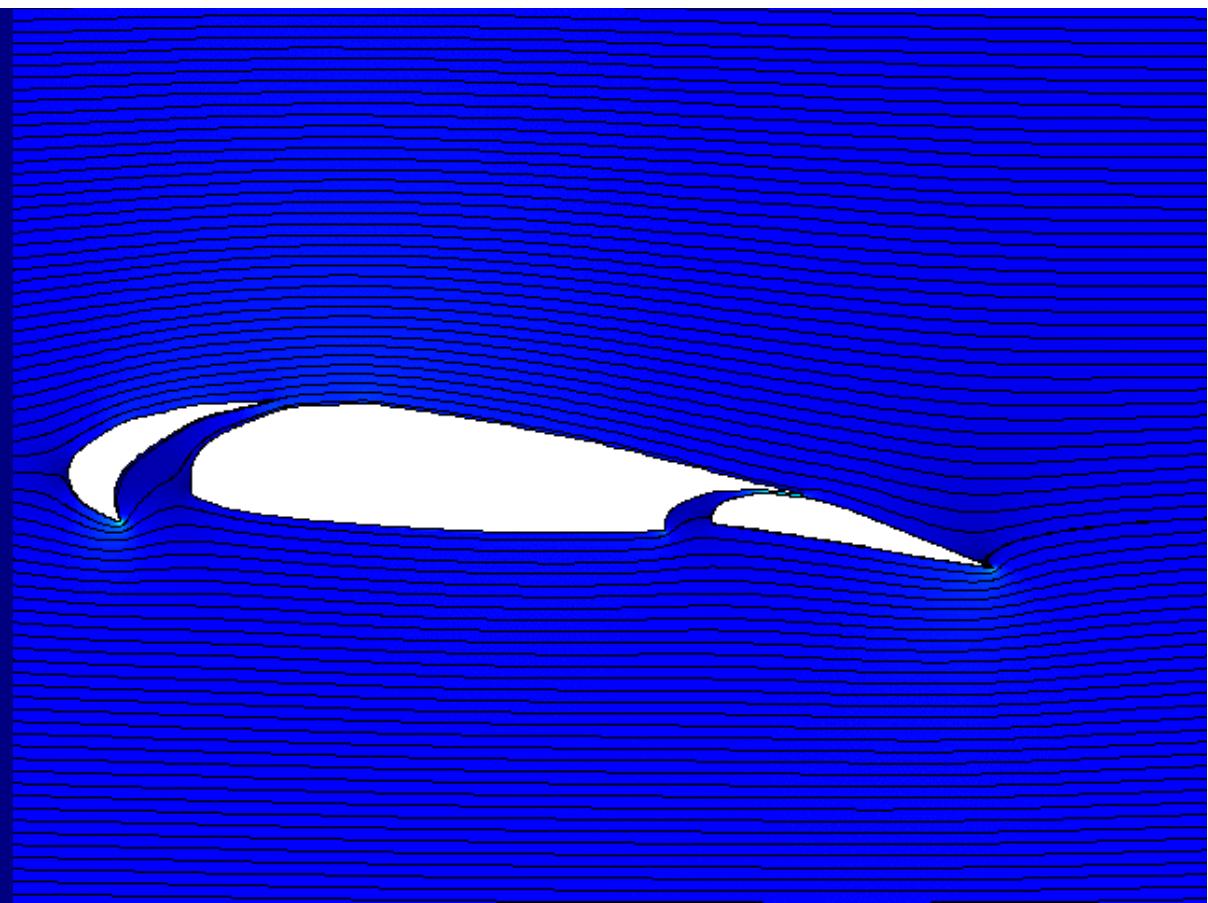


Slat & Flap 2D CFD

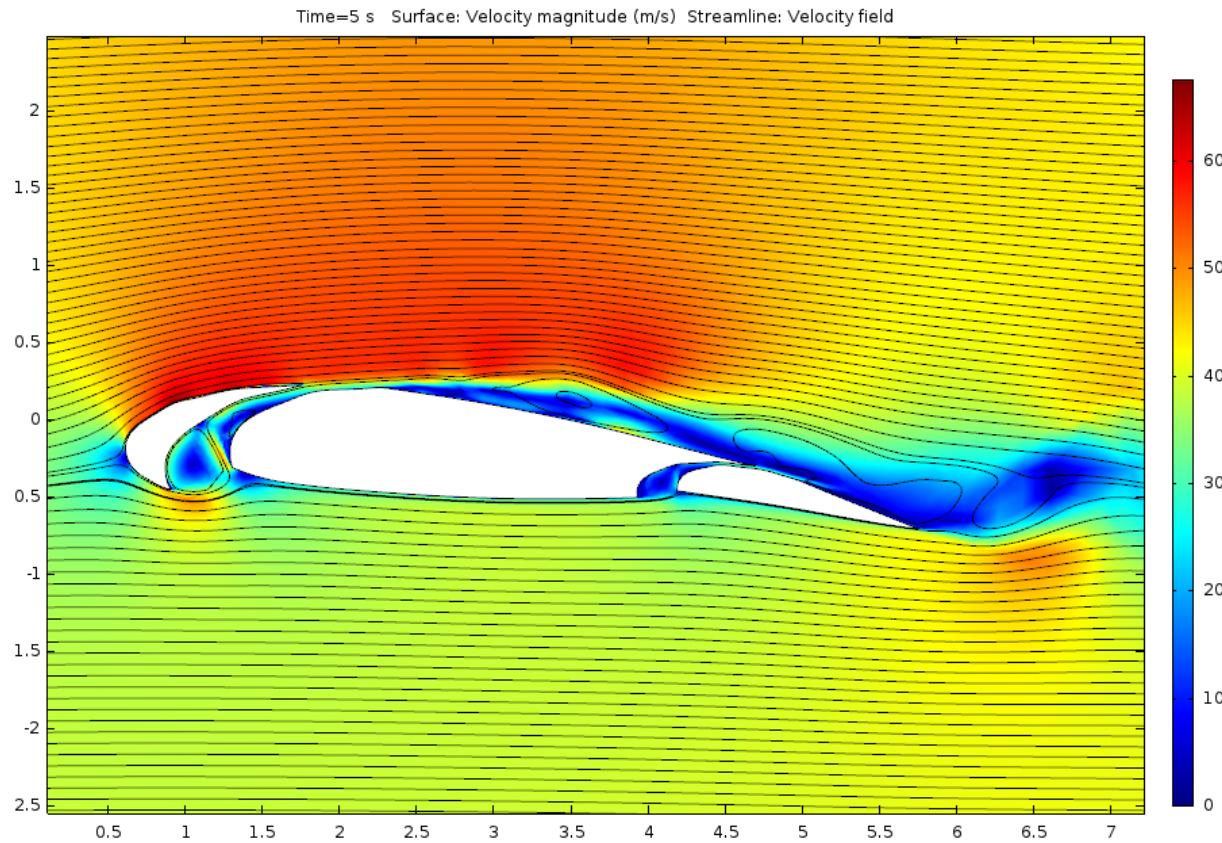
Acceleration from 0 m/s to 240 m/s



40 m/s steady flow



Slat & Flap 2D CFD



Lift (N/m)	Drag(N/m)	Lift/v^2	Drag/v^2
4988.564948	424.2375945	3.117853093	0.265148497

$$\frac{1}{2} \cdot C_L \cdot \rho \cdot A = 0.705 / \text{span}$$

$$\rightarrow \frac{1}{2} \cdot C_L \cdot \rho \cdot A = 3.118 / \text{span}$$

$$\frac{1}{2} \cdot C_D \cdot \rho \cdot A = 0.114 / \text{span}$$

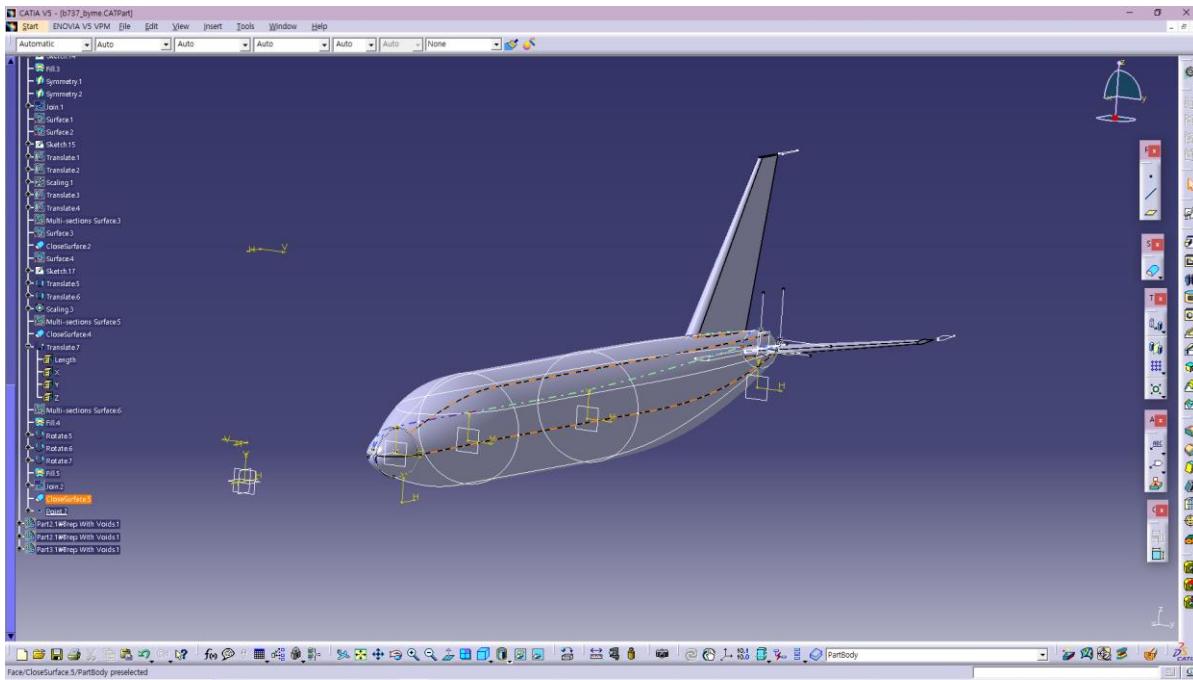
$$\rightarrow \frac{1}{2} \cdot C_D \cdot \rho \cdot A = 0.265 / \text{span}$$

$$C_L/C_D = 6.184 \rightarrow C_L/C_D = 11.77$$

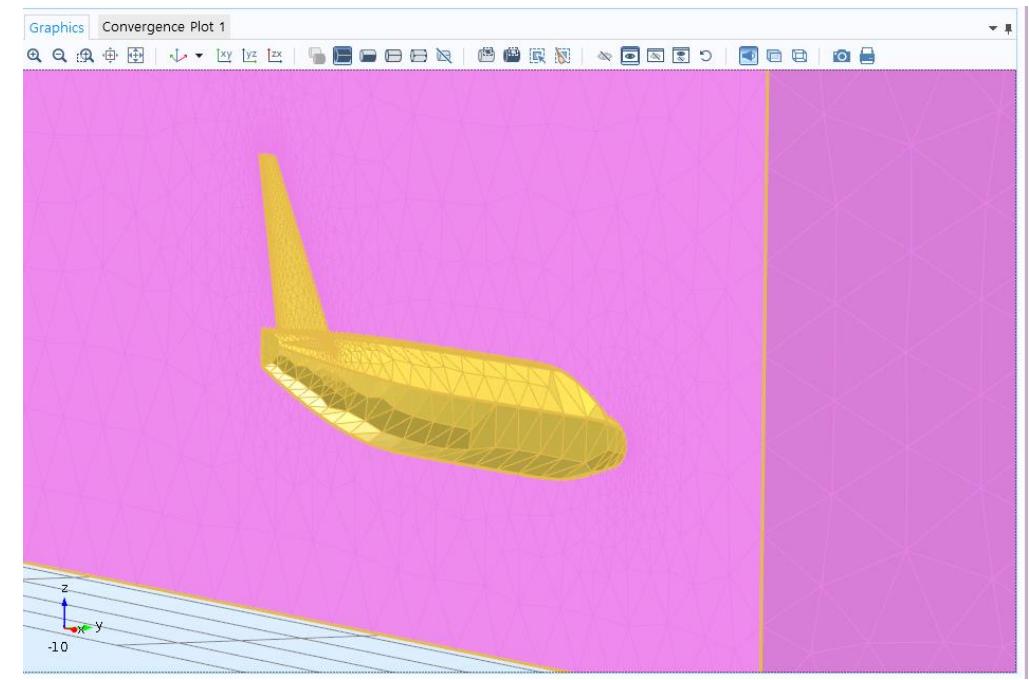
Body & Tailwing 3D CFD

Body & Tail 3D Model

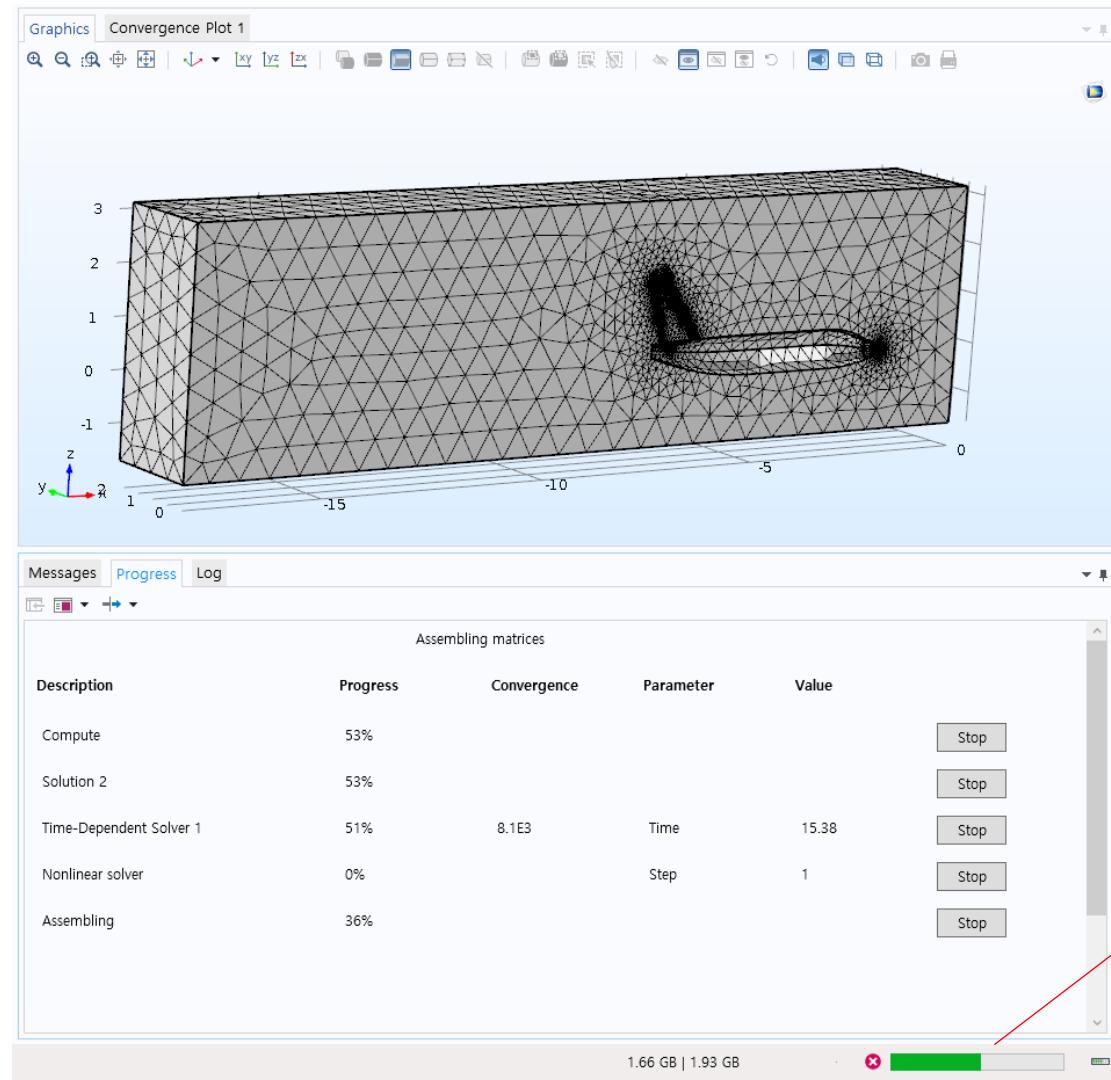
Full Model



Half Model



Body & Tail 3D CFD



Messages Progress Log

124410	15.589	0.00010028	445053	222459	445053	1	98045	1	3.7e-012	4.7e-014
124411	15.589	0.00010028	445055	222460	445055	1	98045	1	1.4e-011	4.3e-014
124412	15.589	0.00010028	445057	222461	445057	1	98045	1	2e-011	7.1e-014
124413	15.59	0.00010132	445061	222463	445061	1	98046	1	4.6e-012	6.2e-014
124414	15.59	0.00010087	445065	222465	445065	1	98047	1	2.9e-012	1.4e-014
124415	15.59	9.7931e-005	445069	222467	445069	1	98048	1	1e-011	2.3e-014
124416	15.59	9.1798e-005	445073	222469	445073	1	98049	1	1.4e-011	2.1e-014
124417	15.59	8.4124e-005	445077	222471	445077	1	98050	1	2.2e-011	3.9e-014

Canceled
Time-Dependent Solver 1 in Study 1/Solution 2 (sol2): Solution time: 114349 s (1 day, 7 hours, 45 minutes, 49 seconds)
Physical memory: 1.71 GB
Virtual memory: 1.99 GB

1 day, 7 hours, 45 minutes

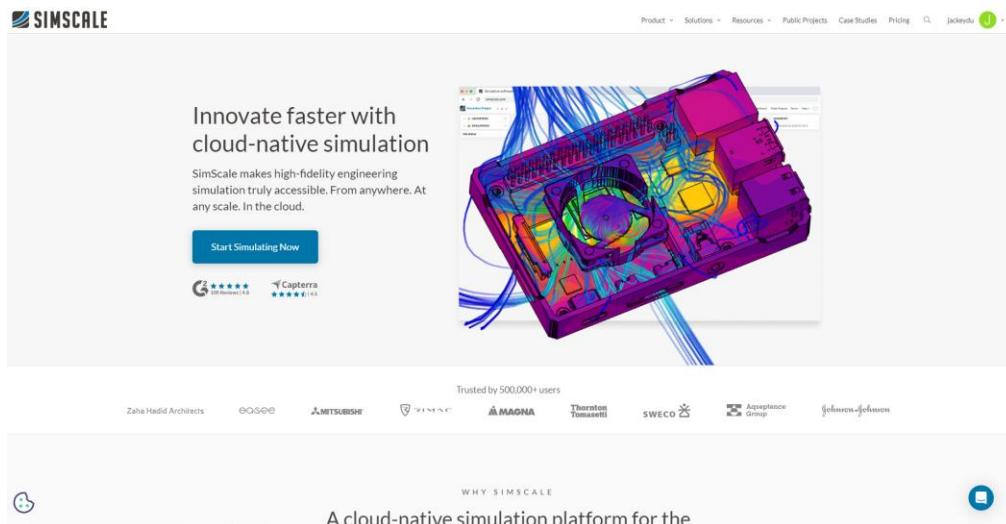
Solution time issue!!

50 %

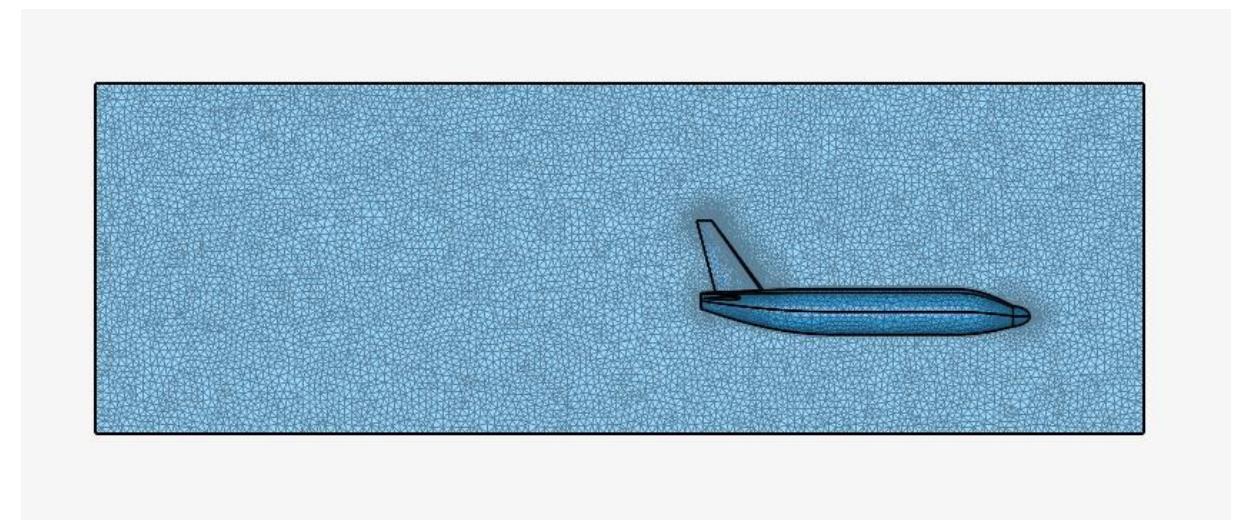
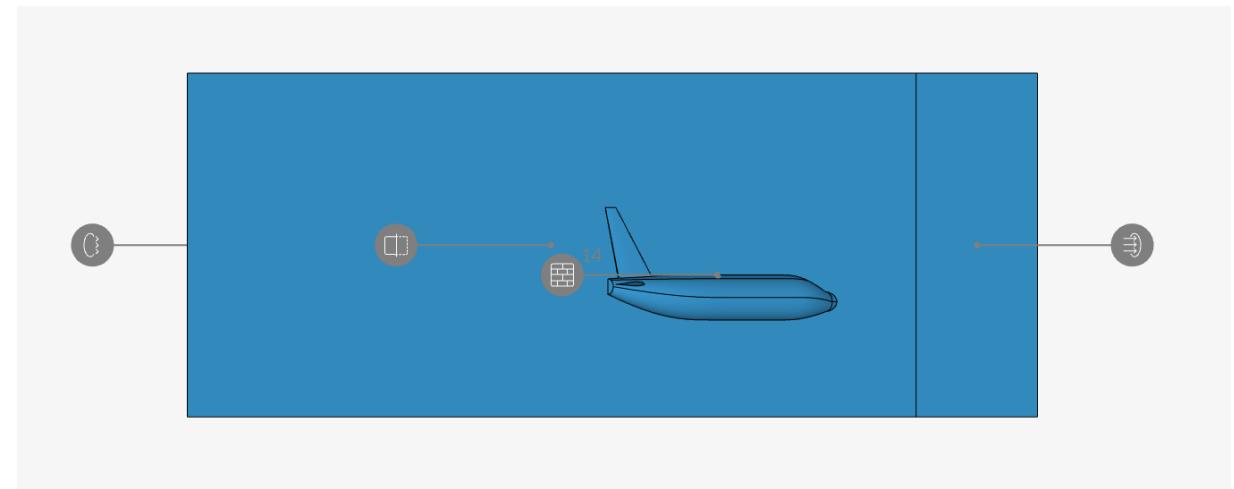
Body & Tail 3D CFD



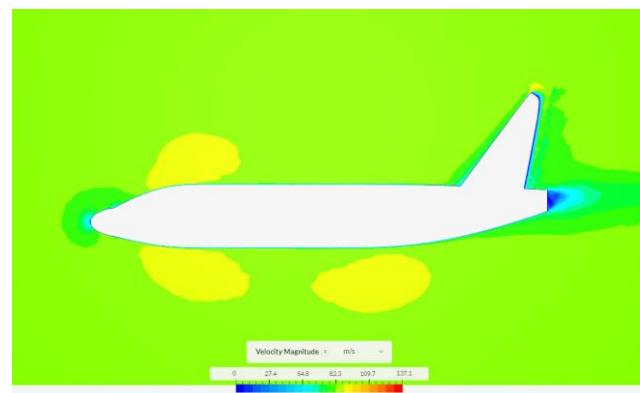
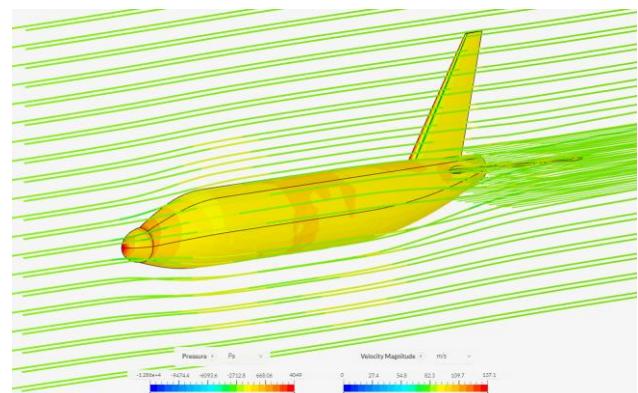
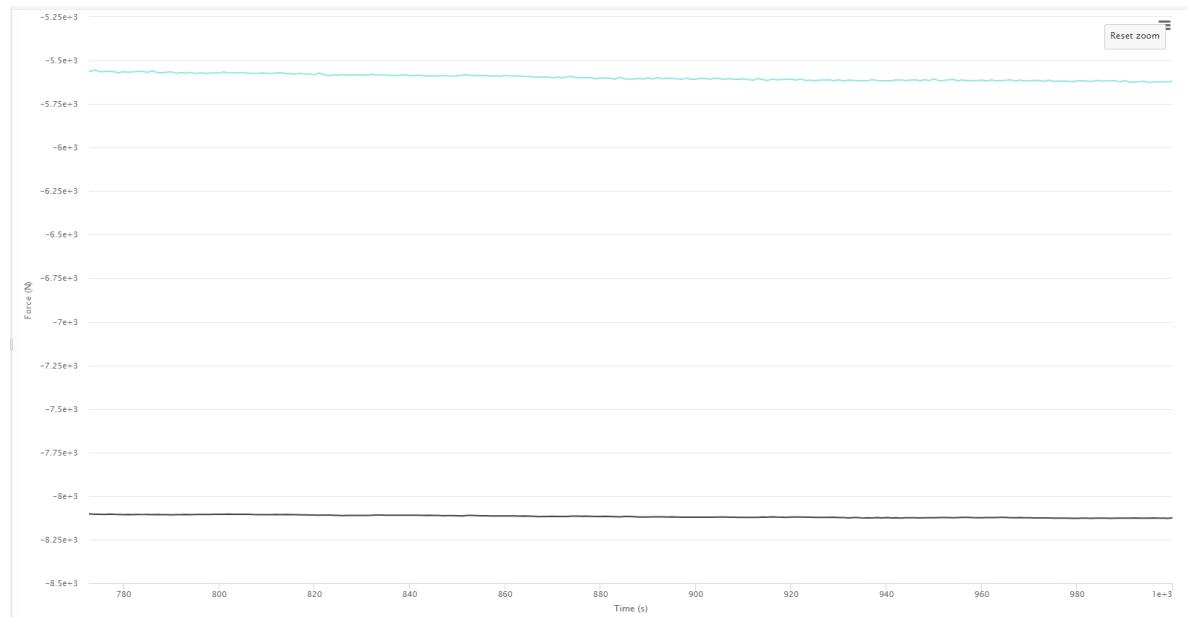
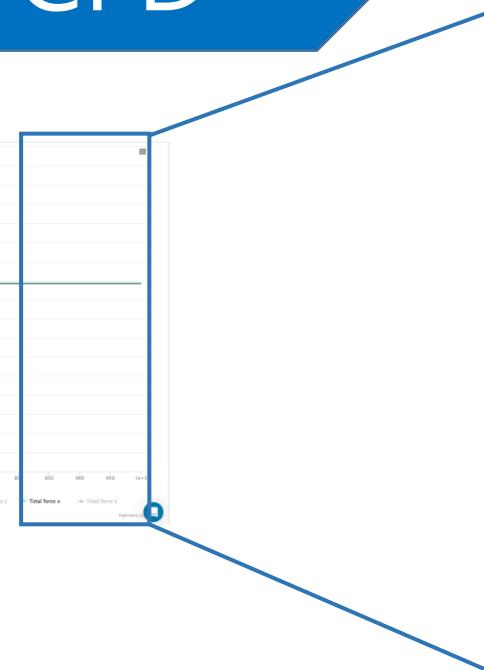
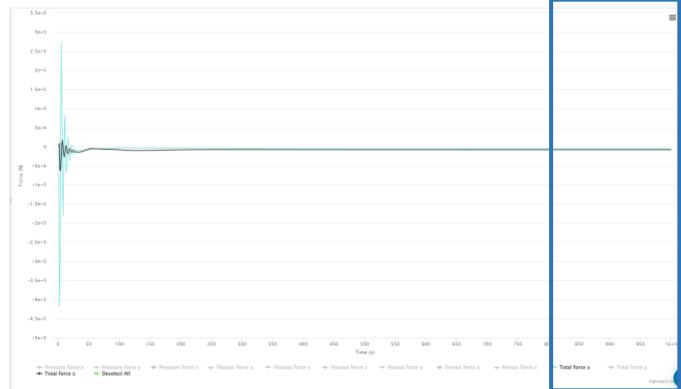
Full-cloud CAE simulation software
Specialized in CFD



The screenshot shows the SimScale homepage. At the top, there's a navigation bar with links for Product, Solutions, Resources, Public Projects, Case Studies, Pricing, and a search bar. Below the navigation is a large call-to-action button with the text "Start Simulating Now". To the left of the button, there's a testimonial: "Innovate faster with cloud-native simulation" and "SimScale makes high-fidelity engineering simulation truly accessible. From anywhere. At any scale. In the cloud." Below this, there are two small reviews from G2 and Capterra. The main feature image shows a 3D model of a mechanical part with a complex internal structure, colored with a rainbow gradient to represent simulation results. At the bottom of the page, there's a section titled "WHY SIMSCALE" with the subtext "A cloud-native simulation platform for the" followed by a list of logos for various clients like Zaha Hadid Architects, OGESE, Mitsubishi, TÜV SÜD, Magna, Thornton-Tomasetti, SWECO, Arup Group, and Johnson & Johnson.



Body & Tail 3D CFD

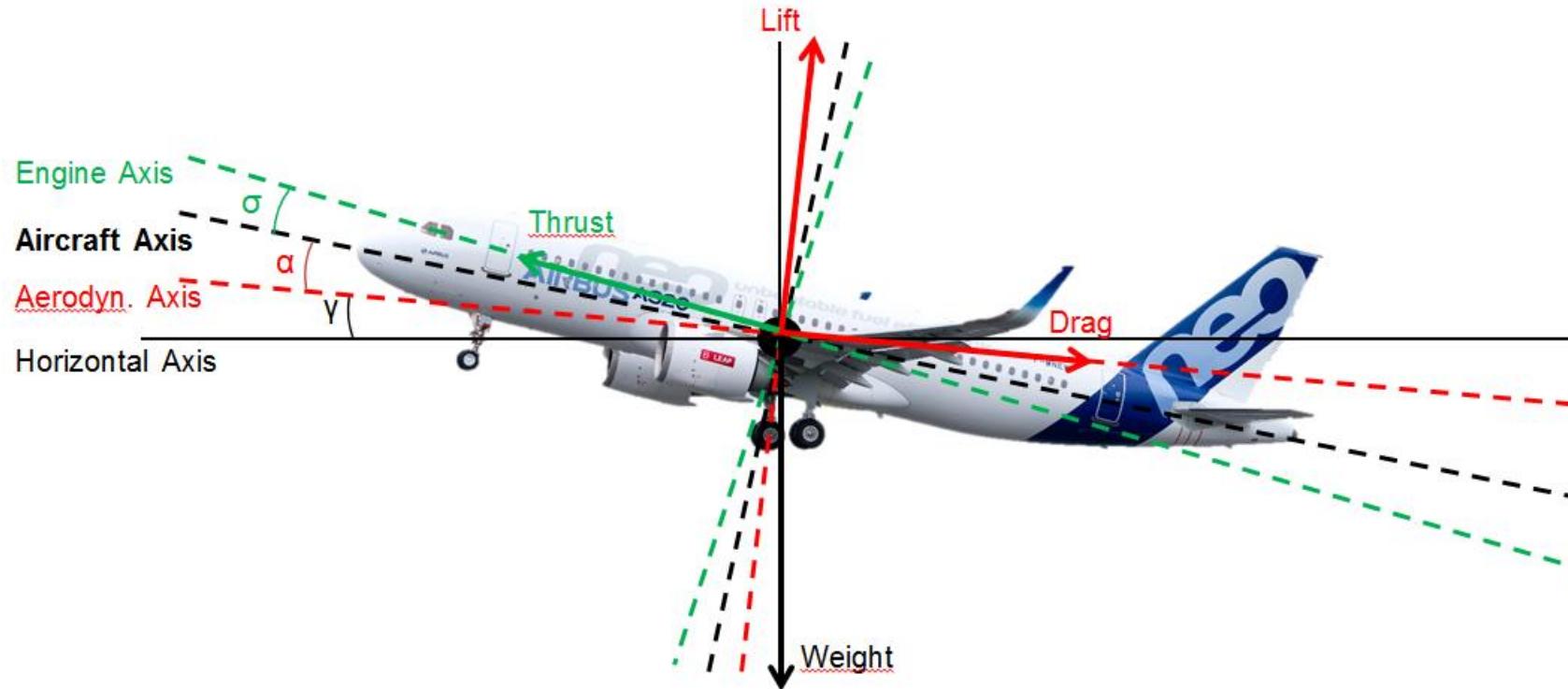


Body & Tail 3D CFD

Time (s)	POROUS_F	POROUS_F	POROUS_FORCE_Z	PRESSURE_FORCE_X	PRESSURE_FORCE_Y	PRESSURE_FORCE_Z	TOTAL_FORCE_X	TOTAL_FORCE_Y	TOTAL_FORCE_Z	VISCOUS_FORCE_X	VISCOUS_FORCE_Y	VISCOUS_FORCE_Z	Total Lift	Total Drag
1	0.00E+00	0.00E+00	0.00E+00	-9.38E+01	-4.83E+03	-1.08E+01	-9.41E+01	-4.83E+03	-1.08E+01	-3.17E-01	-5.61E-03	-1.92E-02	-8.12E+03	5.60E+03
2	0.00E+00	0.00E+00	0.00E+00	-4.19E+05	-2.29E+07	8.41E+03	-4.19E+05	-2.29E+07	8.42E+03	-9.18E+01	2.53E+00	2.43E+00	Lift/v^2	Drag/v^2
3	0.00E+00	0.00E+00	0.00E+00	-3.61E+05	-1.77E+07	-6.00E+04	-3.61E+05	-1.77E+07	-6.00E+04	-9.20E+01	3.40E+00	2.53E+00	-1.27E+00	8.75E-01
4	0.00E+00	0.00E+00	0.00E+00	4.78E+04	4.10E+06	-6.31E+04	4.77E+04	4.10E+06	-6.31E+04	-9.35E+01	3.59E+00	2.31E+00		
5	0.00E+00	0.00E+00	0.00E+00	2.74E+05	1.53E+07	-2.84E+04	2.74E+05	1.53E+07	-2.84E+04	-9.19E+01	3.76E+00	2.04E+00		
6	0.00E+00	0.00E+00	0.00E+00	1.49E+05	7.84E+06	7.19E+03	1.49E+05	7.84E+06	7.20E+03	-8.91E+01	3.84E+00	1.90E+00		
7	0.00E+00	0.00E+00	0.00E+00	-9.55E+04	-5.16E+06	1.73E+04	-9.56E+04	-5.16E+06	1.73E+04	-8.74E+01	3.92E+00	1.88E+00		
8	0.00E+00	0.00E+00	0.00E+00	-1.82E+05	-9.17E+06	5.83E+02	-1.82E+05	-9.17E+06	5.85E+02	-8.68E+01	3.98E+00	1.91E+00		
9	0.00E+00	0.00E+00	0.00E+00	-7.49E+04	-2.86E+06	-2.06E+04	-7.50E+04	-2.86E+06	-2.06E+04	-8.63E+01	4.02E+00	1.90E+00		
10	0.00E+00	0.00E+00	0.00E+00	6.00E+04	4.32E+06	-2.75E+04	5.99E+04	4.32E+06	-2.75E+04	-8.47E+01	4.03E+00	1.81E+00		
11	0.00E+00	0.00E+00	0.00E+00	8.13E+04	5.02E+06	-1.69E+04	8.12E+04	5.02E+06	-1.69E+04	-8.23E+01	4.03E+00	1.71E+00		
12	0.00E+00	0.00E+00	0.00E+00	3.57E+03	5.11E+05	-2.12E+03	3.49E+03	5.11E+05	-2.12E+03	-7.99E+01	4.09E+00	1.63E+00		
13	0.00E+00	0.00E+00	0.00E+00	-6.63E+04	-3.14E+06	2.65E+03	-6.64E+04	-3.14E+06	2.65E+03	-7.80E+01	4.22E+00	1.64E+00		
14	0.00E+00	0.00E+00	0.00E+00	-6.20E+04	-2.55E+06	-4.95E+03	-6.21E+04	-2.55E+06	-4.95E+03	-7.66E+01	4.36E+00	1.67E+00		
15	0.00E+00	0.00E+00	0.00E+00	-1.00E+04	4.12E+05	-1.55E+04	-1.01E+04	4.12E+05	-1.55E+04	-7.51E+01	4.46E+00	1.69E+00		
16	0.00E+00	0.00E+00	0.00E+00	2.45E+04	2.10E+06	-1.89E+04	2.45E+04	2.10E+06	-1.89E+04	-7.34E+01	4.49E+00	1.71E+00		
17	0.00E+00	0.00E+00	0.00E+00	1.29E+04	1.21E+06	-1.34E+04	1.28E+04	1.21E+06	-1.34E+04	-7.16E+01	4.47E+00	1.72E+00		
18	0.00E+00	0.00E+00	0.00E+00	-2.04E+04	-5.74E+05	-6.72E+03	-2.05E+04	-5.74E+05	-6.71E+03	-6.99E+01	4.43E+00	1.73E+00		
19	0.00E+00	0.00E+00	0.00E+00	-3.72E+04	-1.23E+06	-5.28E+03	-3.72E+04	-1.23E+06	-5.28E+03	-6.87E+01	4.38E+00	1.75E+00		
20	0.00E+00	0.00E+00	0.00E+00	-2.59E+04	-4.41E+05	-9.19E+03	-2.60E+04	-4.41E+05	-9.18E+03	-6.76E+01	4.33E+00	1.74E+00		
21	0.00E+00	0.00E+00	0.00E+00	-4.85E+03	5.76E+05	-1.38E+04	-4.92E+03	5.76E+05	-1.38E+04	-6.65E+01	4.26E+00	1.71E+00		
22	0.00E+00	0.00E+00	0.00E+00	4.24E+03	7.57E+05	-1.50E+04	4.18E+03	7.57E+05	-1.50E+04	-6.53E+01	4.18E+00	1.67E+00		
23	0.00E+00	0.00E+00	0.00E+00	-3.22E+03	1.74E+05	-1.26E+04	-3.28E+03	1.74E+05	-1.26E+04	-6.43E+01	4.05E+00	1.62E+00		
24	0.00E+00	0.00E+00	0.00E+00	-1.54E+04	-3.70E+05	-1.00E+04	-1.55E+04	-3.70E+05	-1.00E+04	-6.33E+01	3.91E+00	1.57E+00		
25	0.00E+00	0.00E+00	0.00E+00	-1.99E+04	-3.50E+05	-9.83E+03	-2.00E+04	-3.50E+05	-9.83E+03	-6.24E+01	3.76E+00	1.52E+00		
26	0.00E+00	0.00E+00	0.00E+00	-1.52E+04	4.40E+04	-1.17E+04	-1.53E+04	4.40E+04	-1.17E+04	-6.17E+01	3.61E+00	1.46E+00		
27	0.00E+00	0.00E+00	0.00E+00	-8.24E+03	3.16E+05	-1.39E+04	-8.30E+03	3.16E+05	-1.39E+04	-6.10E+01	3.46E+00	1.40E+00		
28	0.00E+00	0.00E+00	0.00E+00	-5.71E+03	2.36E+05	-1.48E+04	-5.78E+03	2.36E+05	-1.48E+04	-6.04E+01	3.32E+00	1.34E+00		
29	0.00E+00	0.00E+00	0.00E+00	-8.26E+03	-1.28E+04	-1.43E+04	-8.32E+03	-1.28E+04	-1.43E+04	-5.98E+01	3.18E+00	1.29E+00		
30	0.00E+00	0.00E+00	0.00E+00	-1.18E+04	-1.40E+05	-1.36E+04	-1.19E+04	-1.40E+05	-1.36E+04	-5.92E+01	3.06E+00	1.24E+00		
31	0.00E+00	0.00E+00	0.00E+00	-1.28E+04	-5.91E+04	-1.35E+04	-1.29E+04	-5.91E+04	-1.35E+04	-5.88E+01	2.94E+00	1.20E+00		
32	0.00E+00	0.00E+00	0.00E+00	-1.11E+04	8.70E+04	-1.42E+04	-1.12E+04	8.70E+04	-1.42E+04	-5.84E+01	2.82E+00	1.15E+00		
33	0.00E+00	0.00E+00	0.00E+00	-9.15E+03	1.36E+05	-1.48E+04	-9.21E+03	1.36E+05	-1.48E+04	-5.81E+01	2.70E+00	1.11E+00		
34	0.00E+00	0.00E+00	0.00E+00	-8.78E+03	6.72E+04	-1.49E+04	-8.84E+03	6.72E+04	-1.49E+04	-5.79E+01	2.59E+00	1.07E+00		
35	0.00E+00	0.00E+00	0.00E+00	-9.88E+03	-1.85E+04	-1.45E+04	-9.94E+03	-1.85E+04	-1.45E+04	-5.77E+01	2.49E+00	1.04E+00		

Take off situation

Take – off



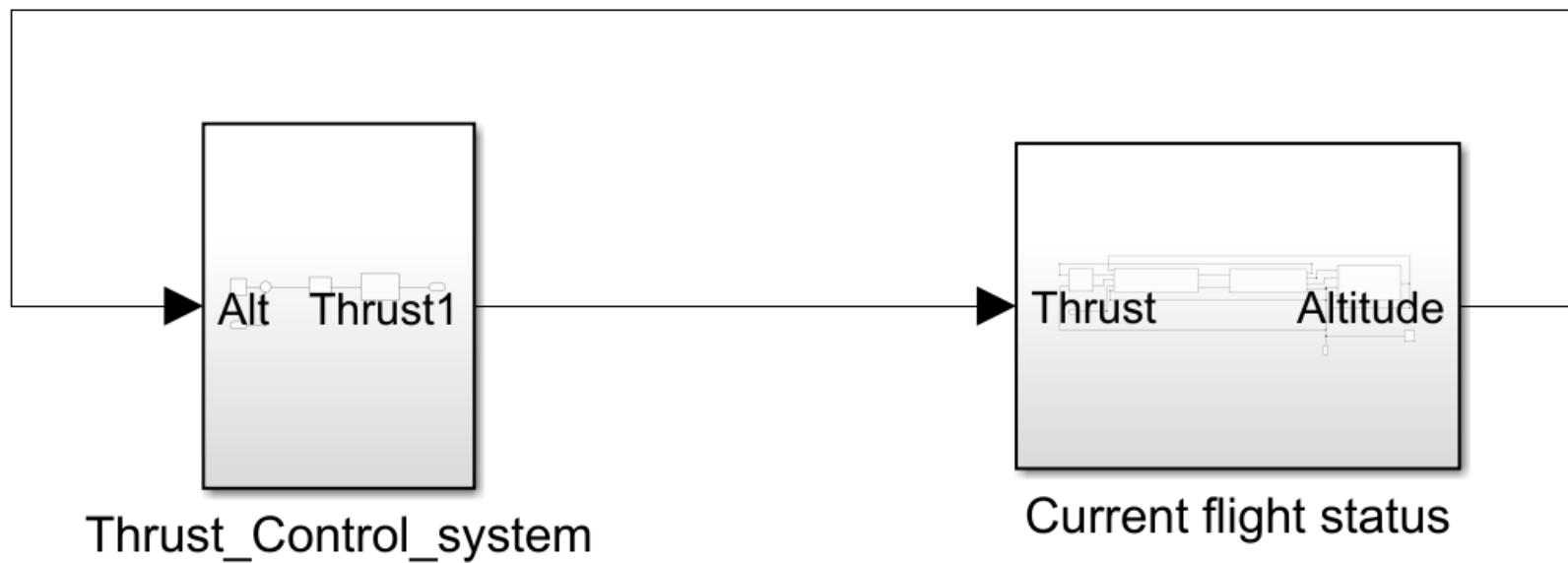
Engine Axis = Aircraft Axis

To negelect an effect of Aerodyn. Axis, set a climb angle by velocity

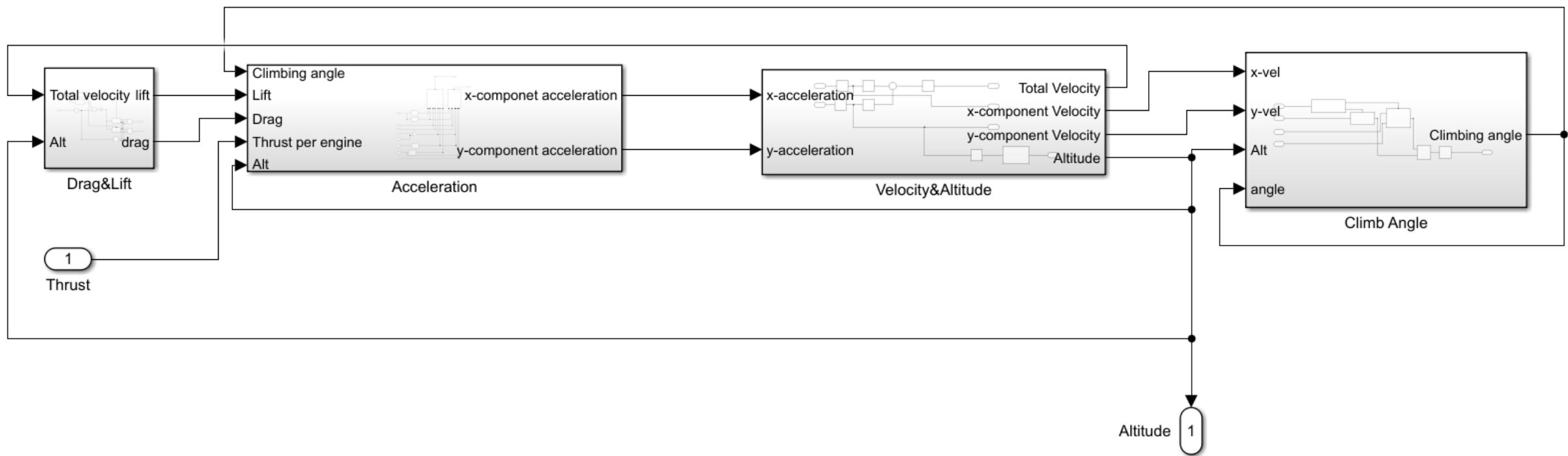
Maintaining altitude at 12000m

Build a system using simulink

System component

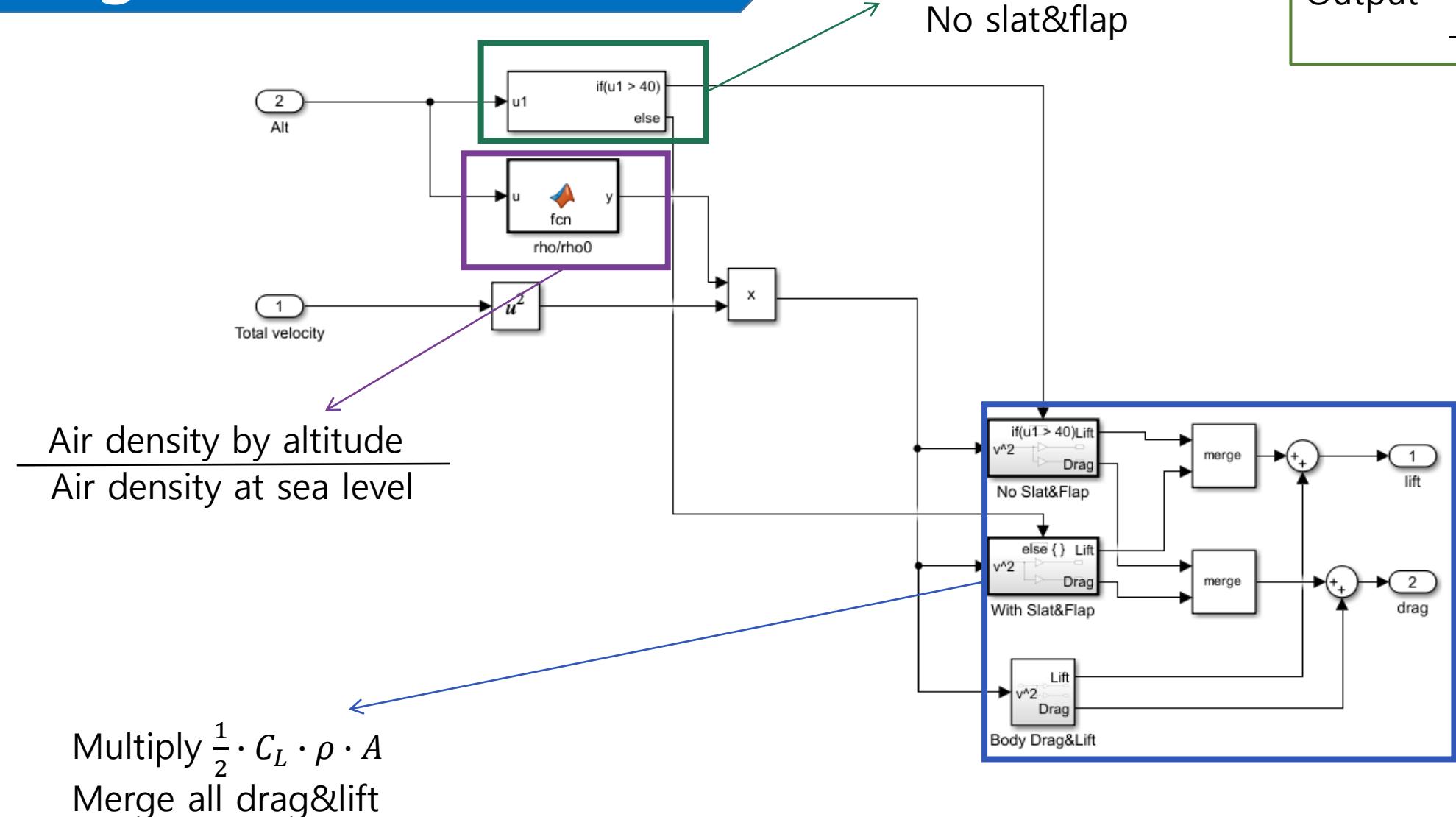


Current flight status



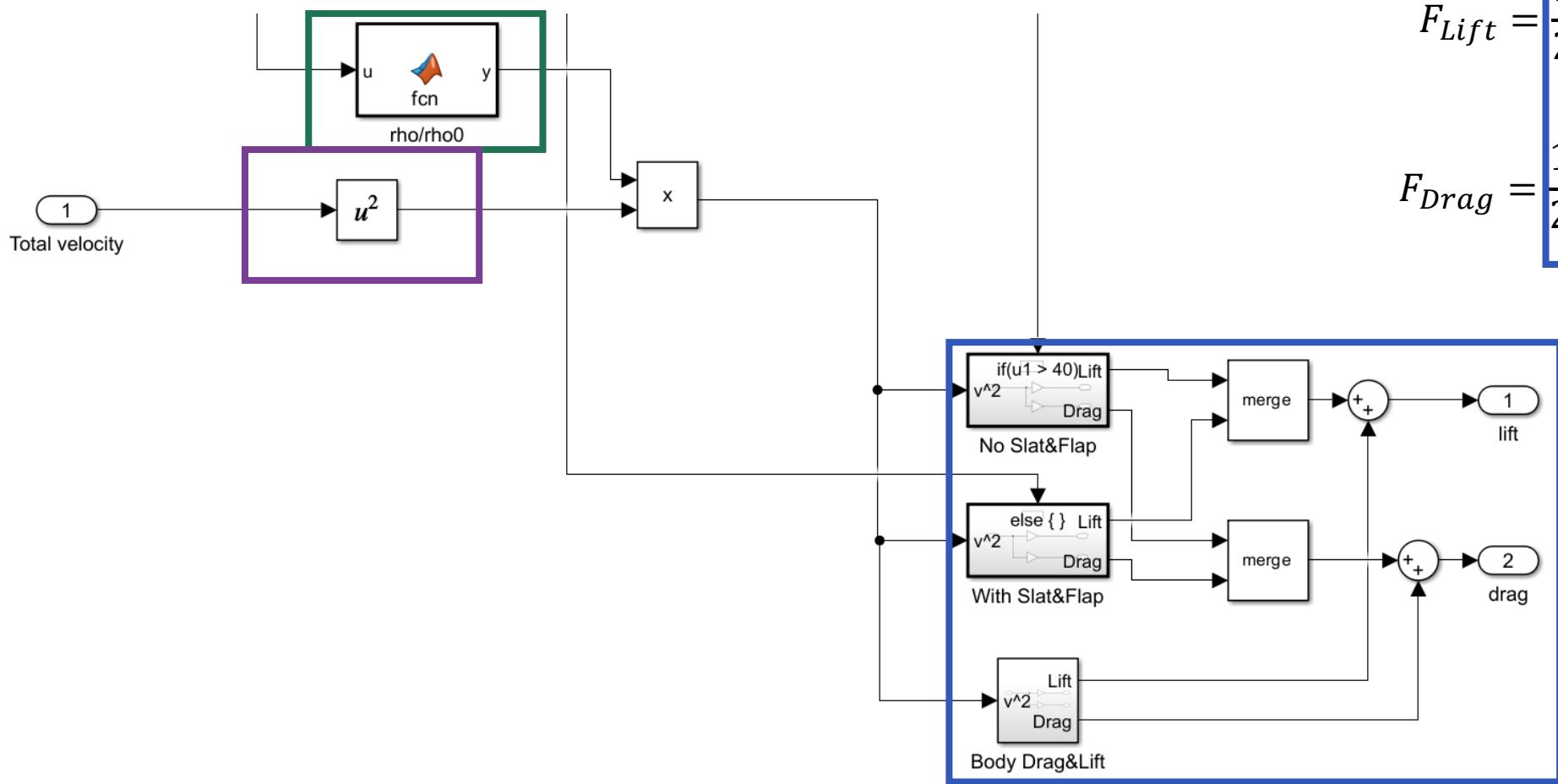
Drag&Lift

Drag&Lift



Input	-Altitude -Total velocity
Output	- Lift - Drag

Drag&Lift



$$F_{Lift} = \frac{1}{2} \cdot C_L \cdot \rho \cdot A \cdot v^2$$

$$F_{Drag} = \frac{1}{2} \cdot C_D \cdot \rho \cdot A \cdot v^2$$

Air density by altitude

Air density at sea level

Screenshot of a MATLAB workspace window showing a function file named rho/rho0.m:

```

rho/rho0 x Acceleration x
Boeing_737_500_5 > Current flight status > Drag&Lift > rho/rho0

function y = fcn(u)
p0 = 101325;
M = 0.0289652;
R = 8.31446;
T0 = 288.15;
L = 0.0065;
h = u;
g = 9.81;
T = T0-L*h;

rho_0 = (p0*M)/(R*T0)*(1)^(-(g*M)/(R*L));
rho = (p0*M)/(R*T)*(1+(L*h)/T0)^(-(g*M)/(R*L));
y = rho/rho_0;

```

$p_0 = 101325$	Pa	sea level standard atmospheric pressure
$T_0 = 288.15$	K	sea level standard temperature
$g = 9.80665$	m/s ²	Earth-surface gravitational acceleration
$L = 0.0065$	K/m	temperature lapse rate
$R = 8.31447$	J/(mol·K)	universal gas constant
$M = 0.0289644$	kg/mol	molar mass of dry air

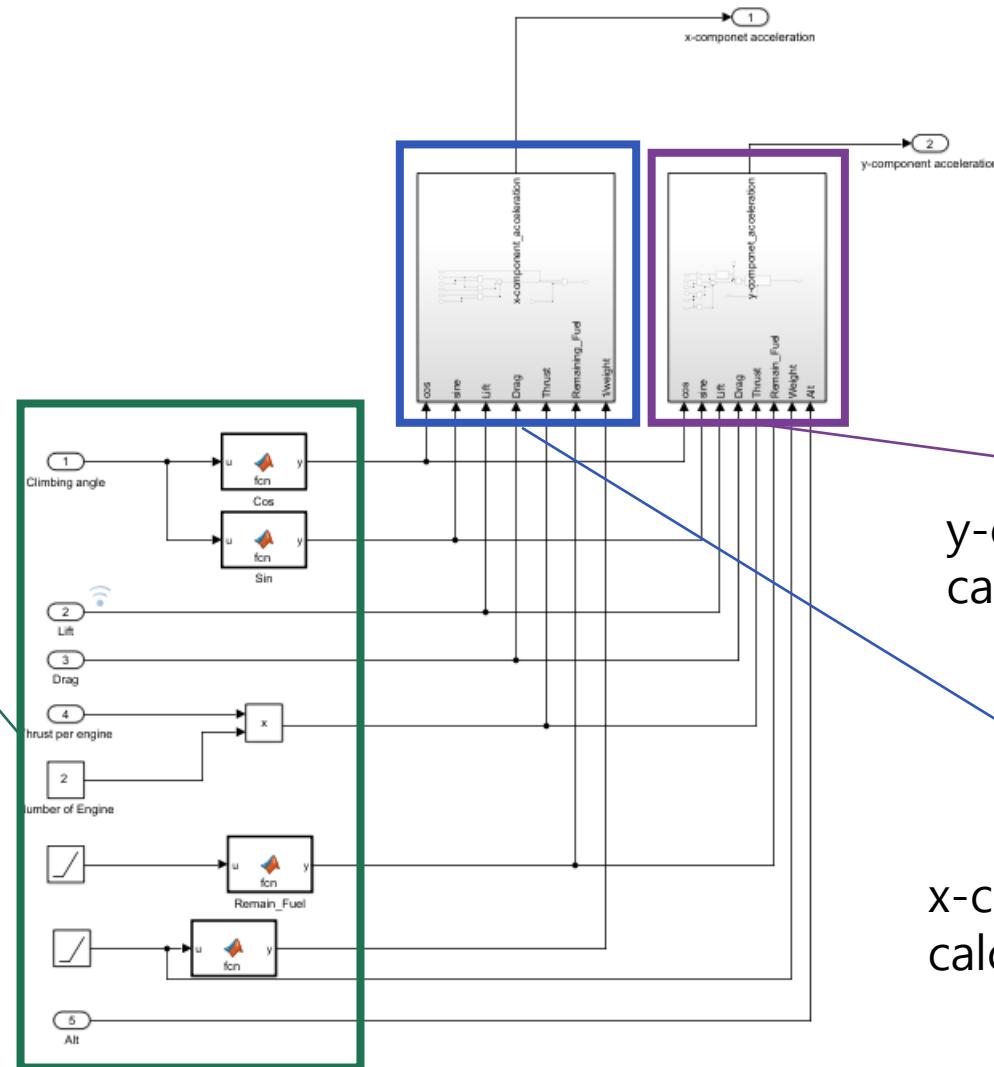
$$p = p_0 \cdot \left(1 + \frac{L \cdot h}{T_0}\right)^{\frac{g \cdot M}{-R \cdot L}}$$

$$\rho = \frac{p}{R \cdot T}$$

Acceleration

Acceleration

Inputs



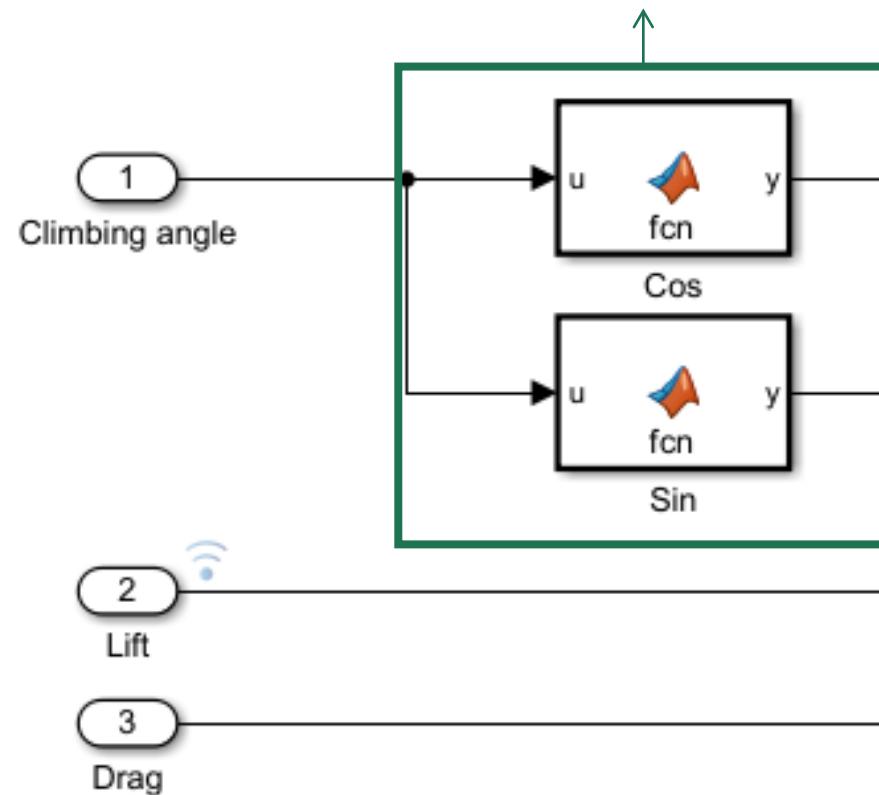
Input	-Climb angle -Lift -Drag -Thrust per engine -Altitude
Output	- x-component acceleration - y-component acceleration

y-component acceleration
calculation sub-system

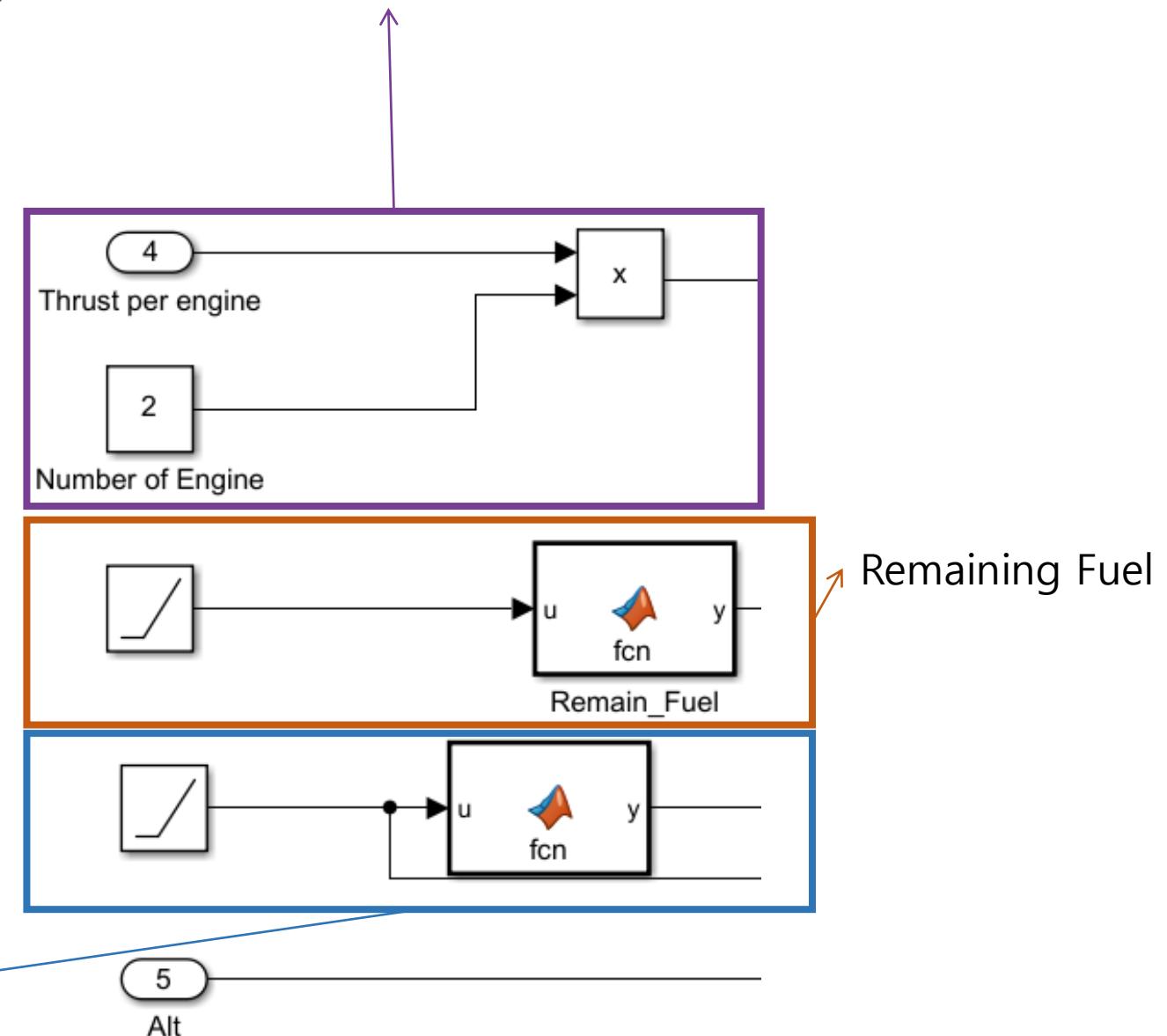
x-component acceleration
calculation sub-system

Inputs

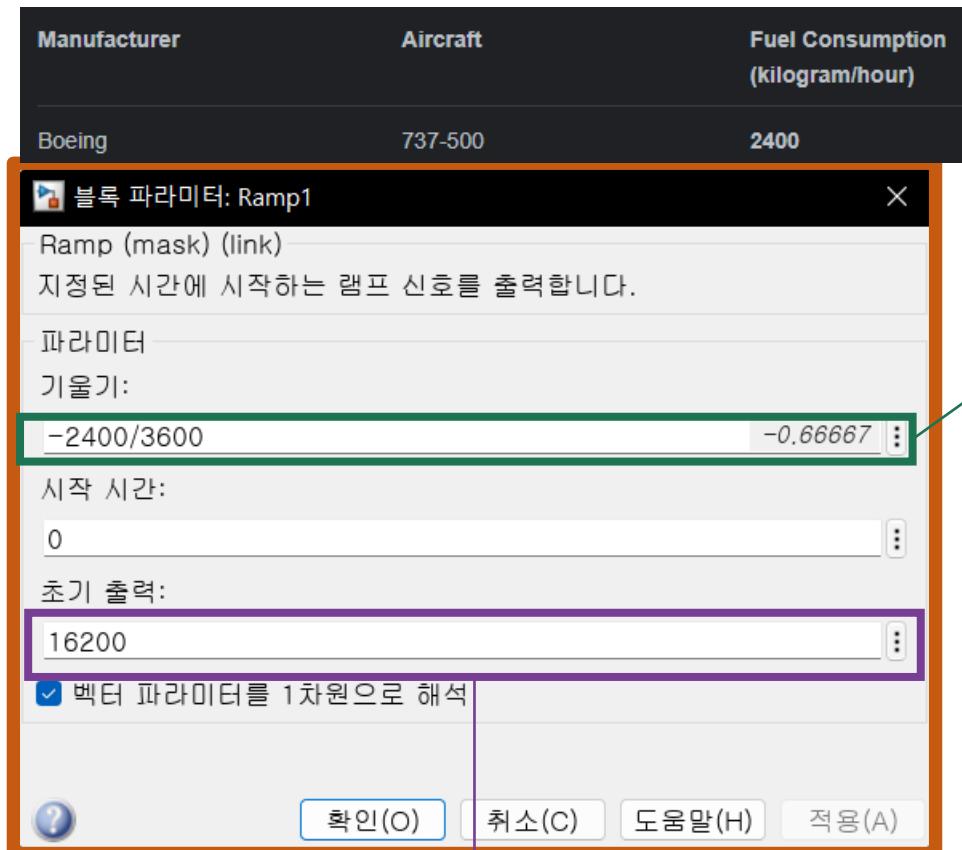
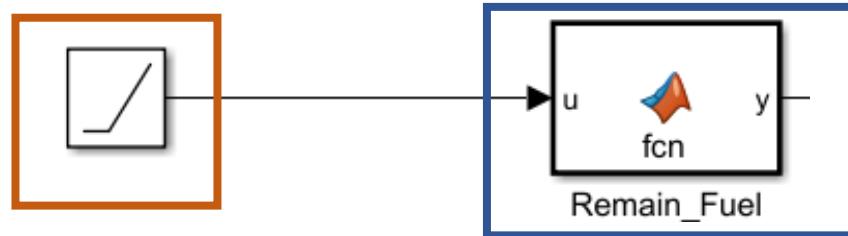
Calculate Cos&Sine value by climb angle



Calculate total thrust



Inputs – Remaining Fuel



Fuel consumption 2400kg/hour

```

function y = fcn(u)

%연료 소비가 다 되었을 때 가속도를 0으로 만들어주는 함수

if u <= 0;
    y = 0;

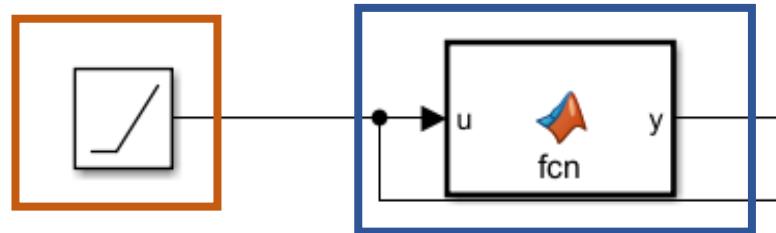
else
    y = 1;

end

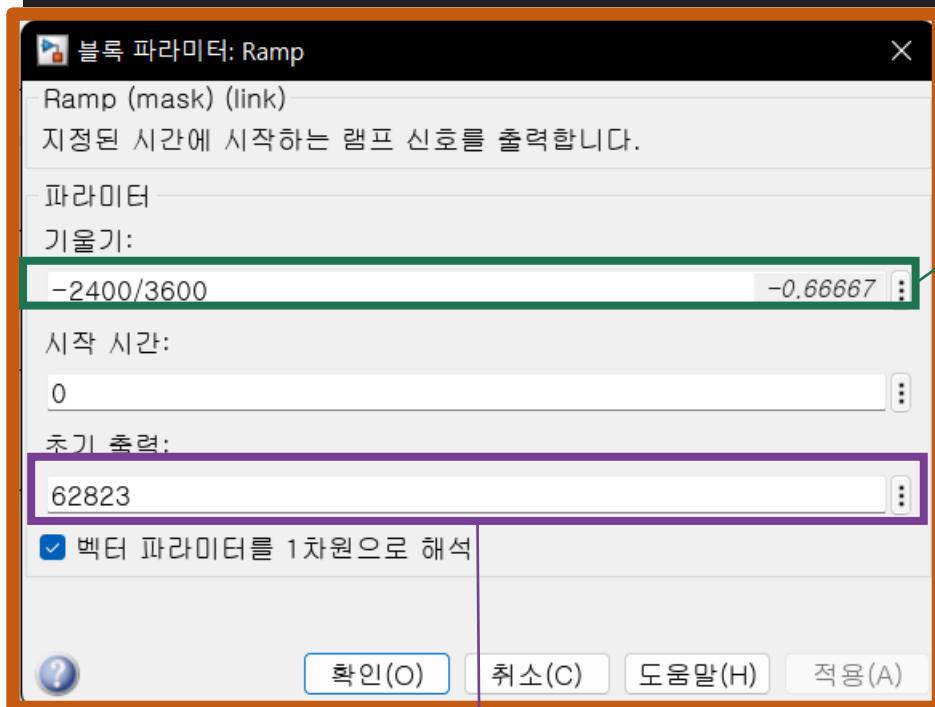
```

Max fuel mass

Inputs – Total aircraft weight



Manufacturer	Aircraft	Fuel Consumption (kilogram/hour)
Boeing	737-500	2400



Fuel consumption 2400kg/hour

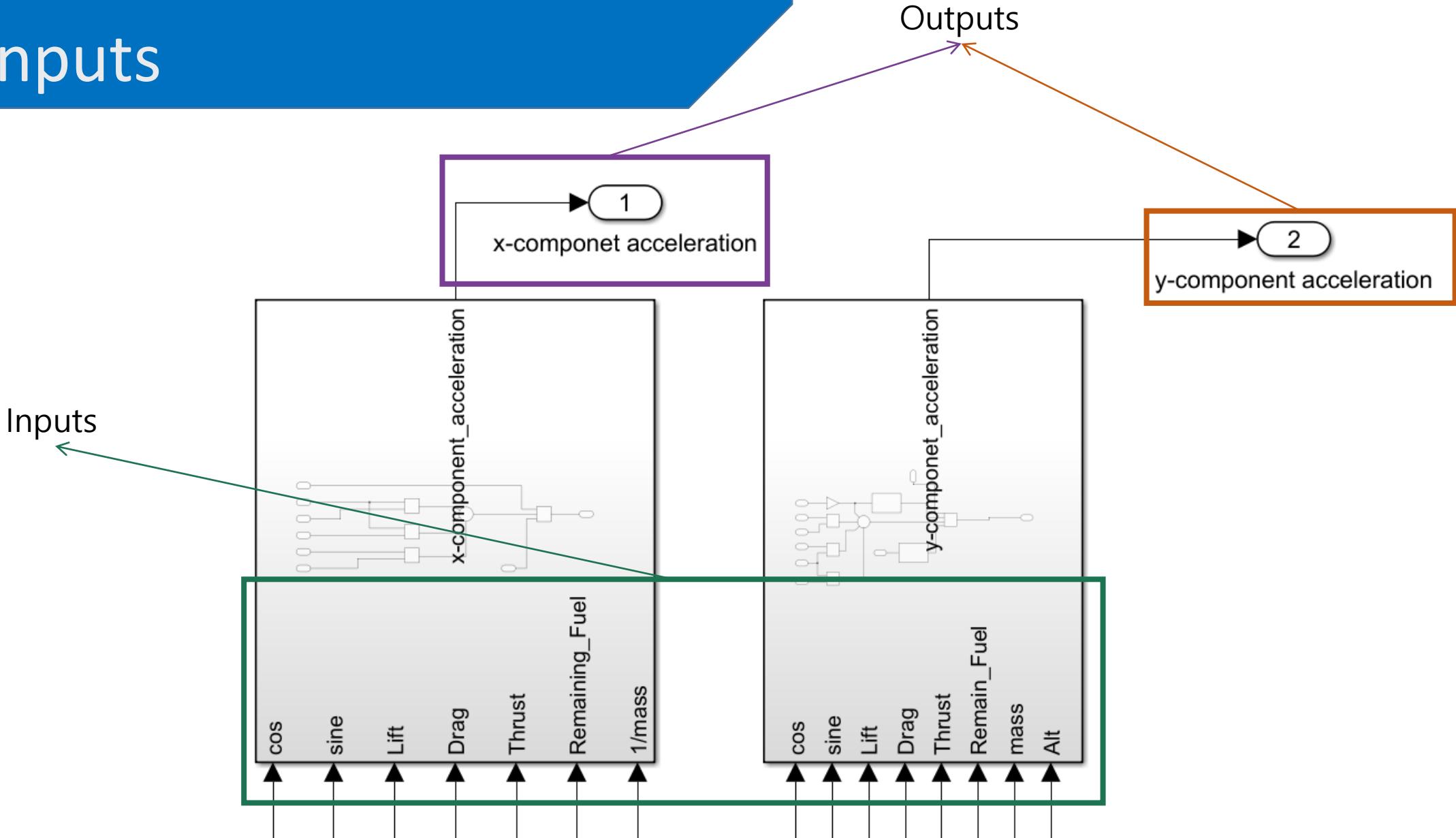
Boeing_737_500_5 > Current flight status > Acceleration > MATLAB Function1

```

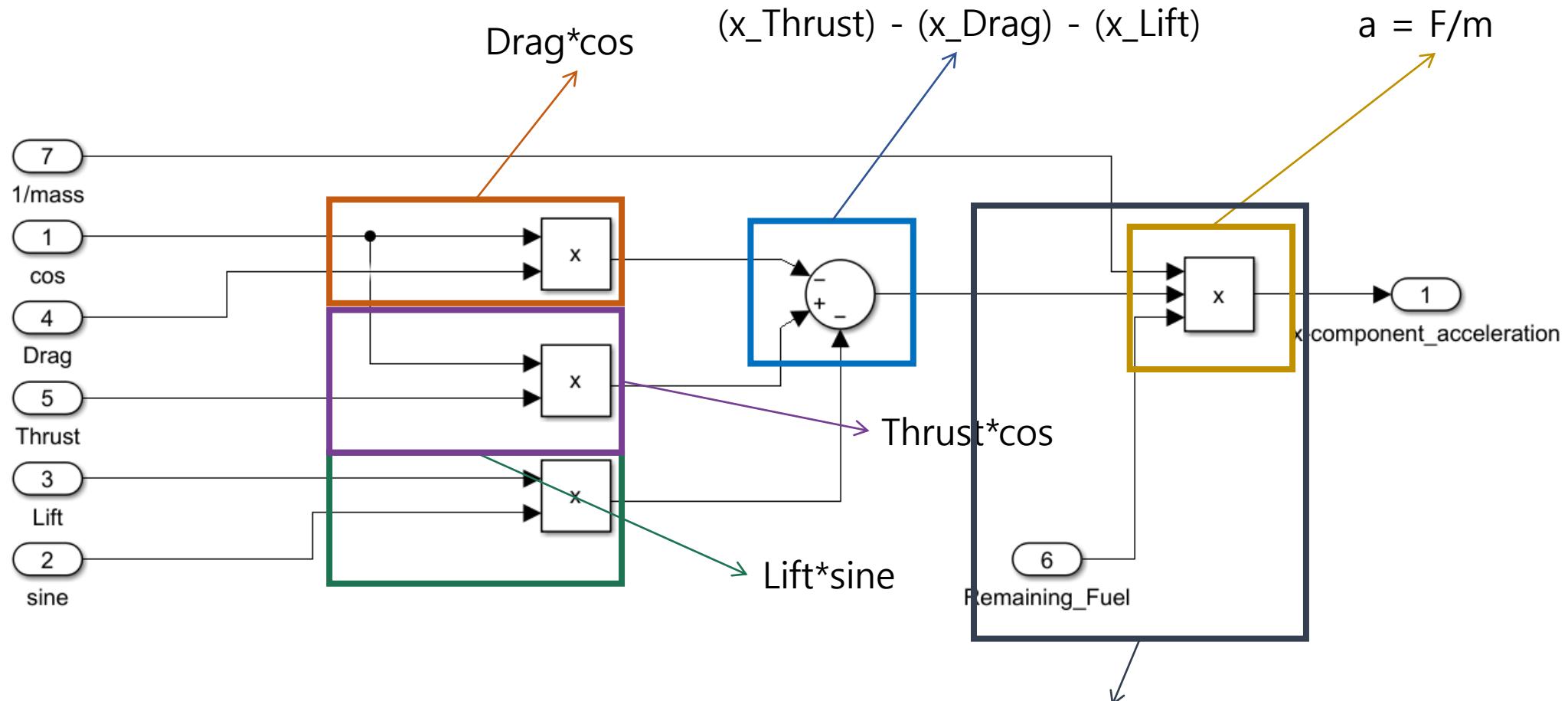
function y = fcn(u)
y = 1/u;
% y = 1/weight
  
```

Max take-off mass

Inputs

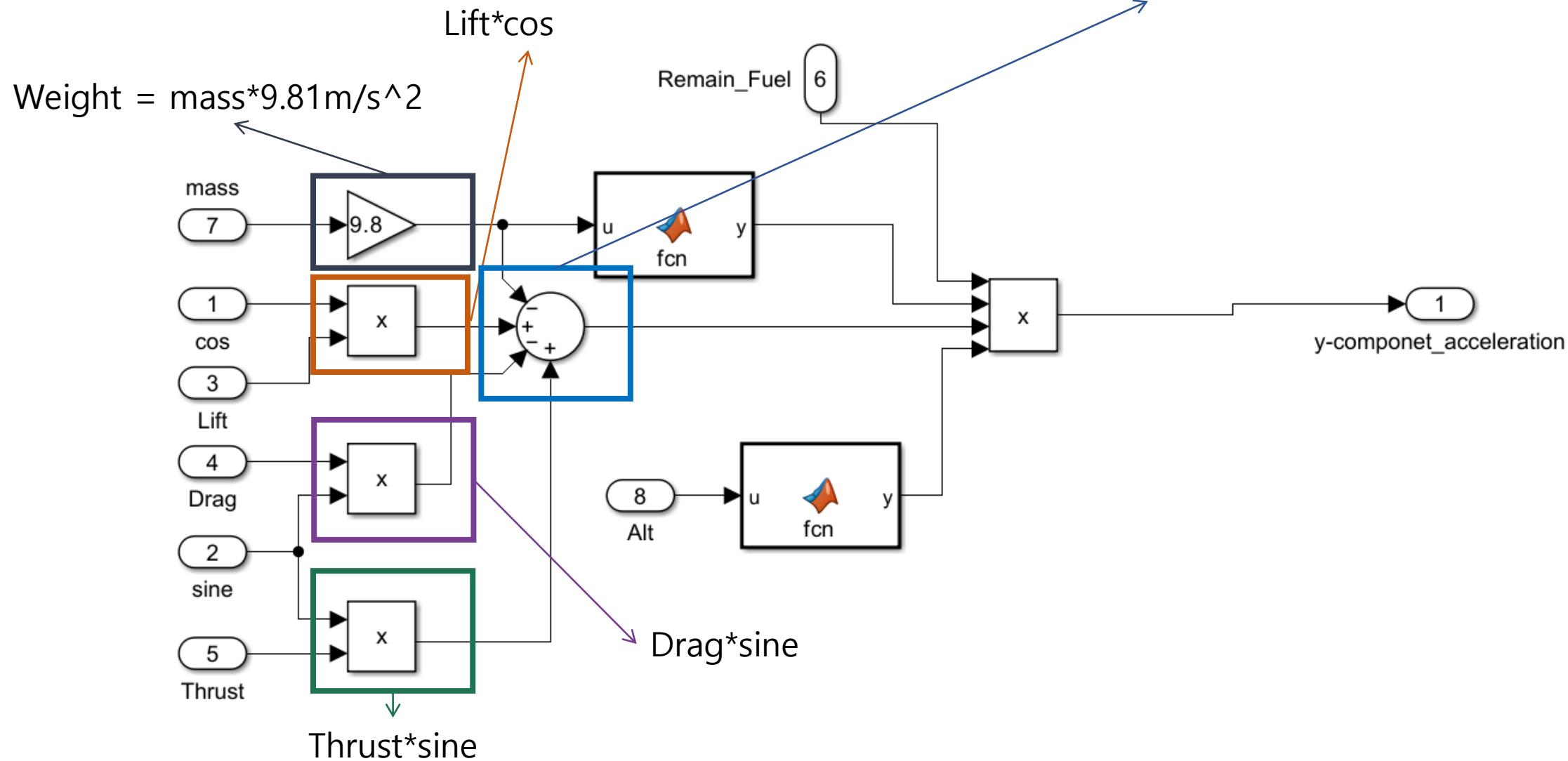


x-component acceleration calculation sub-system



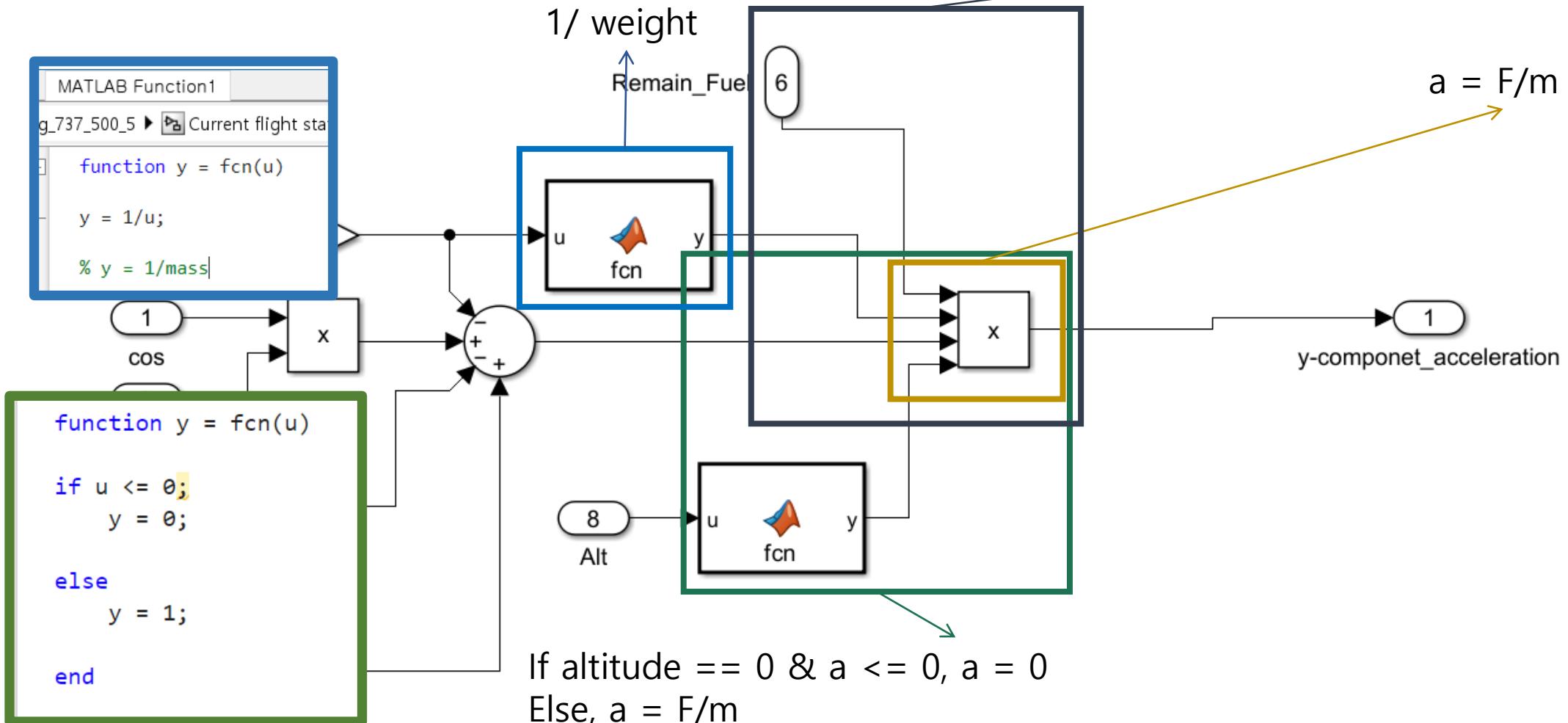
If remaining fuel is 0, input = 0, $a = 0$
 Else, Input = 1, $a=F/m$

y-component acceleration calculation sub-system



y-component acceleration calculation sub-system

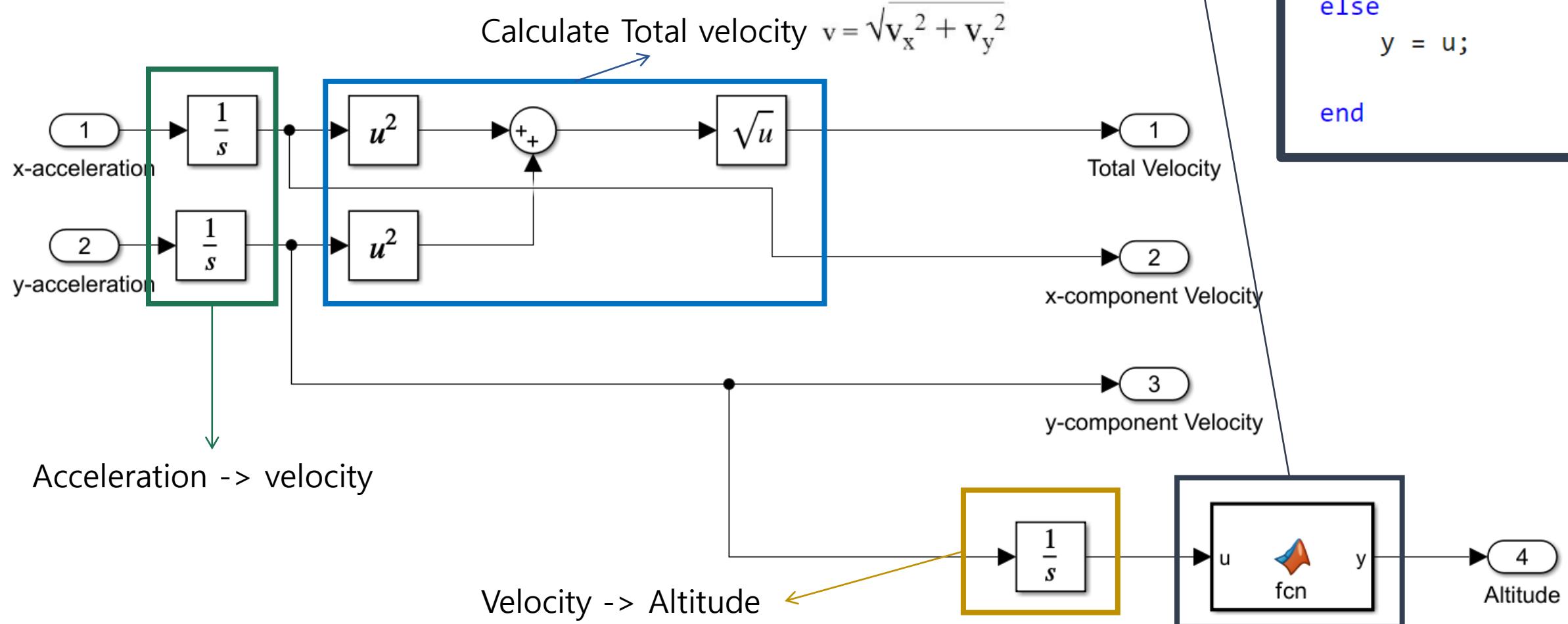
If remaining fuel ≤ 0 , input = 0, $a = 0$
 Else, Input = 1, $a = F/m$



With out this function, y-accel is negative when the altitude is 0. So, altitude will have a negative value.

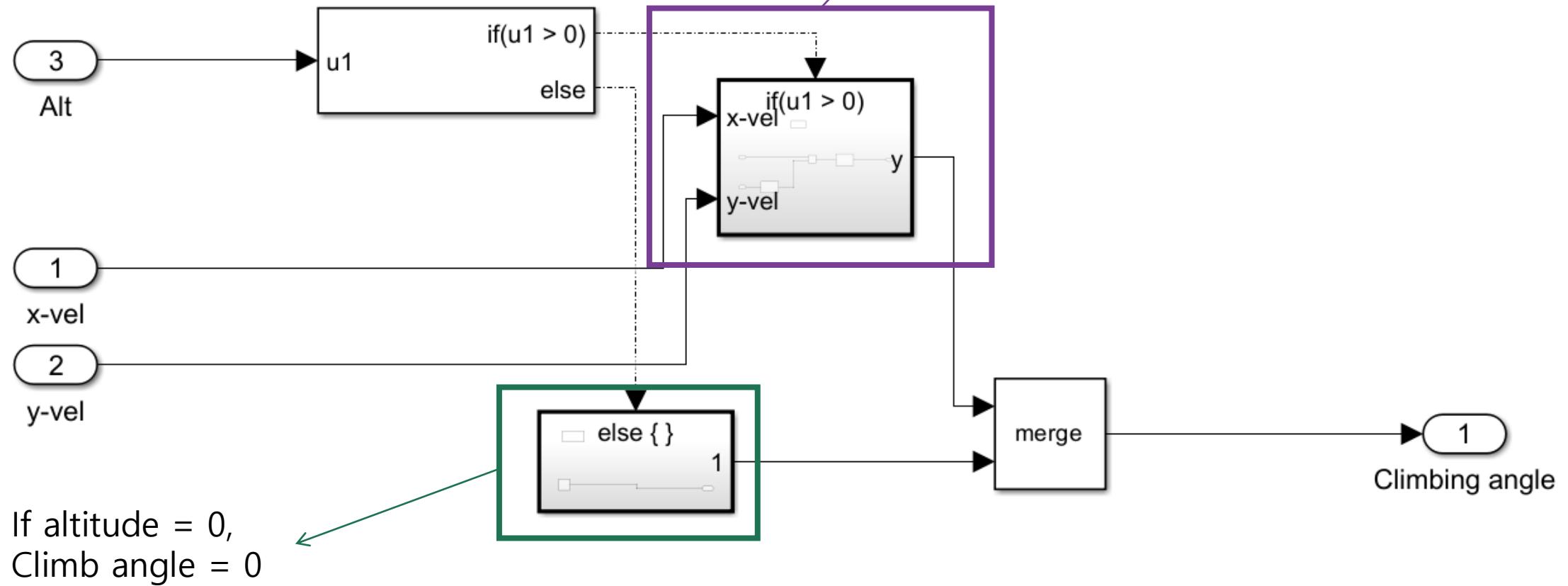
Velocity&Altitude

Velocity&Altitude

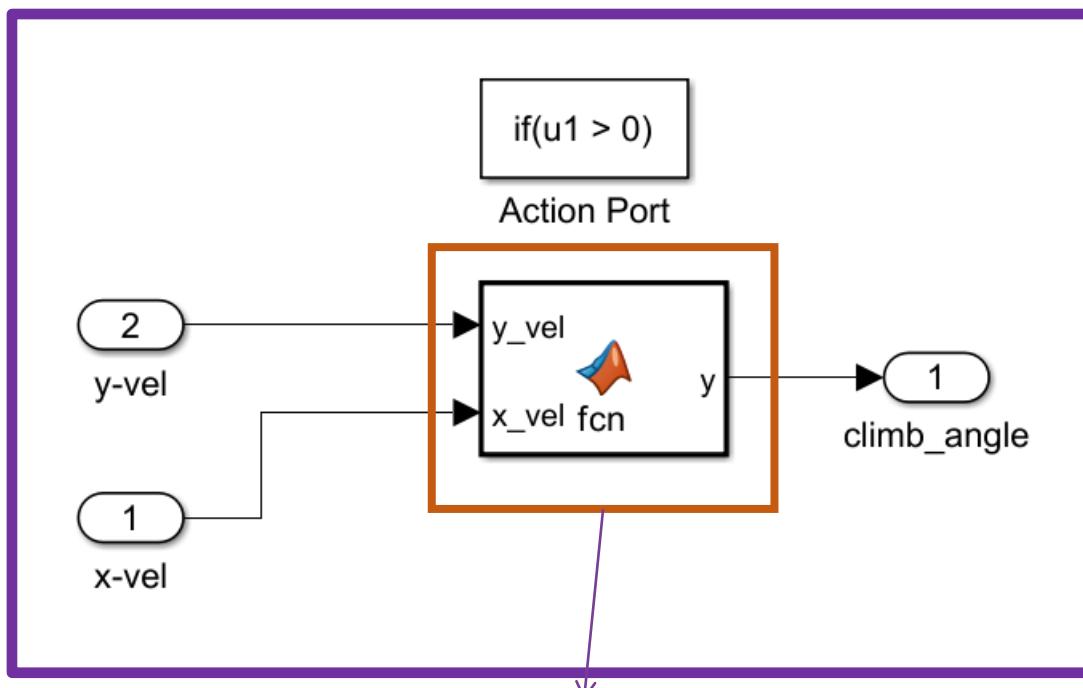


Climb Angle

Climb angle



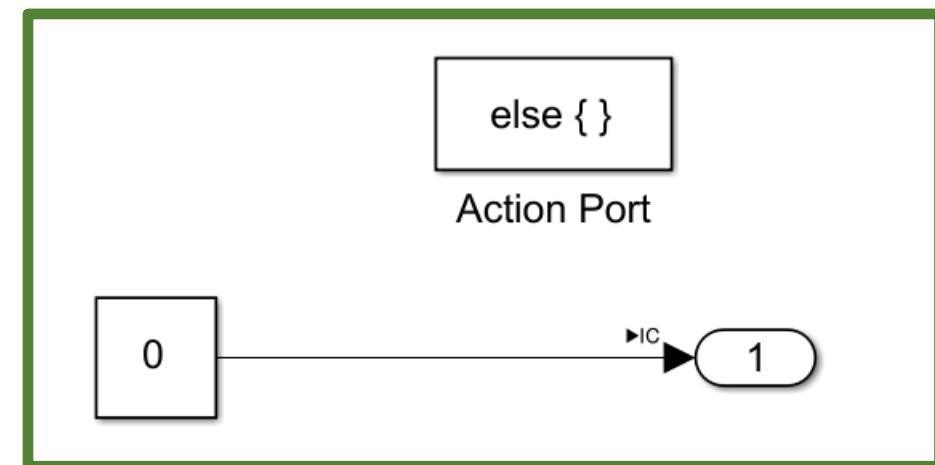
Climb angle



Calculate climb angle

```
function y = fcn(y_vel, x_vel)
u = y_vel/x_vel;
y = atan(u);
```

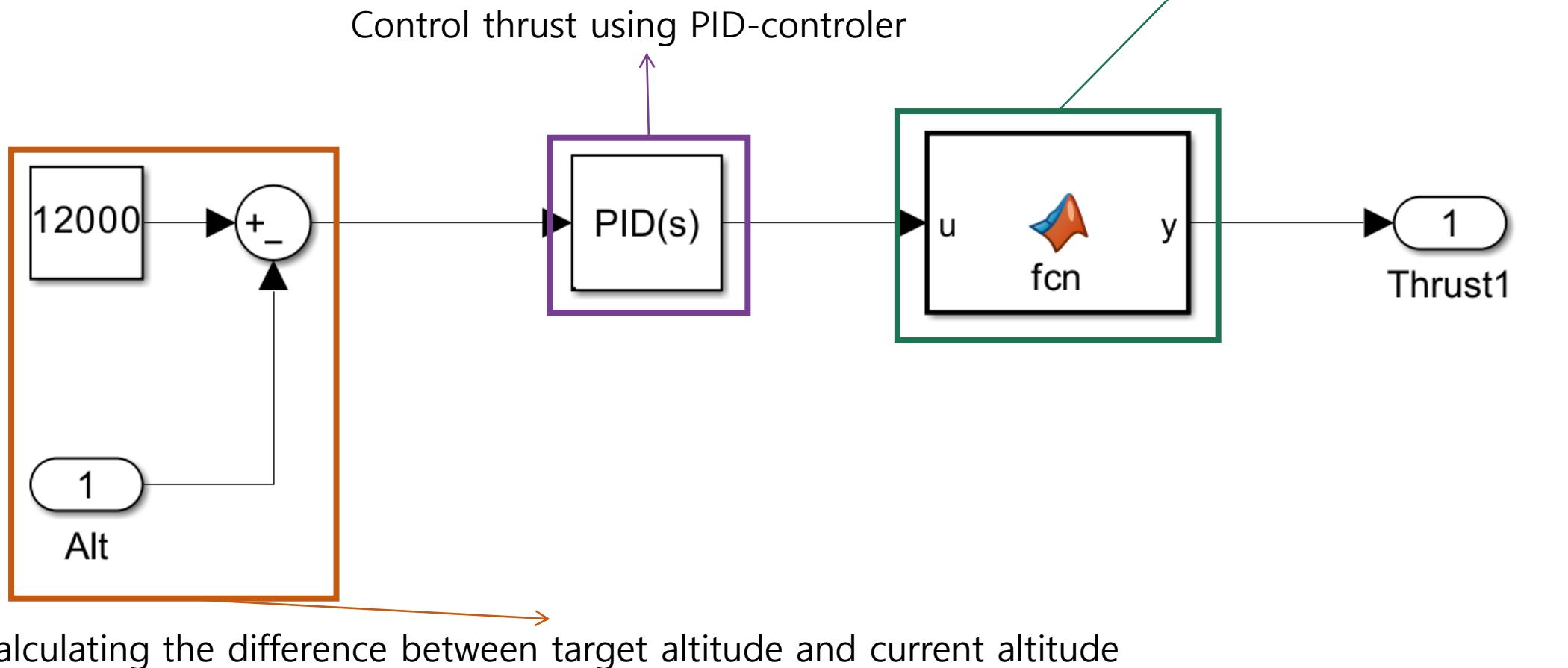
By using this function, we can align aircraft axis and aerodyn. axis



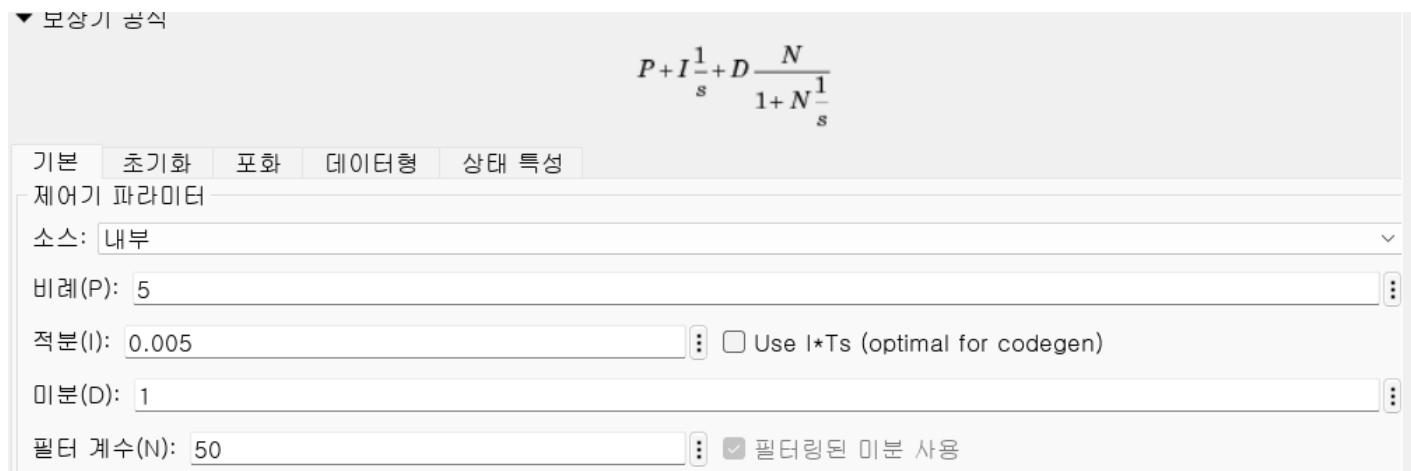
Calculate climb angle

Thrust Control System

Thrust control system



Thrust control system



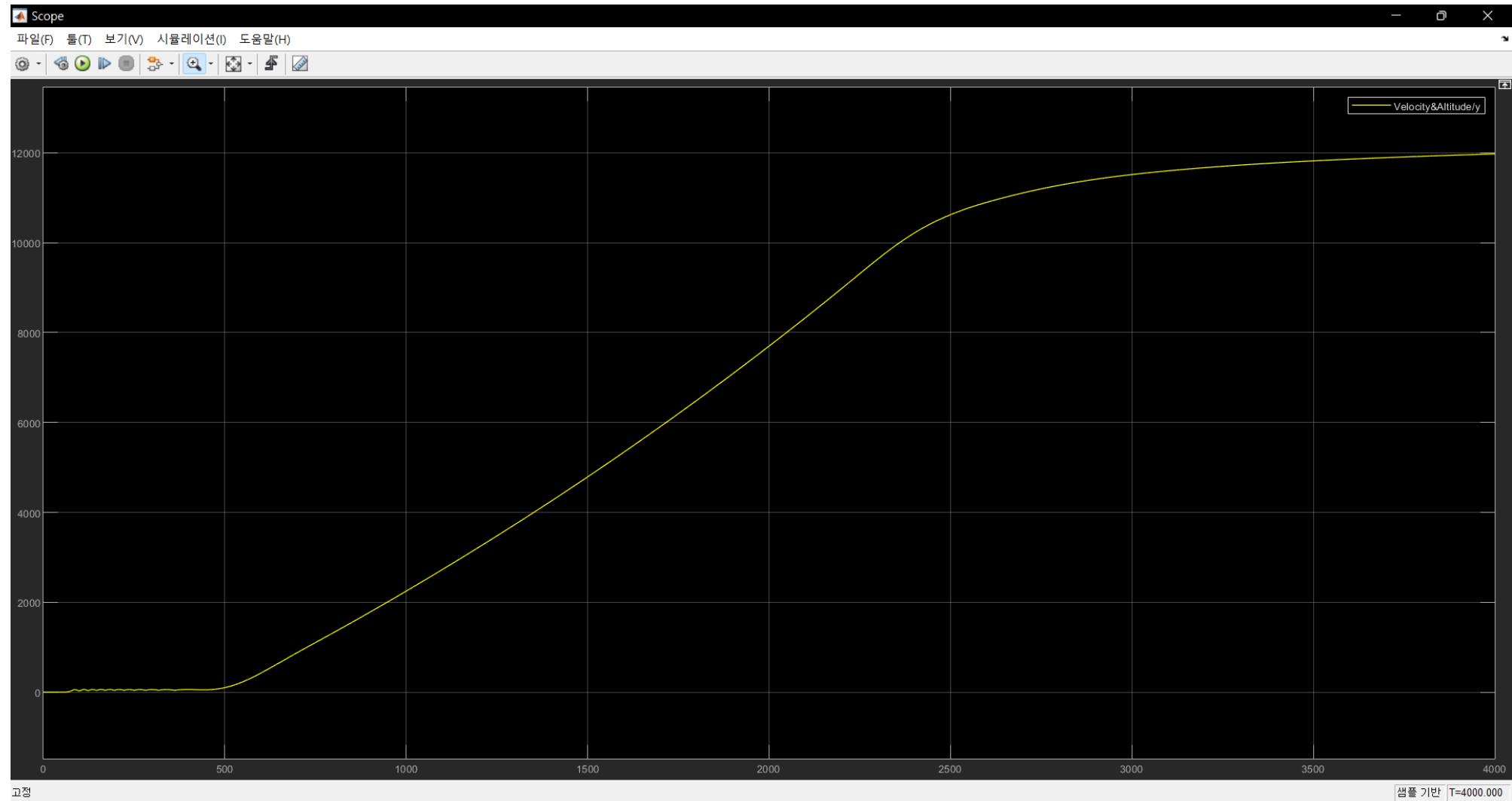
After trial and error, we adjusted the gain values.

the max thrust of the engine = 82.3kN

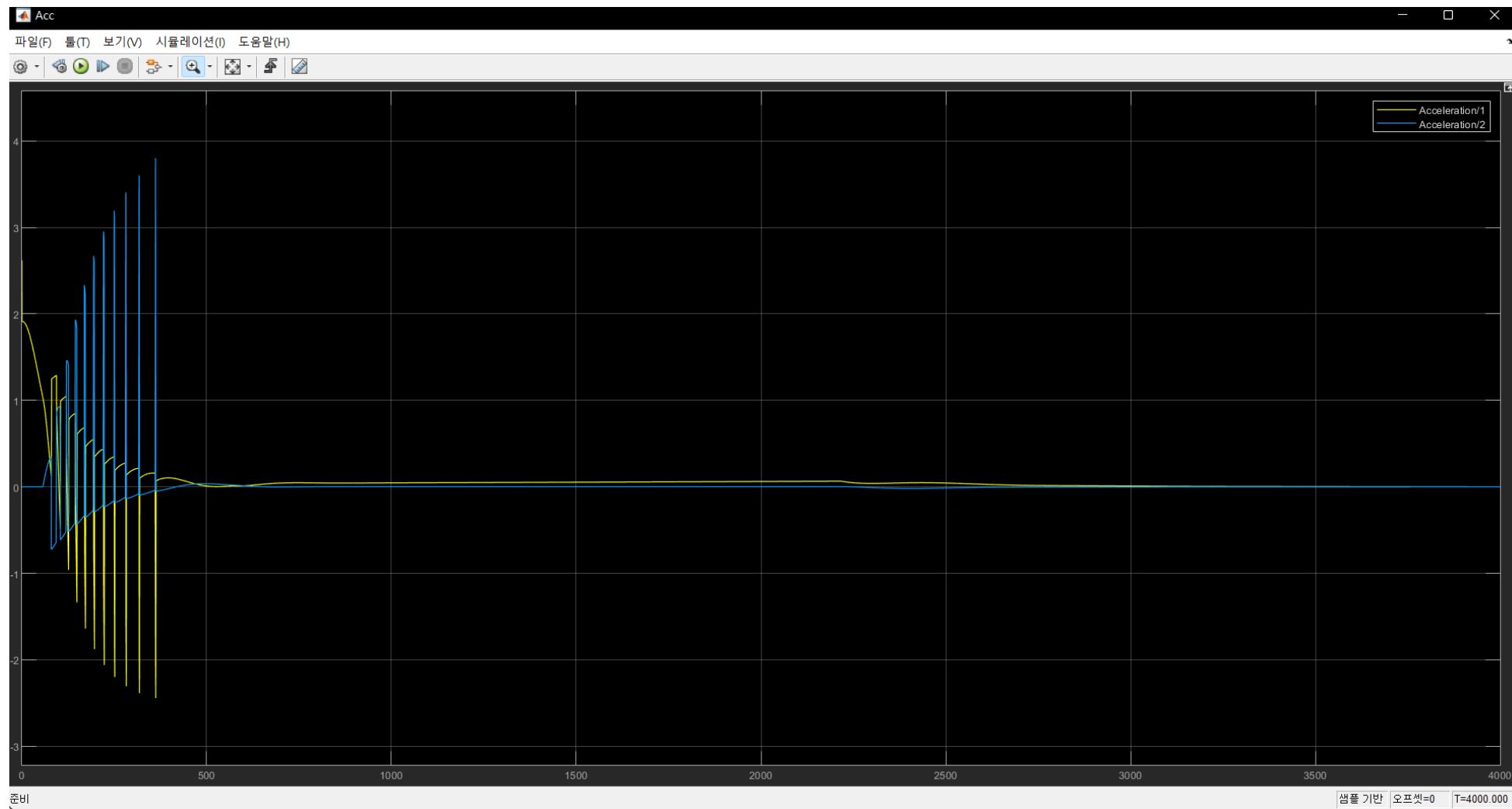
```
function y = fcn(u)  
  
if u <= 82300  
    y = u;  
  
else  
    y = 82300;  
end
```

Simulation

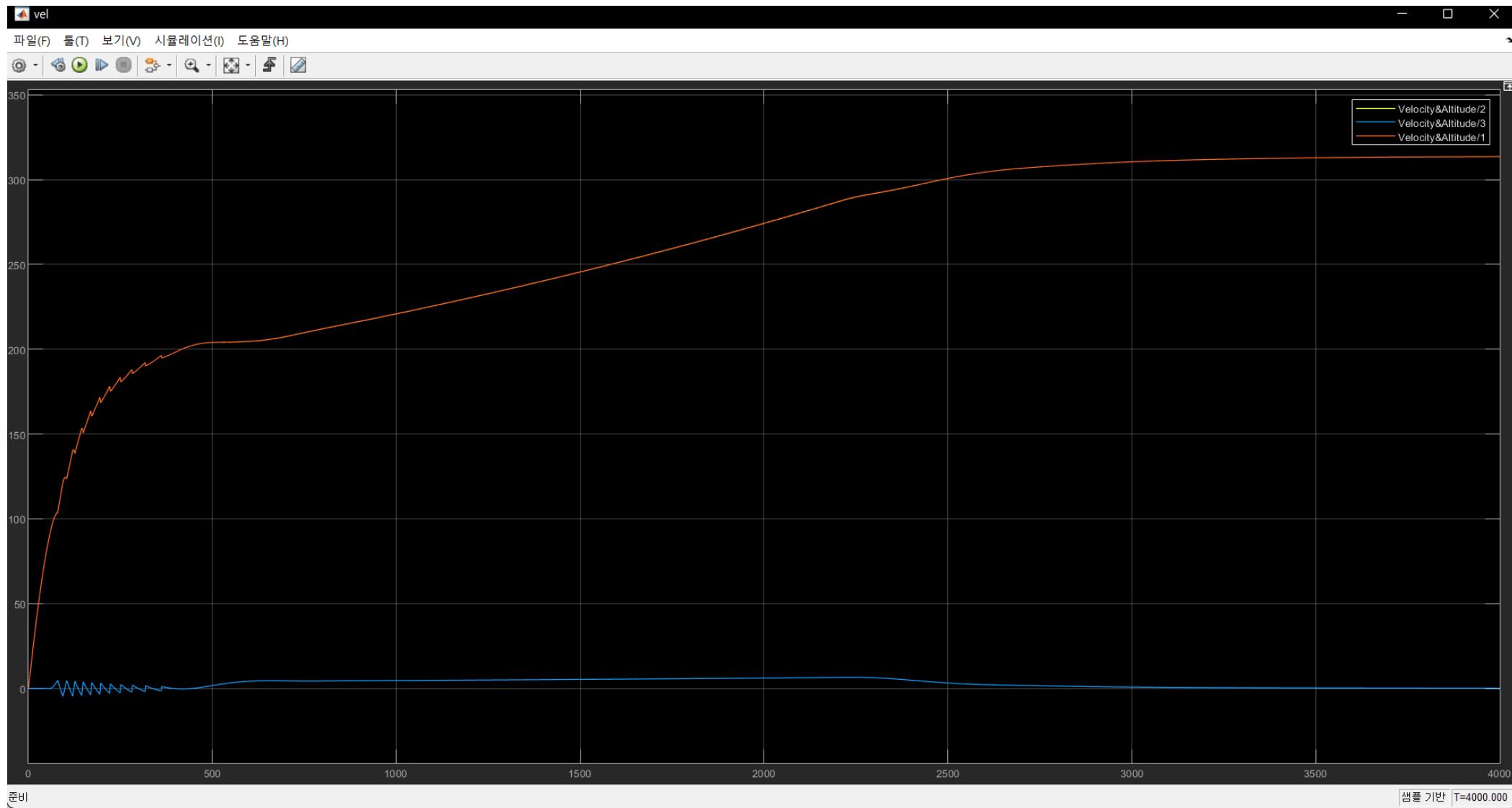
Altitude



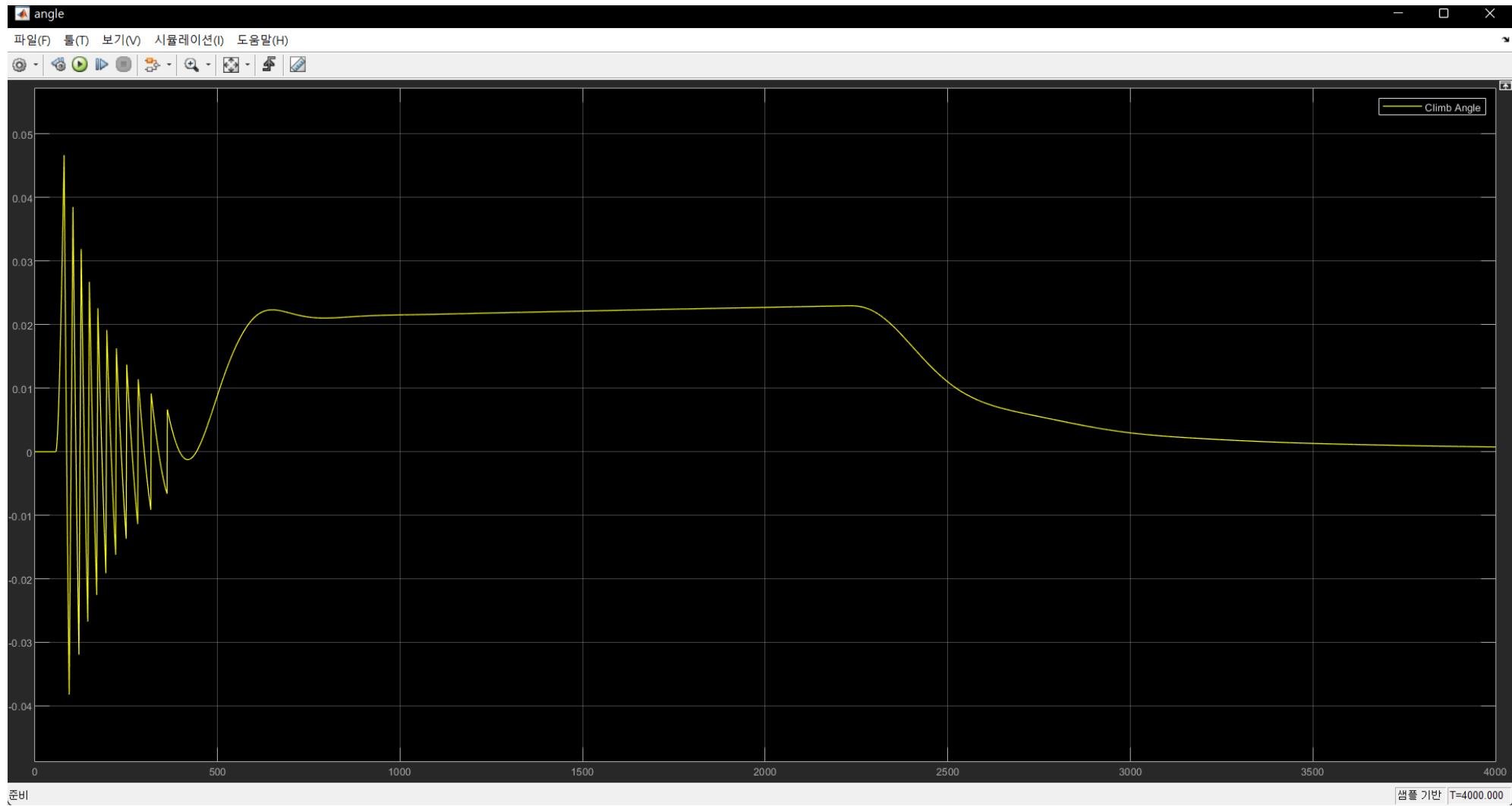
Acceleration



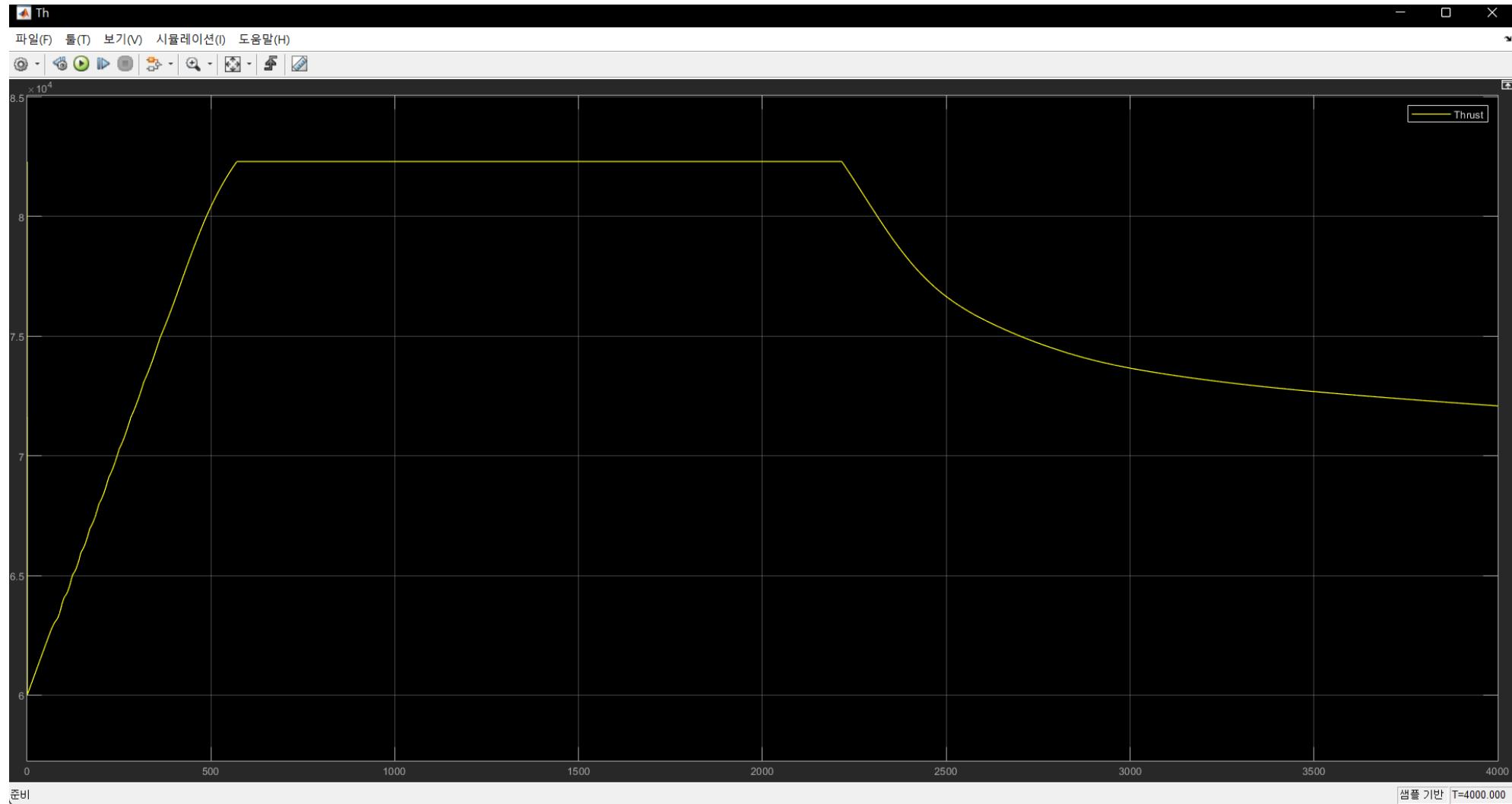
Velocity



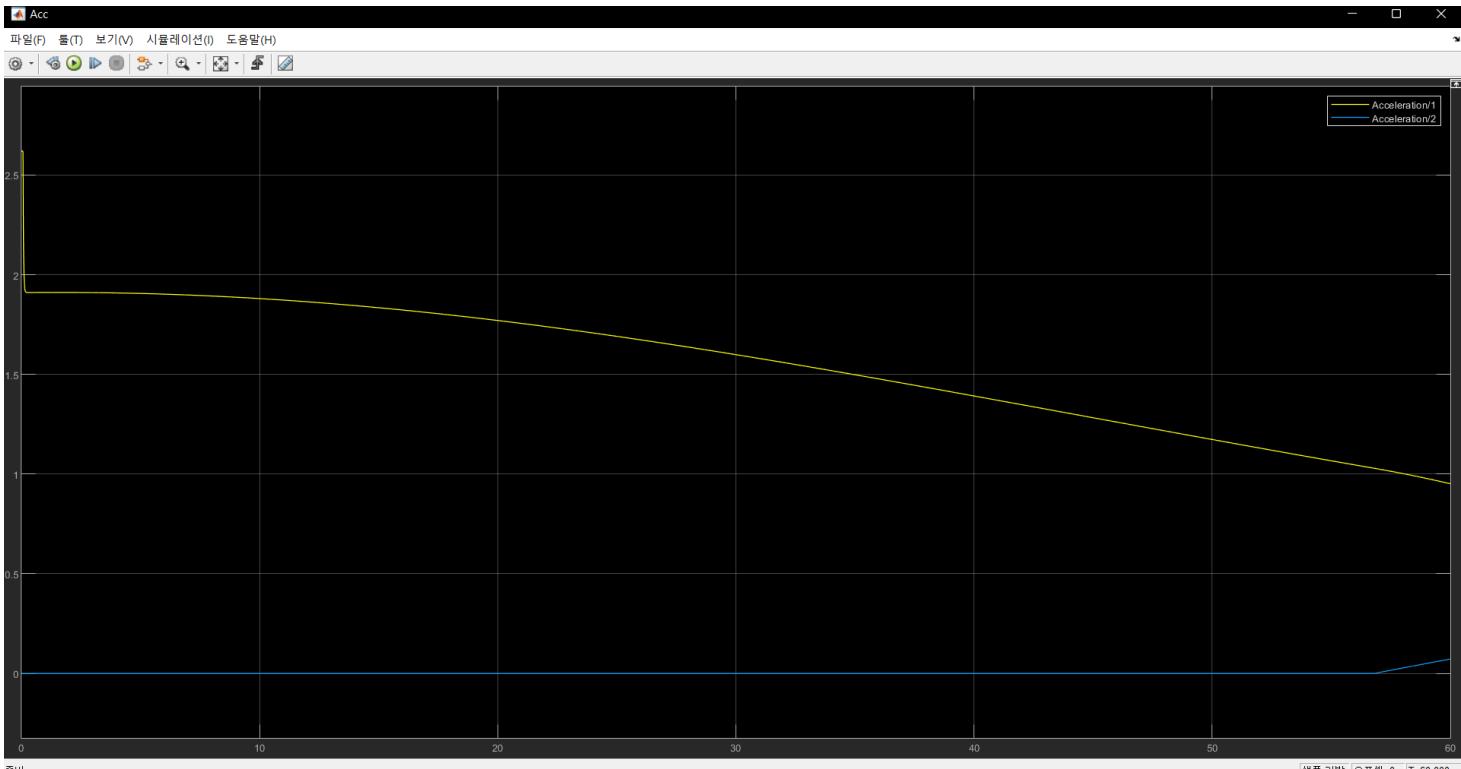
Climb Angle



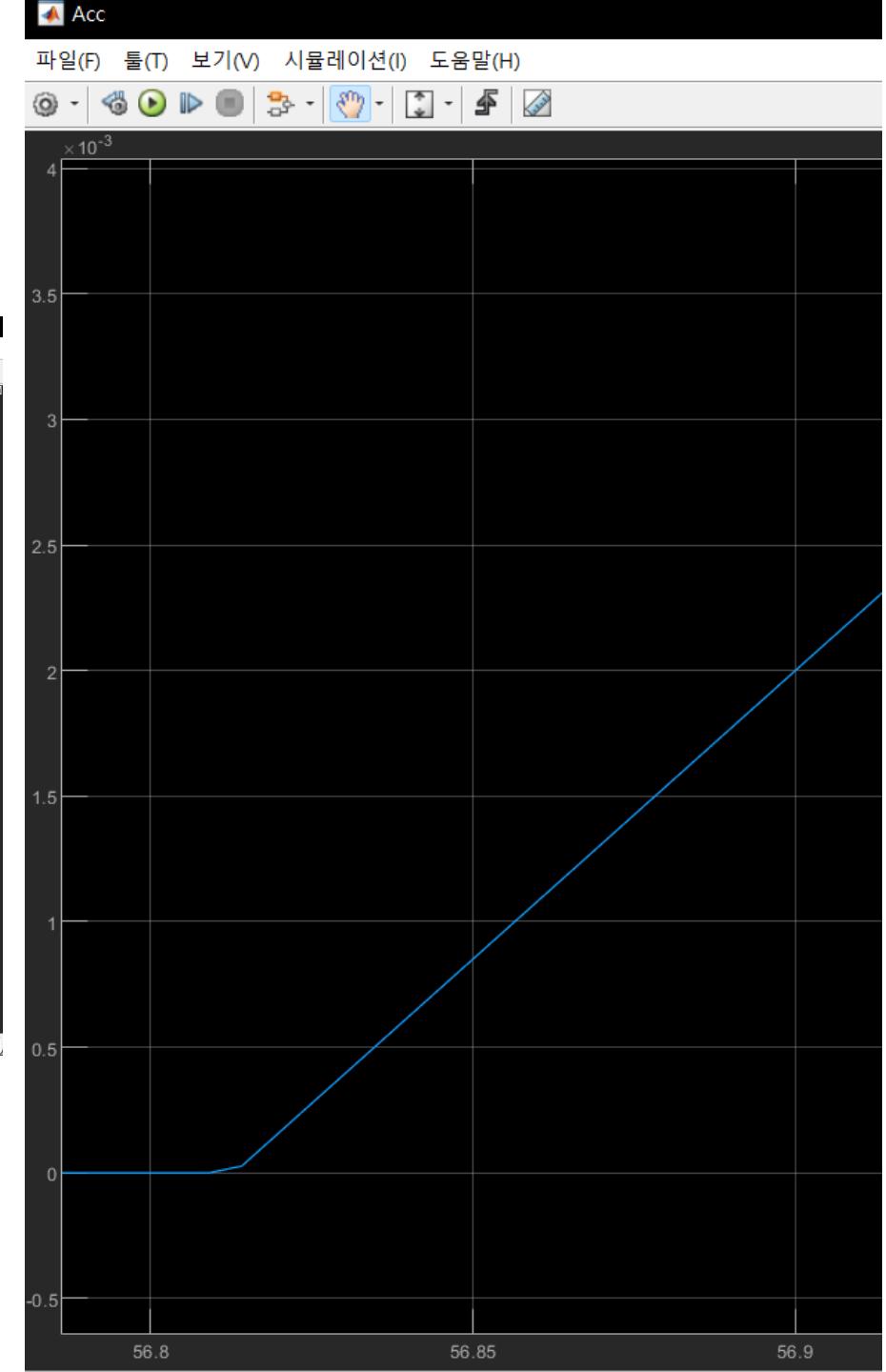
Thrust



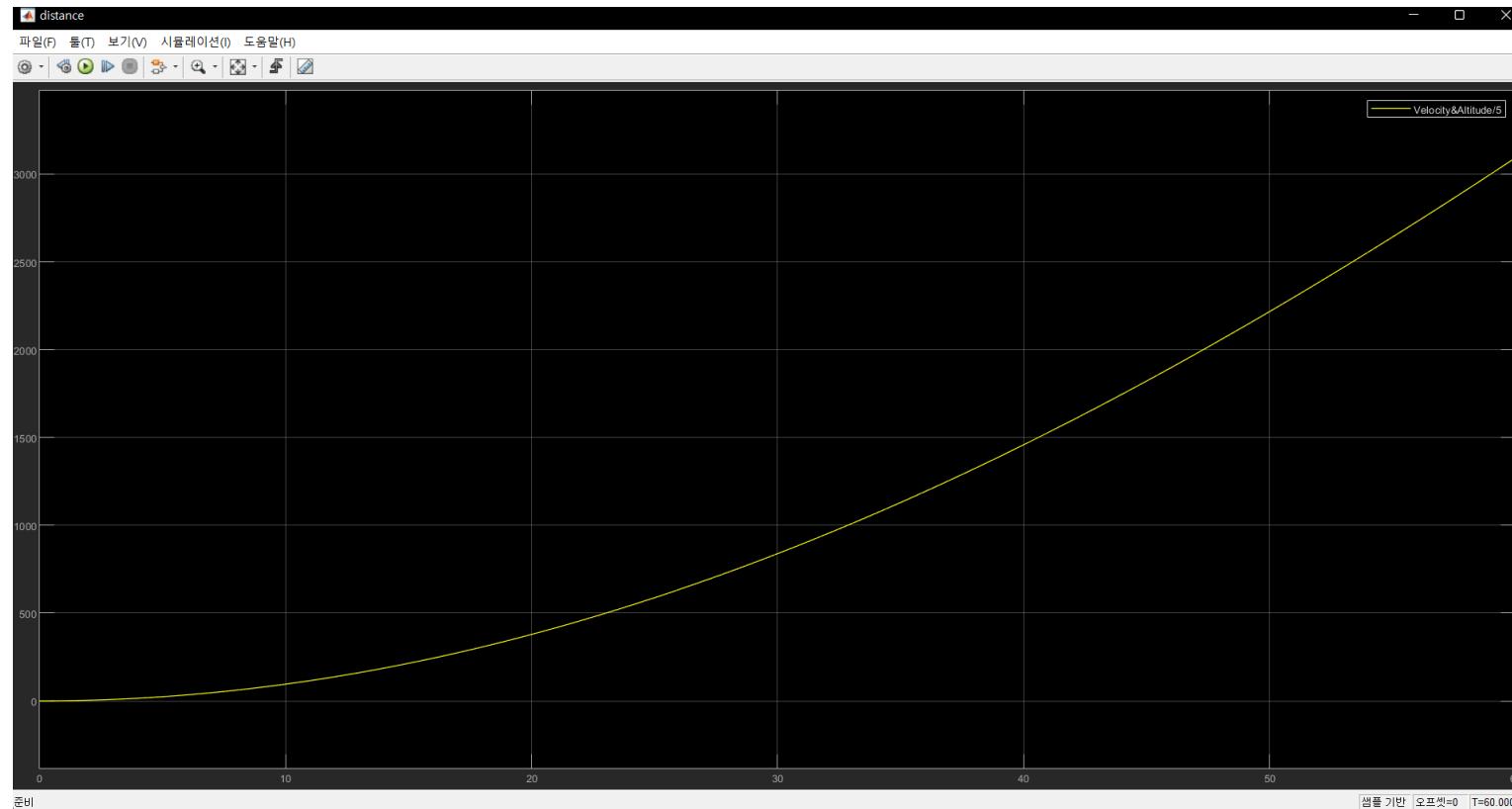
Take-off Time



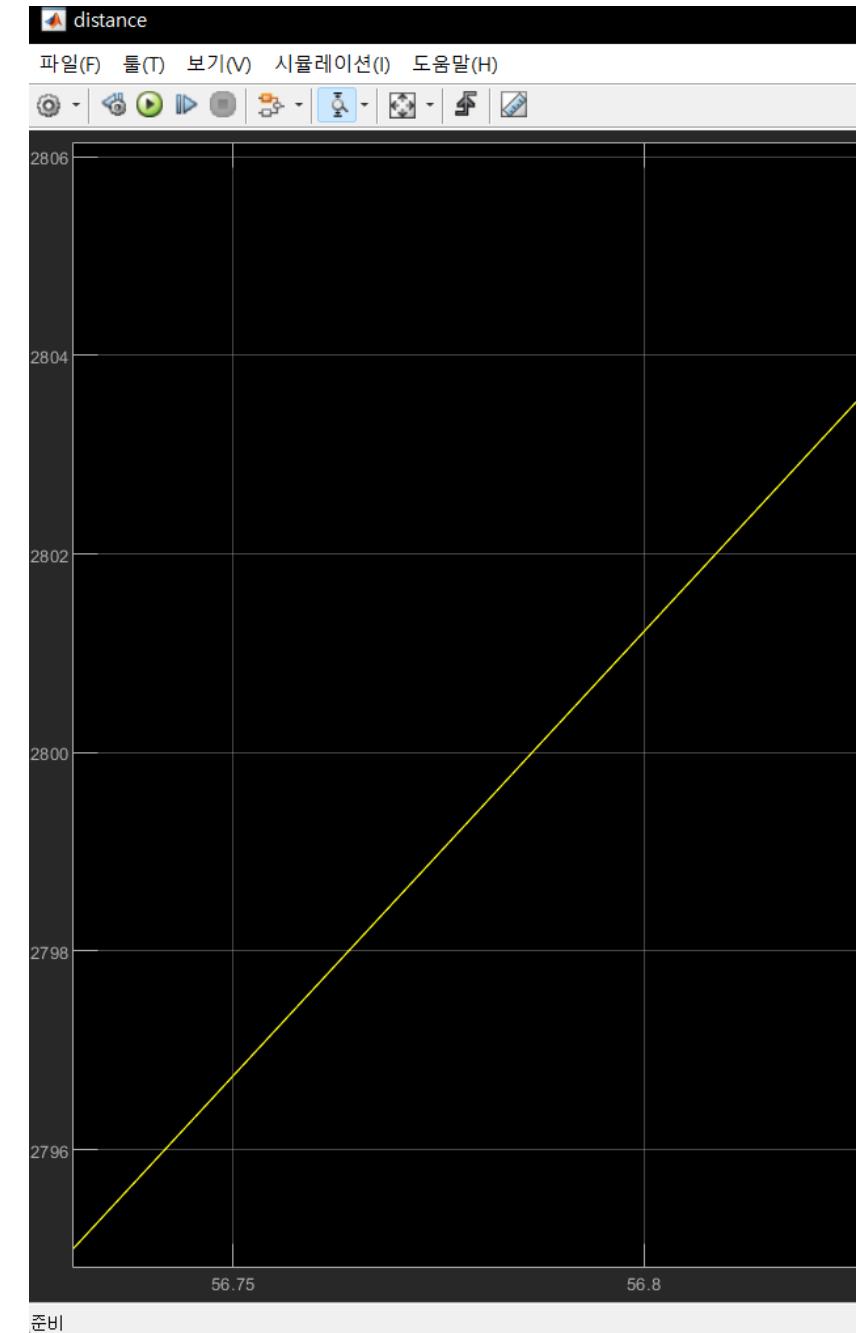
About 56.8 sec



Take-off distance

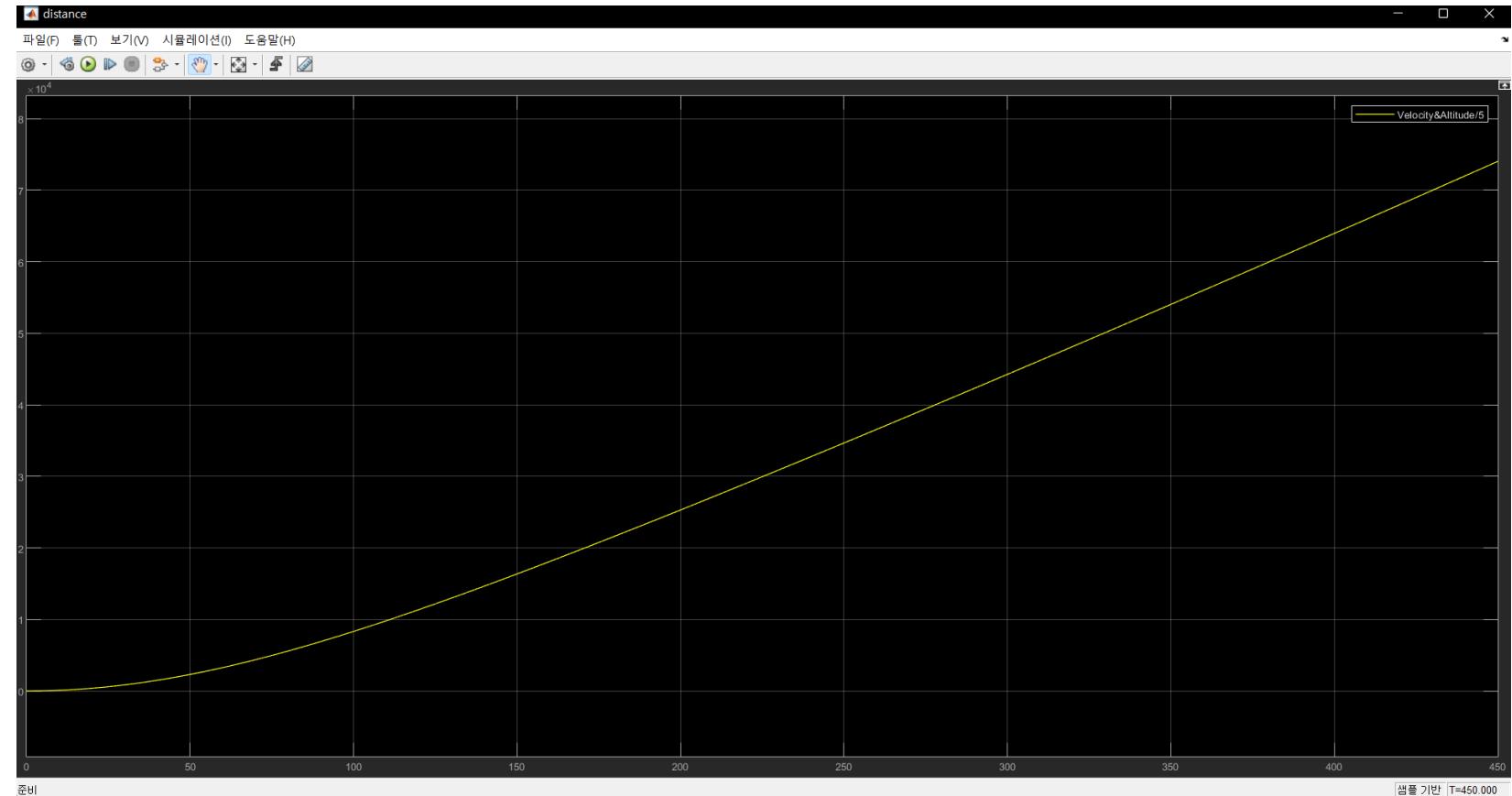


About 2801m

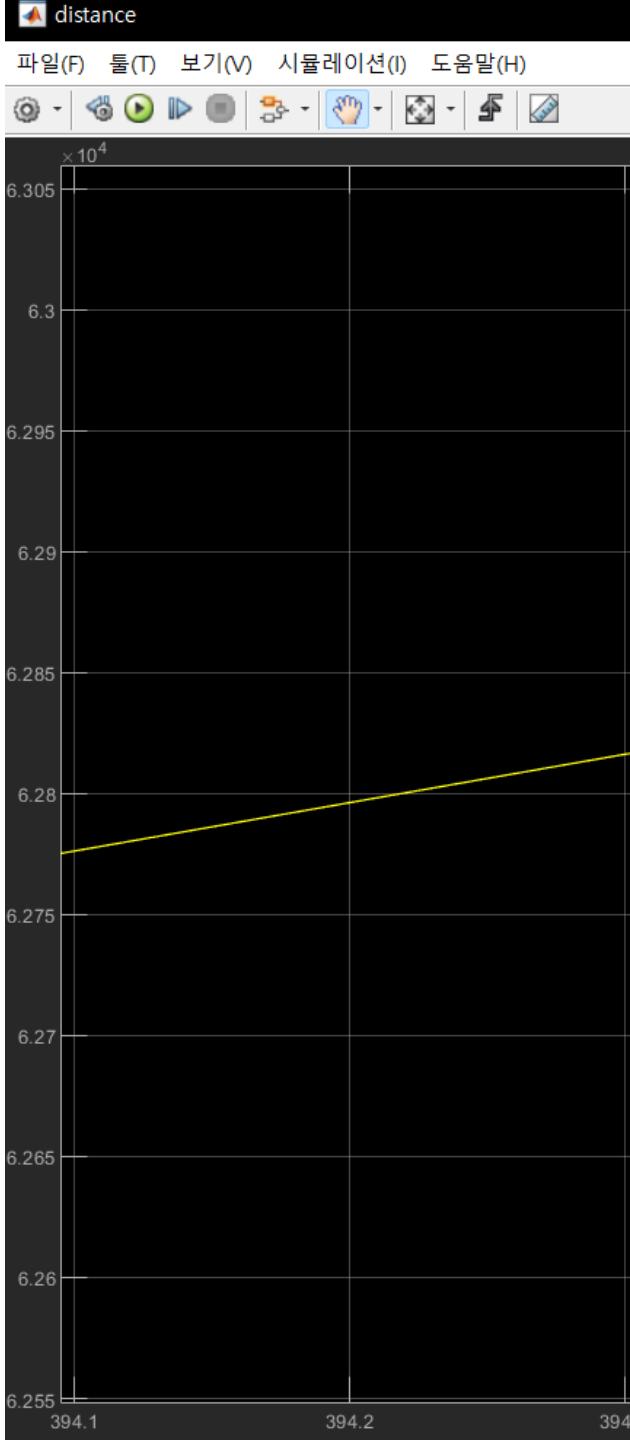


Comparison between “With slat&flap” and “No slat&Flap”

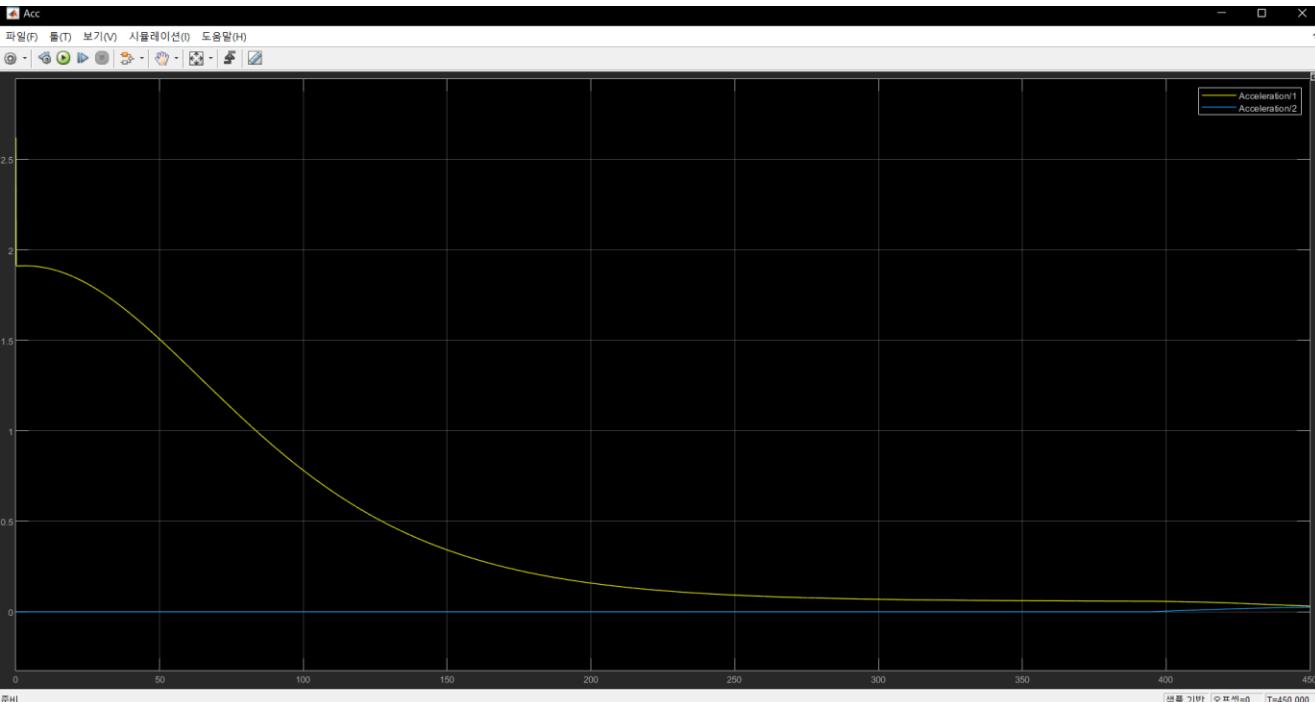
Take-off distance



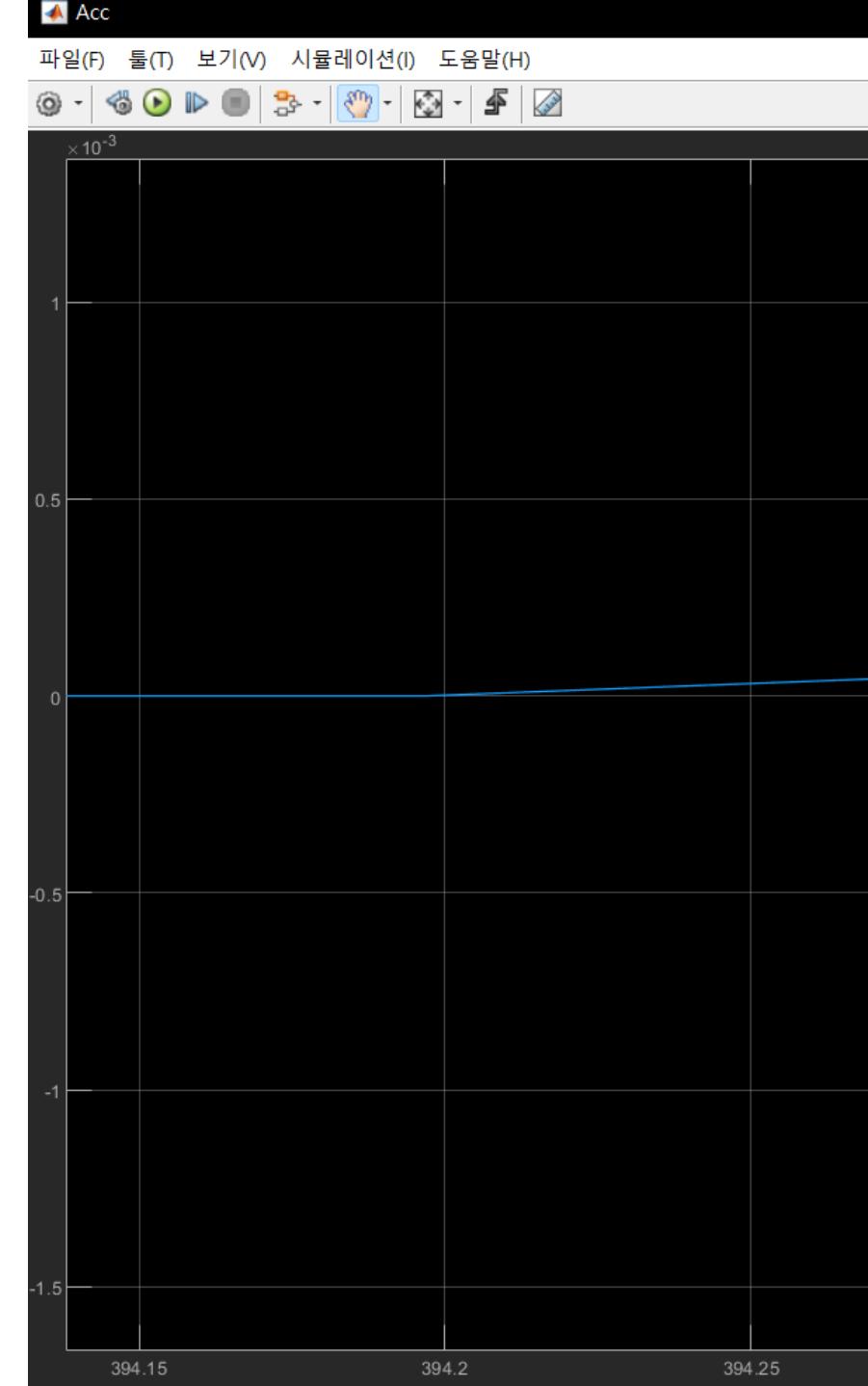
About 62800m >>>>>> 2801m



Take-off Time

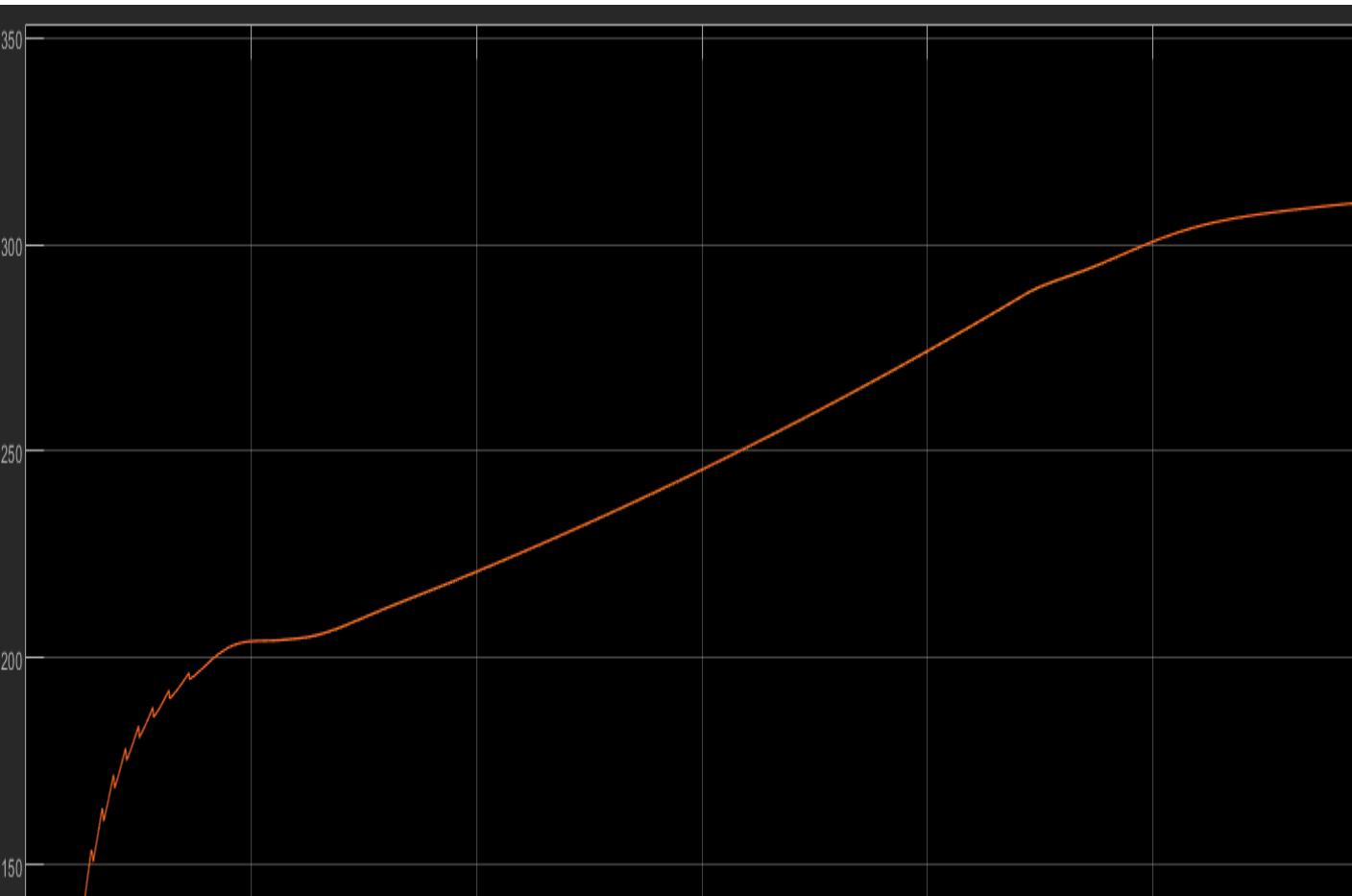


About 394.2 sec >>>>> 56.8 sec



Improvements

Climb angle control

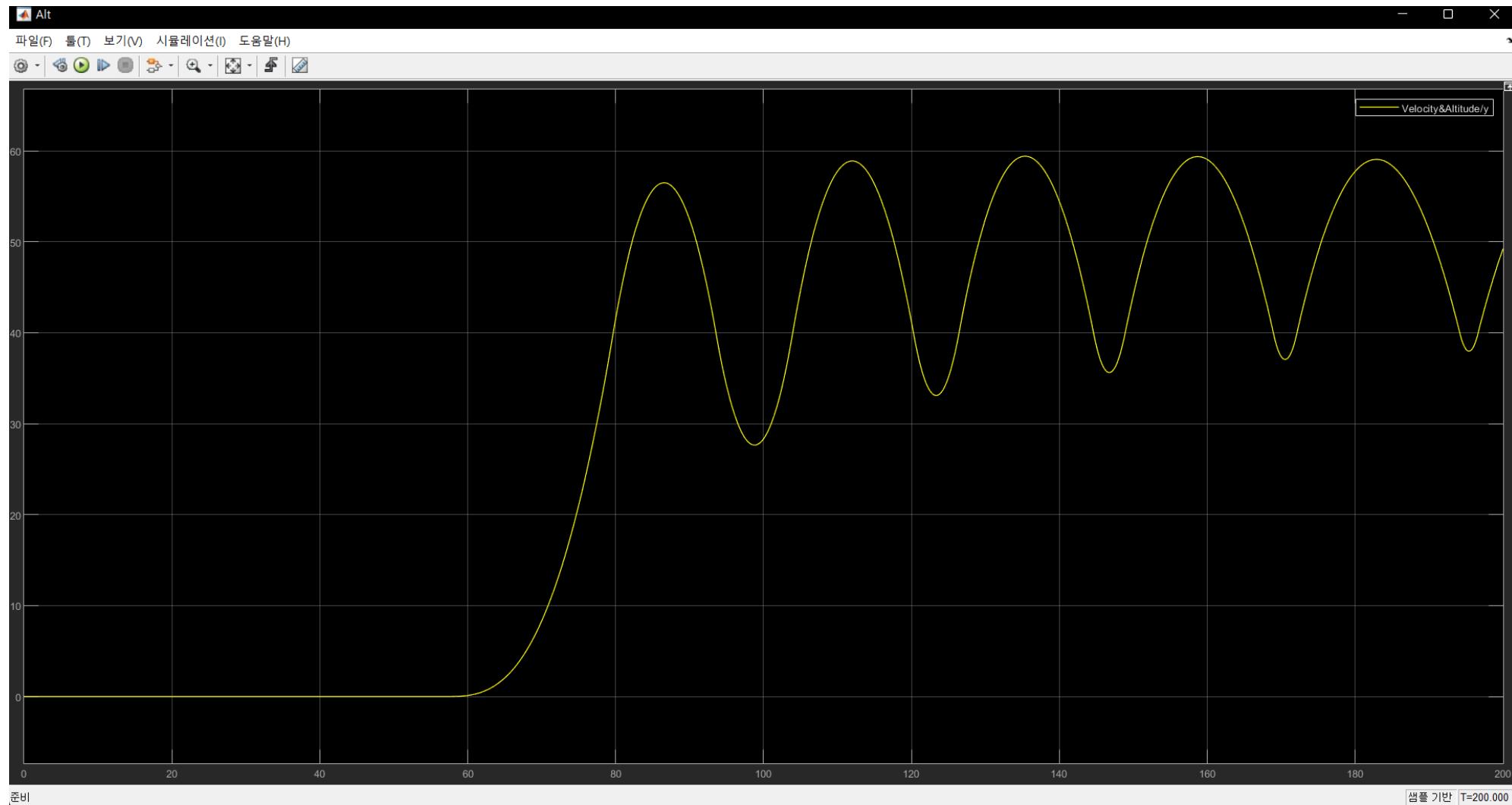


다음 그래프는 시간에 따른 속도 그래프인데, 속도가 300m/s를 넘는 것을 볼 수 있다. 비행기의 순항 속도가 보통 216m/s인 것을 감안하면 매우 빠른 속도이다.

원인은 비행기의 각도 제어가 들어가 있지 않아 오로지 추력으로만 고도를 조절하기 때문이다. 비행기의 각도 제어를 한다면 원하는 속도로 고도를 유지하는 것이 가능할 것이다. 다만 수많은 AoA에 대한 Cl&Cd 값이 필요할 것이다.

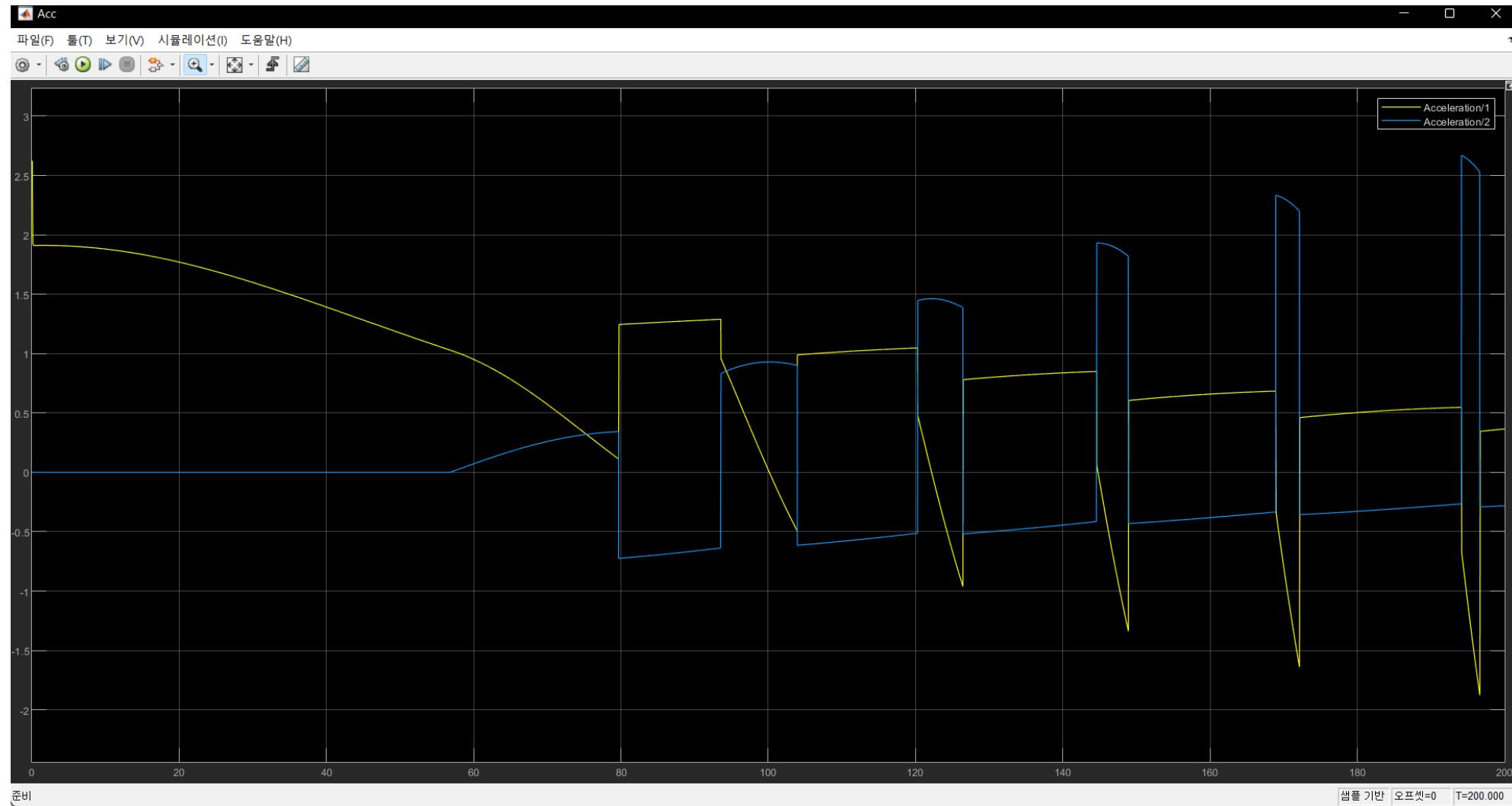
Altitude

Various slat and flap angles



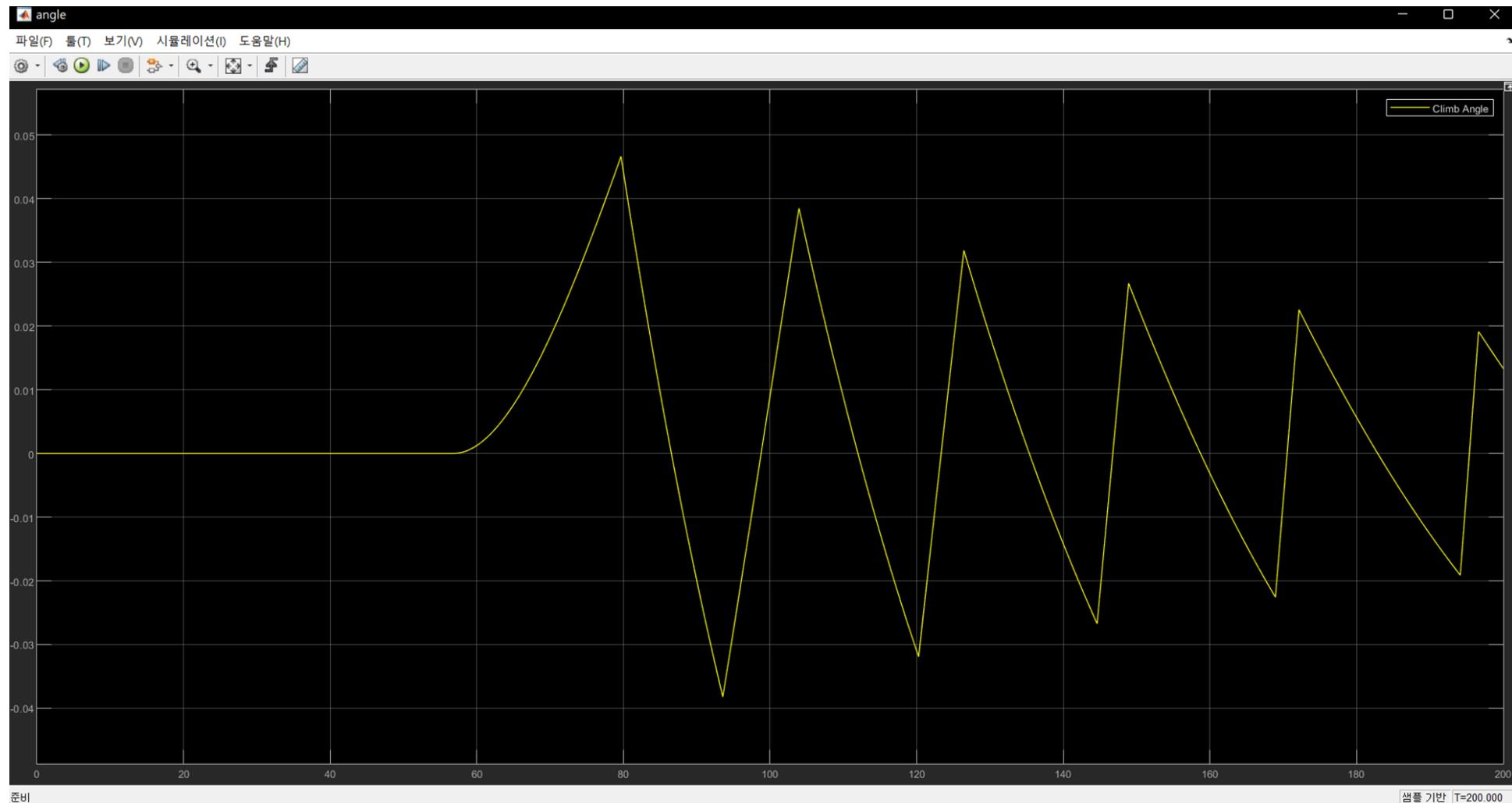
Accerlation

Various slat and flap angles



Climb angle

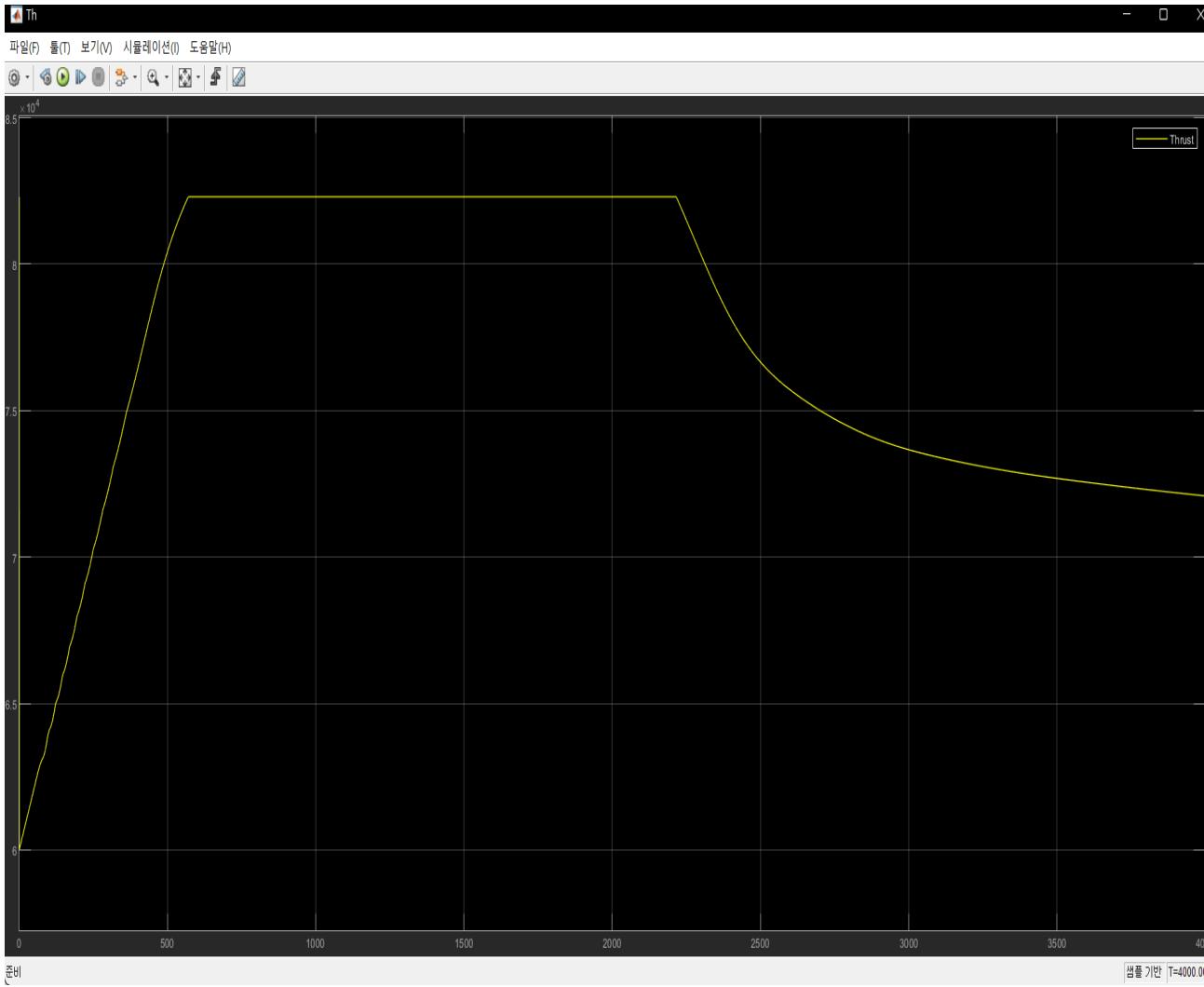
Various slat and flap angles



Various slat and flap angles

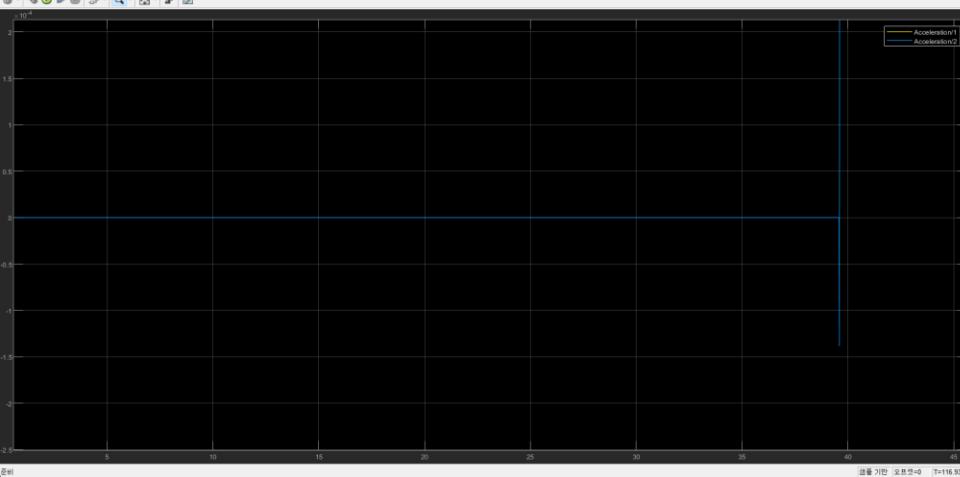
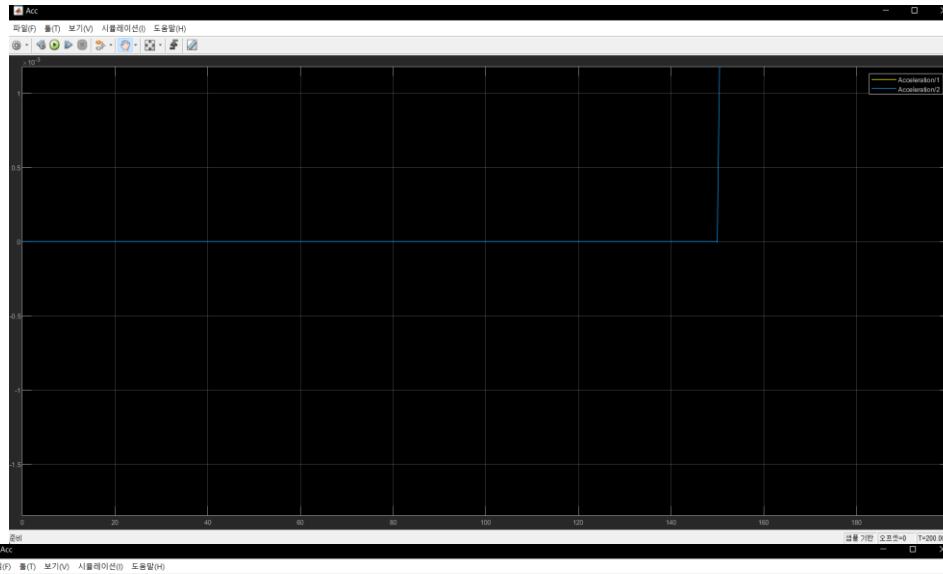
Slat&flap이 접힐 때 갑자기 접히기 때문에 Lift와 Drag의 값이 급격하게 변화하고 이에 따라 심한 진동이 발생한다. 이는 세분화된 slat&flap 별 Lift와 Drag의 값을 알 수 있다면 해소될 수 있는 문제라고 생각한다.

More accurate control system



초반 최대 추력으로 빠르게 속도를 올린 후 이륙 해야하지만 PID 제어의 한계로 초반에 추력을 최대로 쓰지 않아 이륙 시간과 거리가 증가하게 되었다.

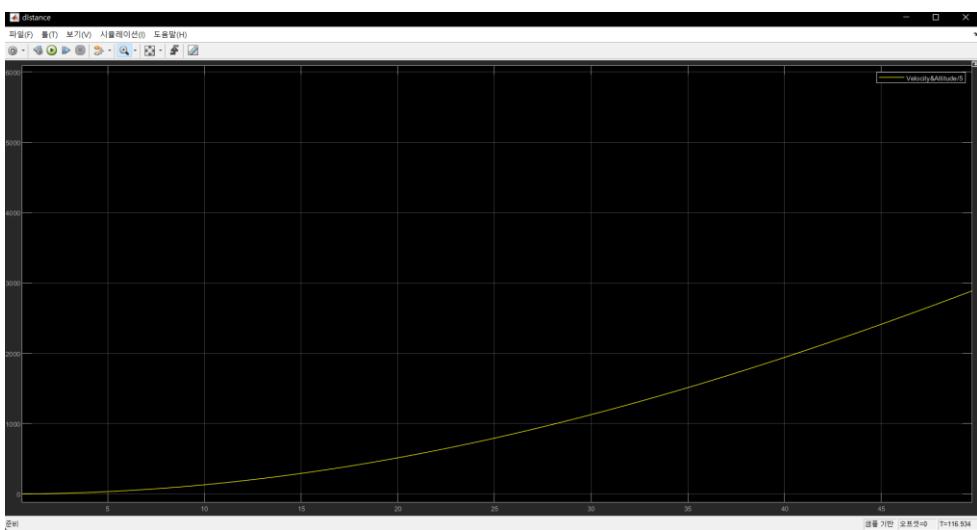
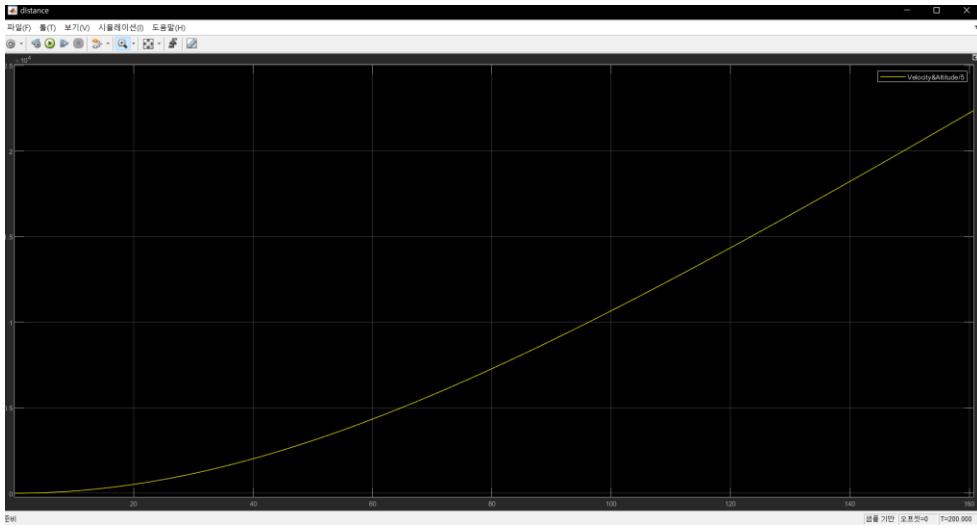
More accurate control system



실재로 추력을 82.3kN인 상수로 대입한 경우

Slat&flap이 접힌 상태는 150초에서,
펼쳐진 상태에선 39.6초에 이뤄했으며

More accurate control system



실재로 추력을 82.3kN인 상수로 대입한 경우

Slat&flap이 접힌 상태는 약 20000m에서,
펼쳐진 상태에선 1700m만에 이륙했다.

References

References

<https://m-selig.ae.illinois.edu/ads/aircraft.html#conventional>
-Airfoil-information

<http://www.b737.org.uk/techspecsDetailed.htm>
-Boeing 737-500 Detailed Technical Data

https://www.boeing.com/resources/boeingdotcom/company/about_bca/startup/pdf/historical/737-classic-passenger.pdf
-Boeing 737-500 official brochure