



# Banned Technology

CAE CHAMPION

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**1**

FRICS

**2**

Full-Car  
Model

**3**

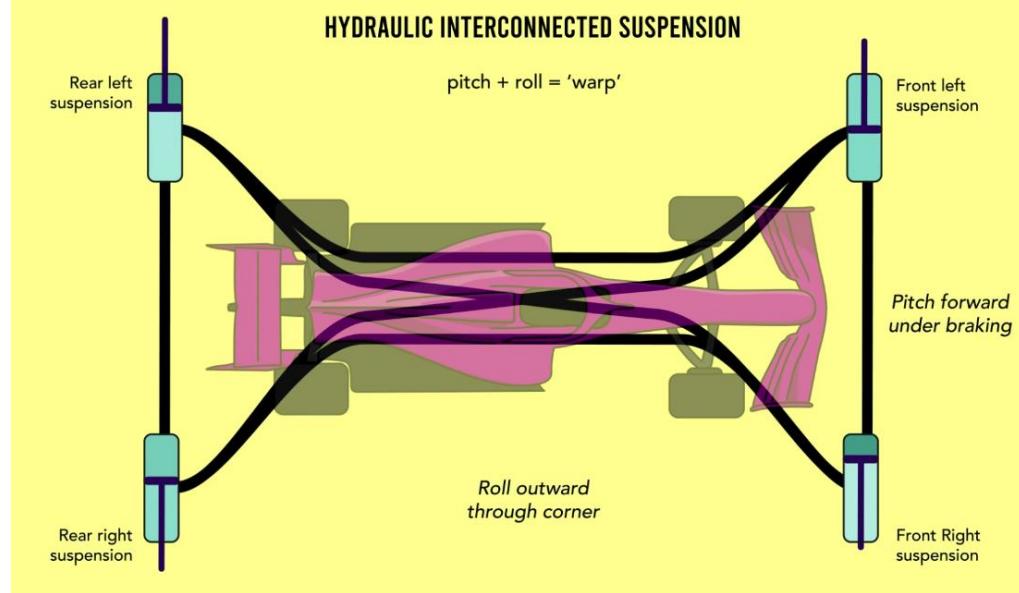
Mass-Damper

**4**

AeroDynamics

**5**

Difficulties  
&  
Reflections



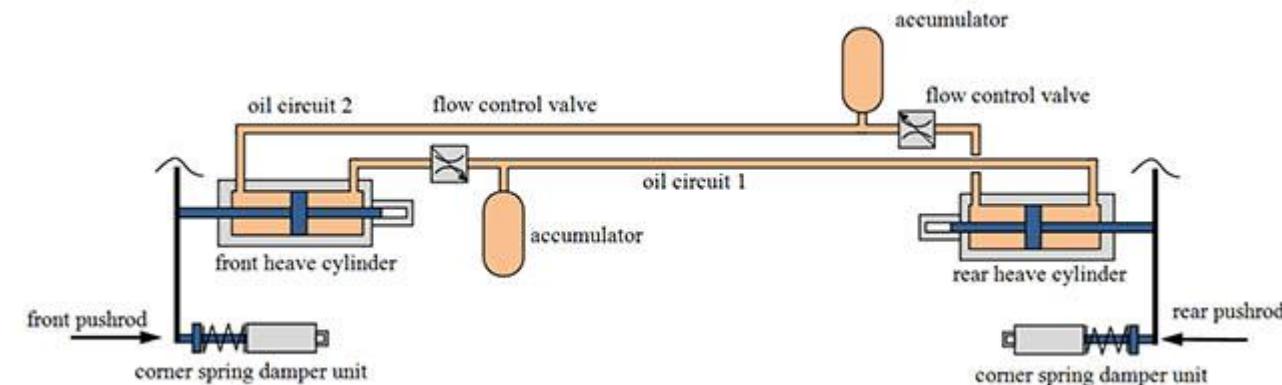
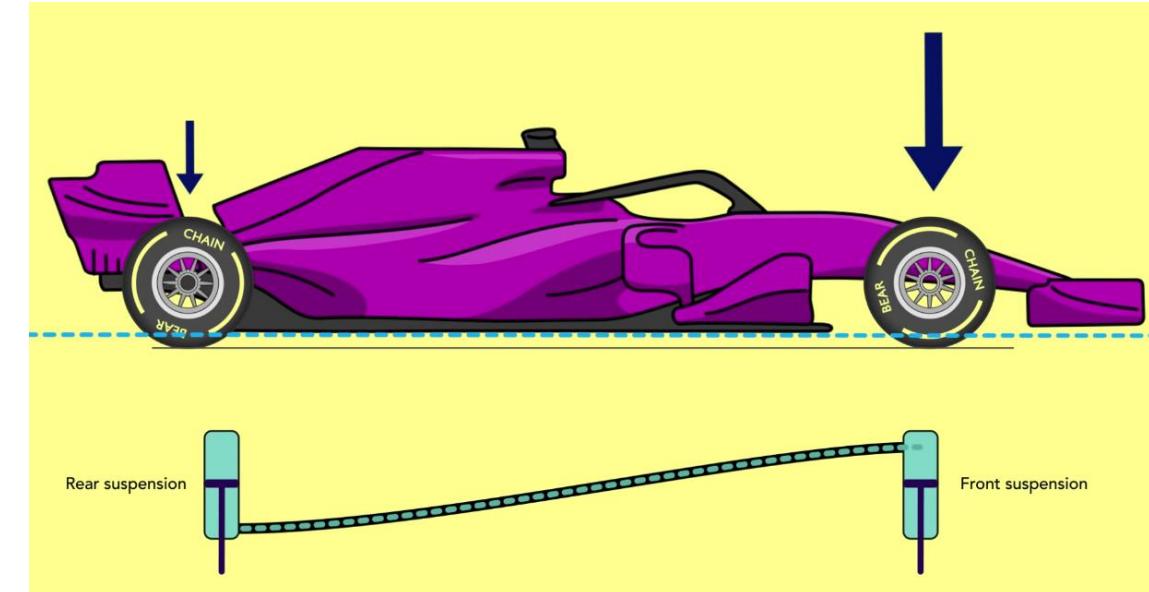
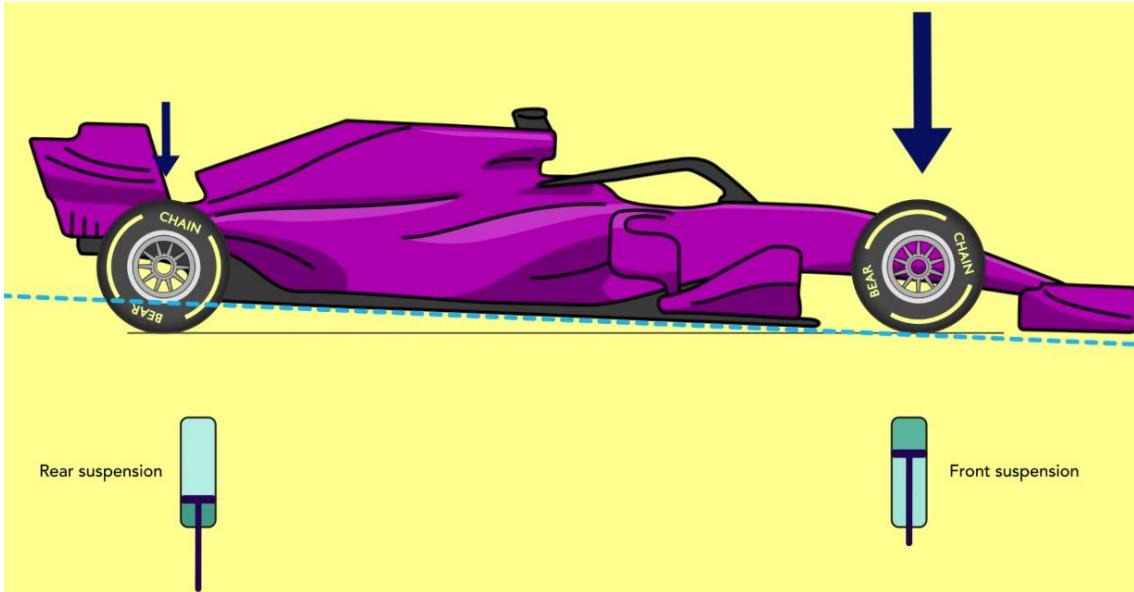
1

# FRICS

**Front and Rear InterConnected Suspension**

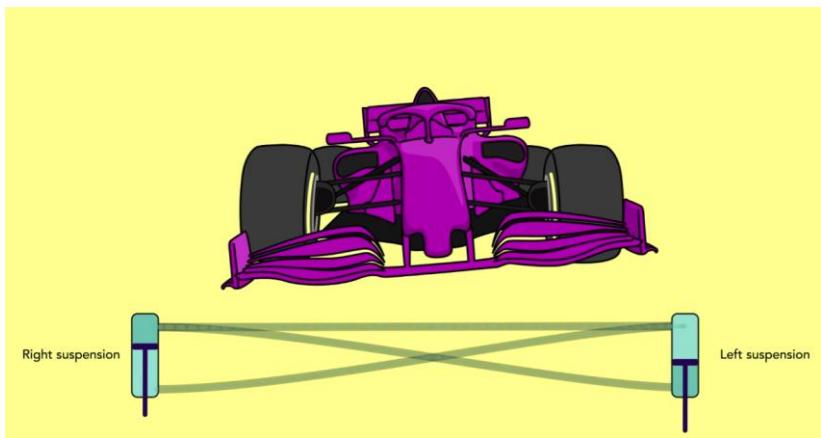
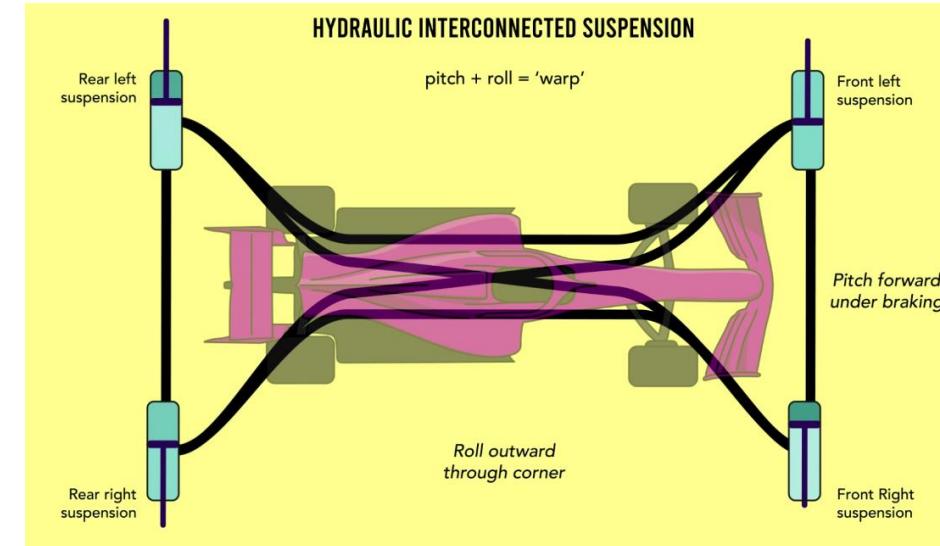
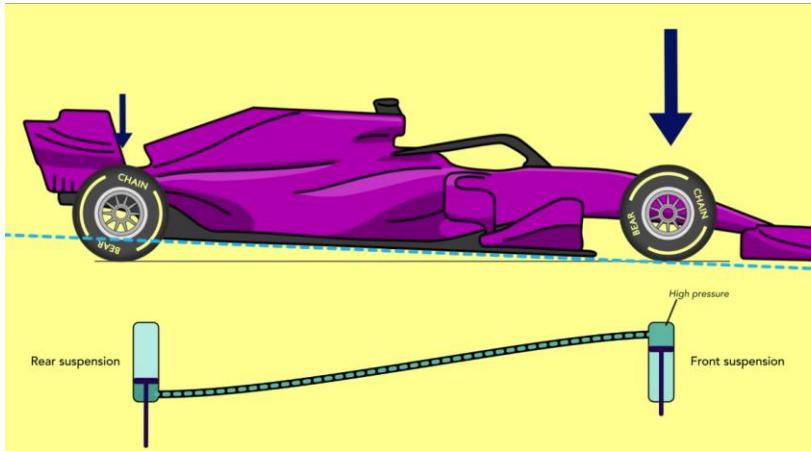
## 1

# FRICS: Front and Rear Interconnected Suspension



## 1

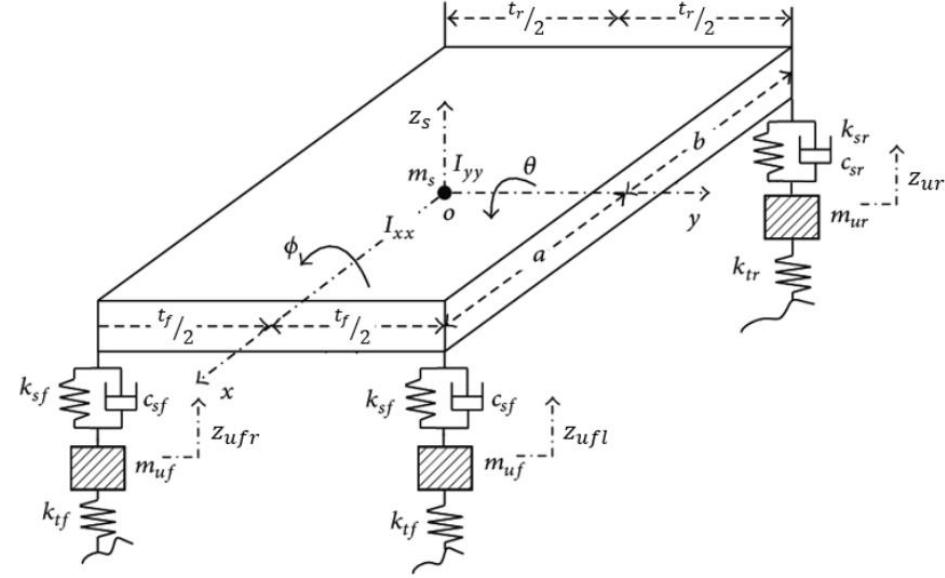
# FRICS: Front and Rear Interconnected Suspension



전방과 후방 서스펜션의 움직임을 상호 연계

주행 중 차량의 자세, 각도의 흔들림을 최소화, 균형 있게 유지

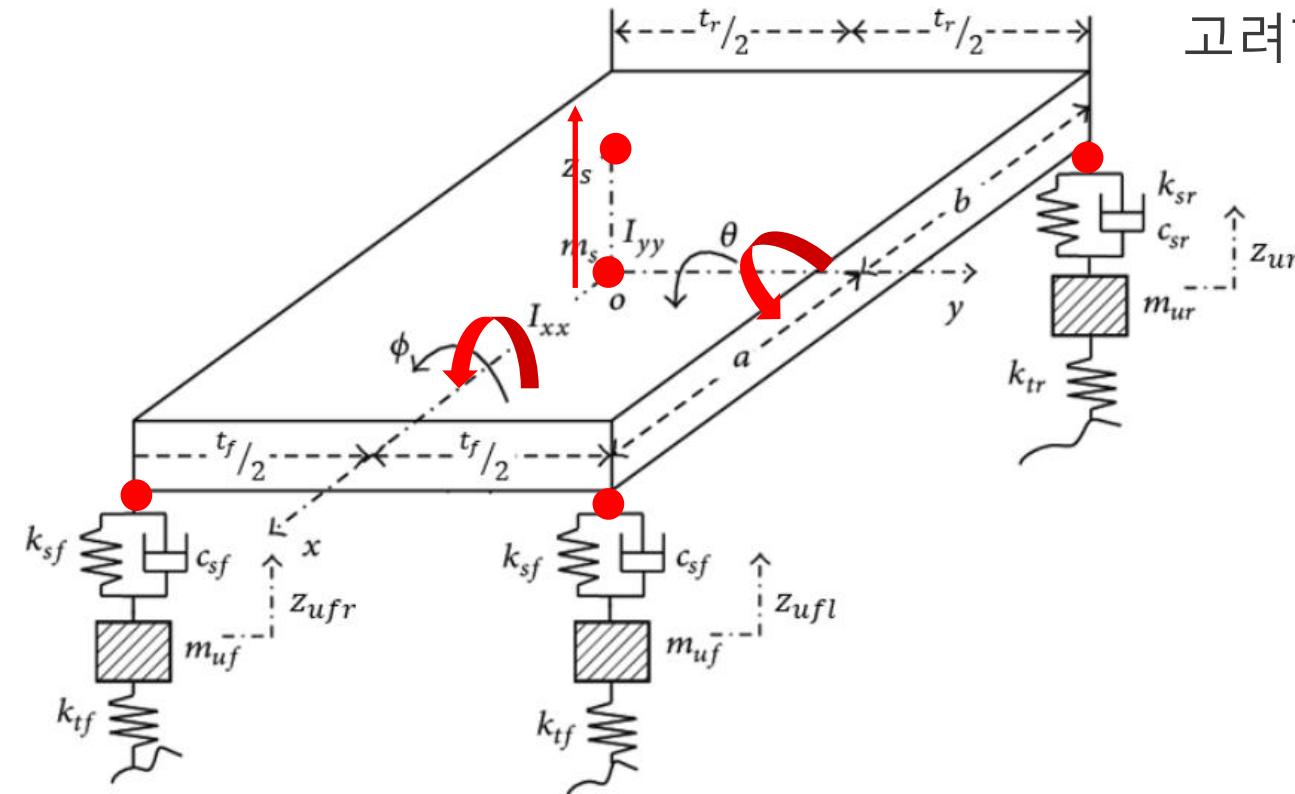
→ Downforce, Dragforce를 일정하게 유지, 고속에서의 안정성 향상



2

# Full - Car Model

FRICS를 설치할 기본 모델 및 대조군의 역할을 위해  
Full – Car Model 작성



고려한 지점 : 각 서스펜션 시스템 4군데, 가운데 무게중심  
고려한 position : Z변위, Pitch, Yaw

지면 변위 4개

$(z_{ground,FR}, z_{ground,FL}, z_{ground,RR}, z_{ground,RL})$

서스펜션(unsprung) 변위 4개

$(z_{FR}, z_{FL}, z_{RR}, z_{RL})$

차량(sprung)에 대한 움직임 3개

$(z, \theta, \phi)$

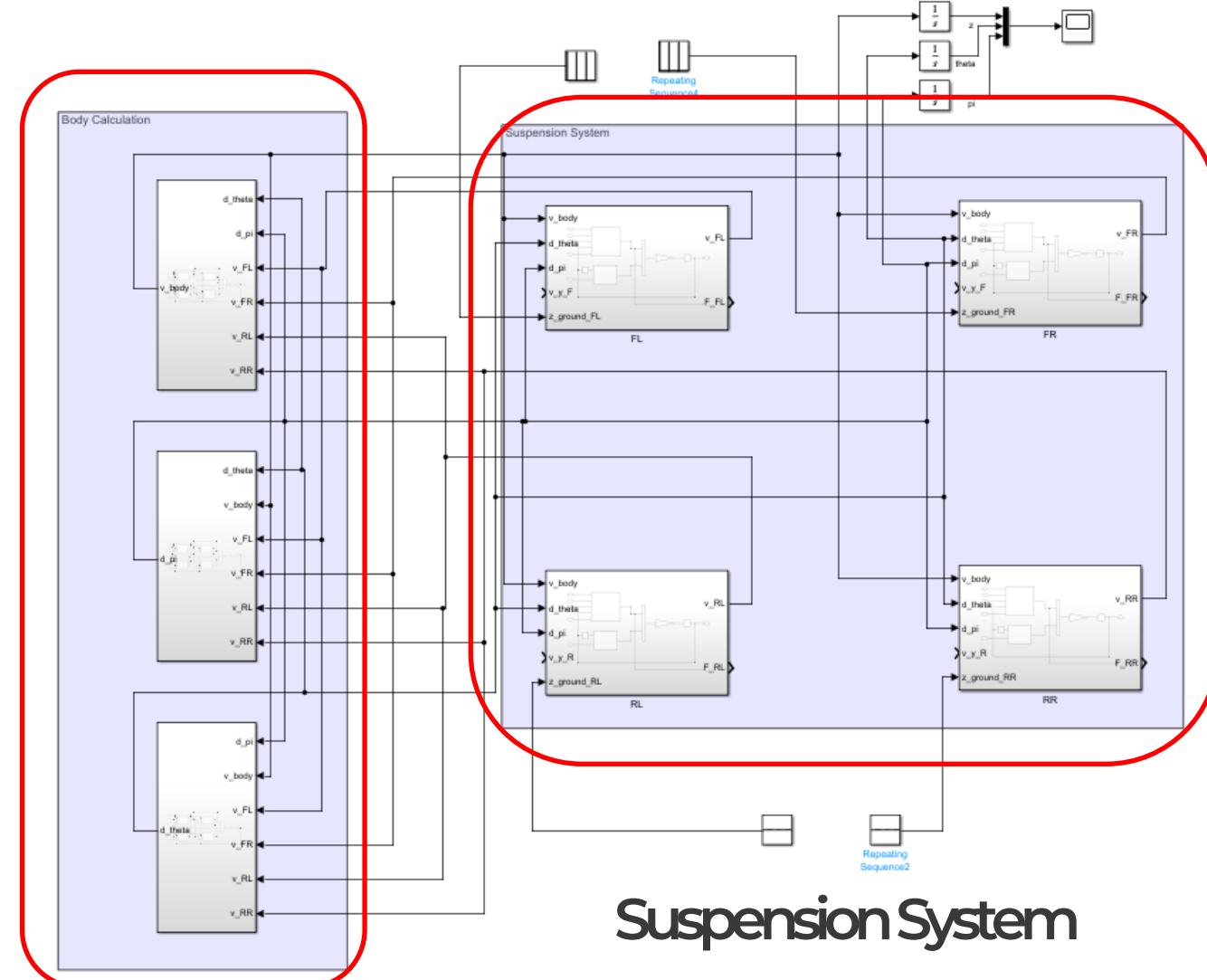
차량의 길이, 질량 등의 정보 10개

$(w, L_F, L_R, m_{vehicle}, I_{xx}, I_{yy})$

$(m_{FR}, m_{FL}, m_{RR}, m_{RL})$

서스펜션에 대한 계수 8개

$(k_{FR}, k_{FL}, k_{RL}, k_{LR}, c_{FR}, c_{FL}, c_{RL}, c_{LR})$

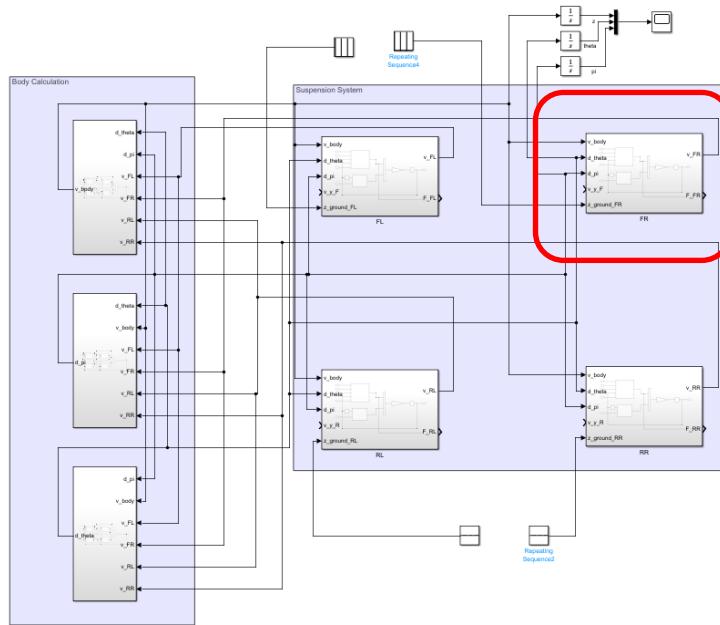


Body Calculation

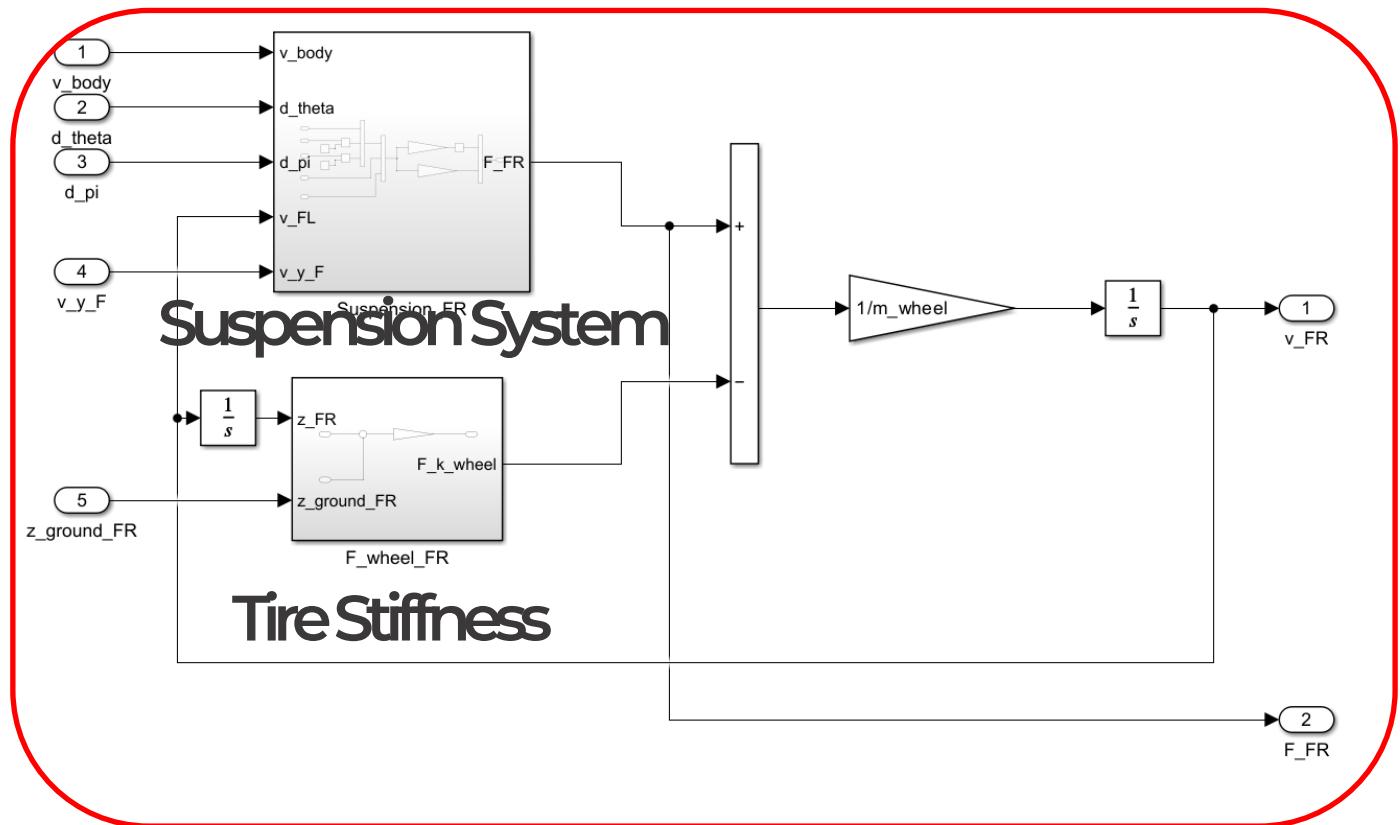
Suspension System

## 2

## Full-Car Model

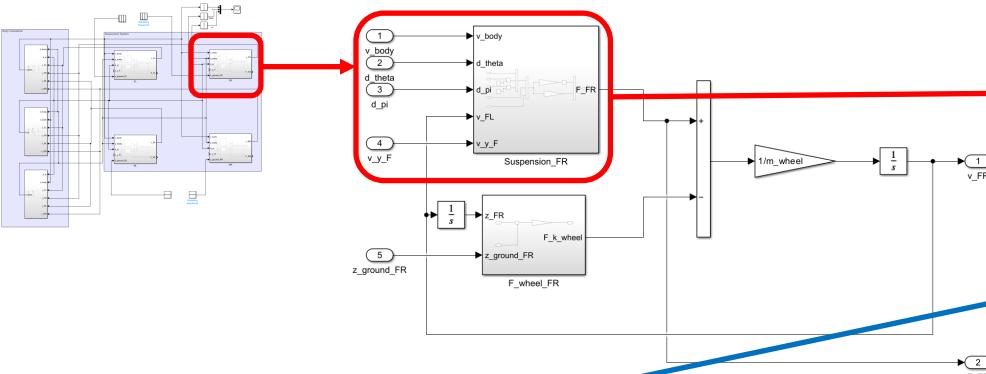


FR (Front, Right): 오른쪽 앞바퀴와 연결된 Suspension System



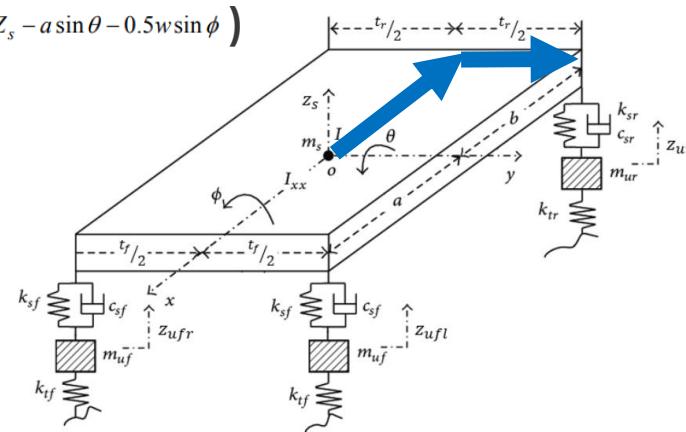
## 2

## Full-Car Model

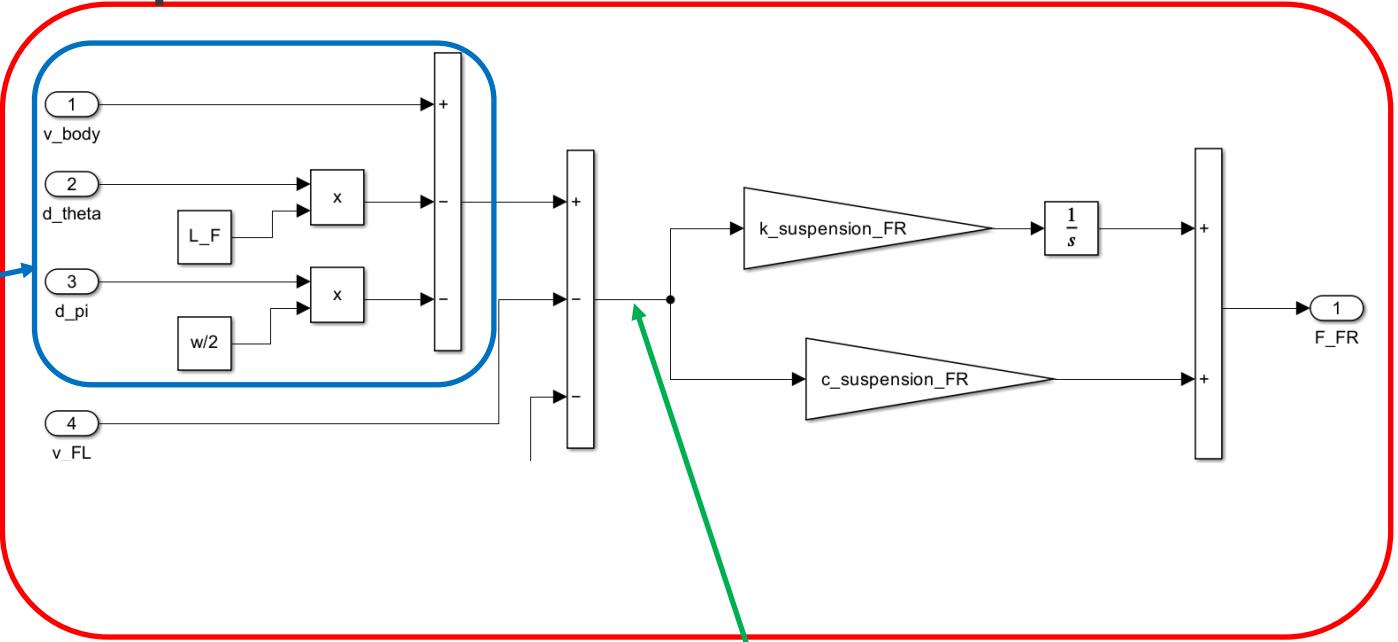


$$Z_{s,fr} = Z_s - a\theta - 0.5w\phi$$

$$( Z_{s,fr} = Z_s - a \sin \theta - 0.5 w \sin \phi )$$



## Suspension\_FR



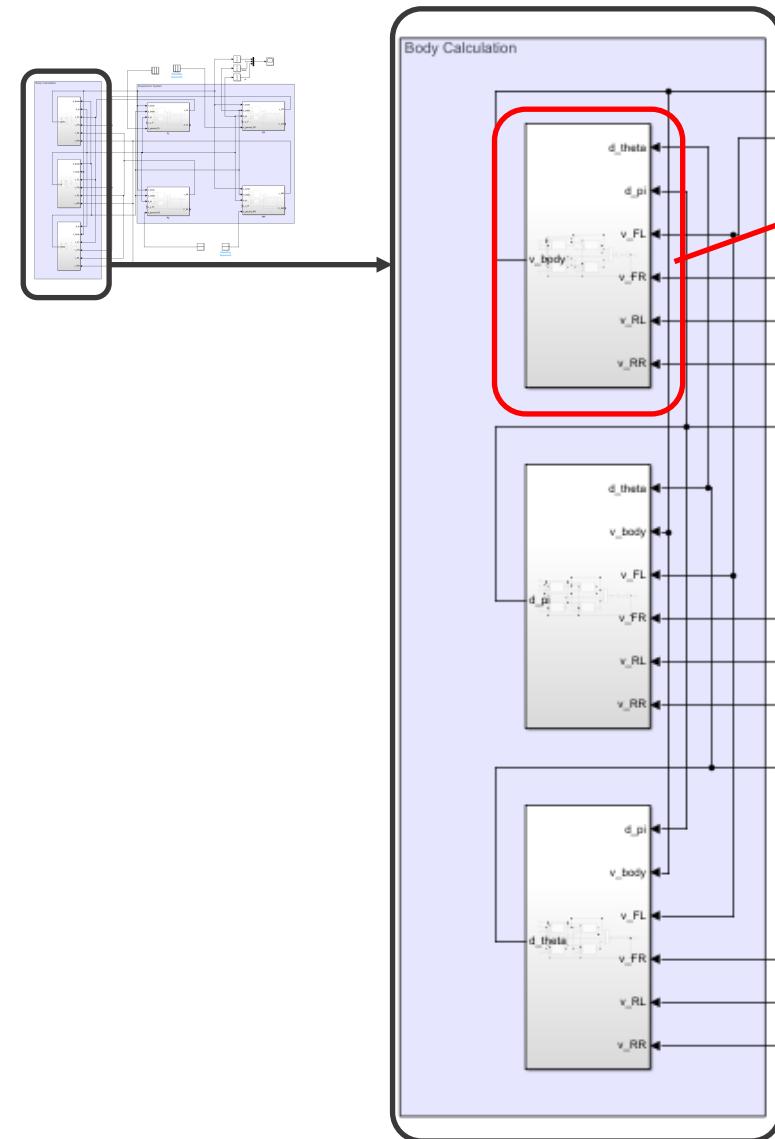
$$F_{fr} = K_{s,fr} (Z_{u,fr} - Z_{s,fr}) + C_{s,fr} (\dot{Z}_{u,fr} - \dot{Z}_{s,fr})$$

변위(속도)를 기반으로 spring, damper의 힘 계산

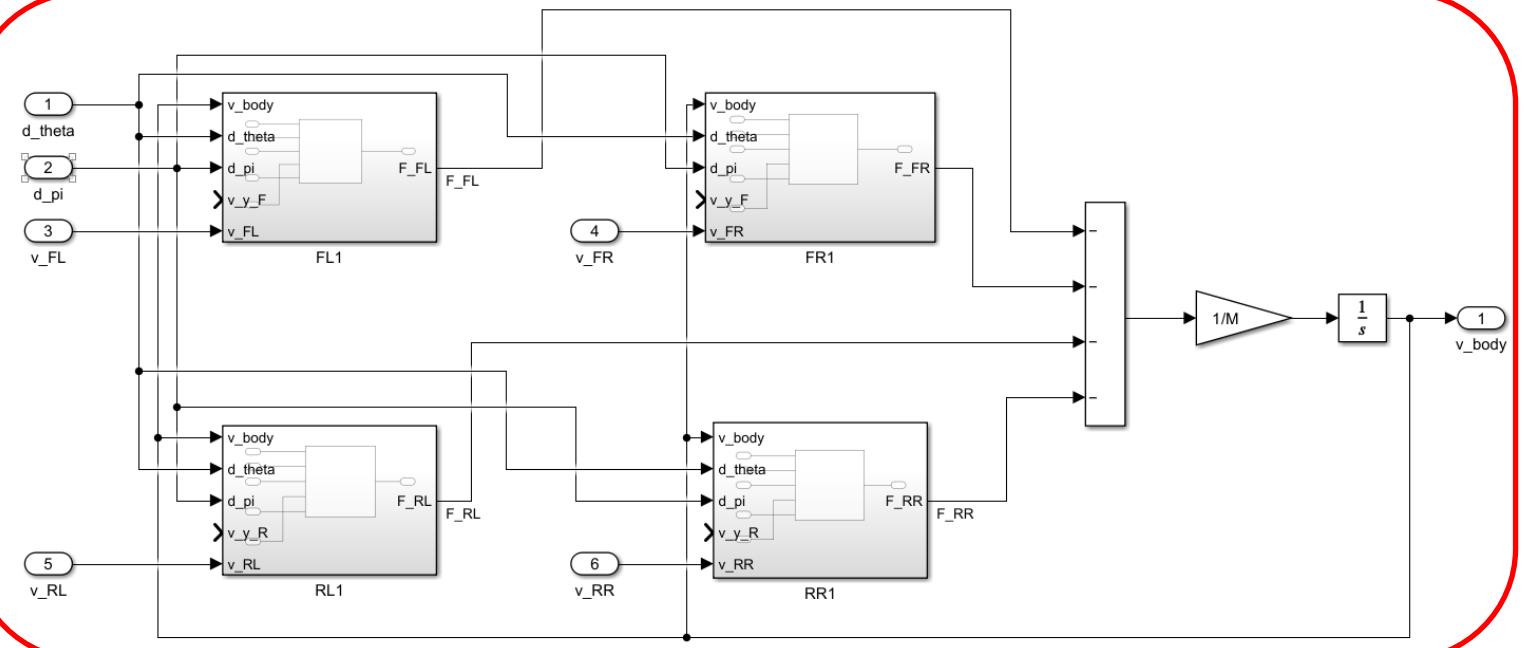
FR지점의 변위(속도)를 차량 무게중심의 변위 기반으로  
Pitch( $\phi$ ), Yaw( $\phi$ )와 차량의 크기를 고려하여 계산

## 2

## Full-Car Model



v body calculation

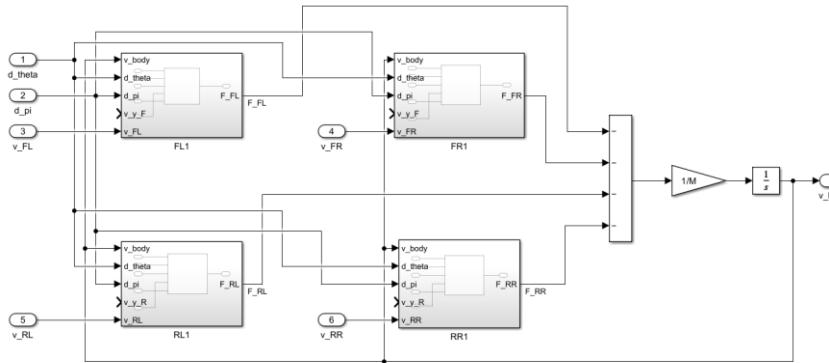


Body의 position 계산하는 area.

각 subsystem 내부는 대부분 위와 같은 형태로 구성되어 있음.

Q) 왜 외부의 서스펜션 (FL, FR, RL, RR)값을 그대로 사용하지 않았는가?  
왜 세 개의 subsystem으로 따로 구현했는가?

Q) 왜 외부의 서스펜션 (FL, FR, RL, RR)값을 그대로 사용하지 않았는가?  
왜 세 개의 subsystem으로 따로 구현했는가?



### 3. 대수 루프 주의 사항

입력과 출력에 동일한 변수를 사용할 때는 대수 루프가 발생할 가능성이 큽니다. 대수 루프는 다음과 같은 문제를 일으킬 수 있습니다:

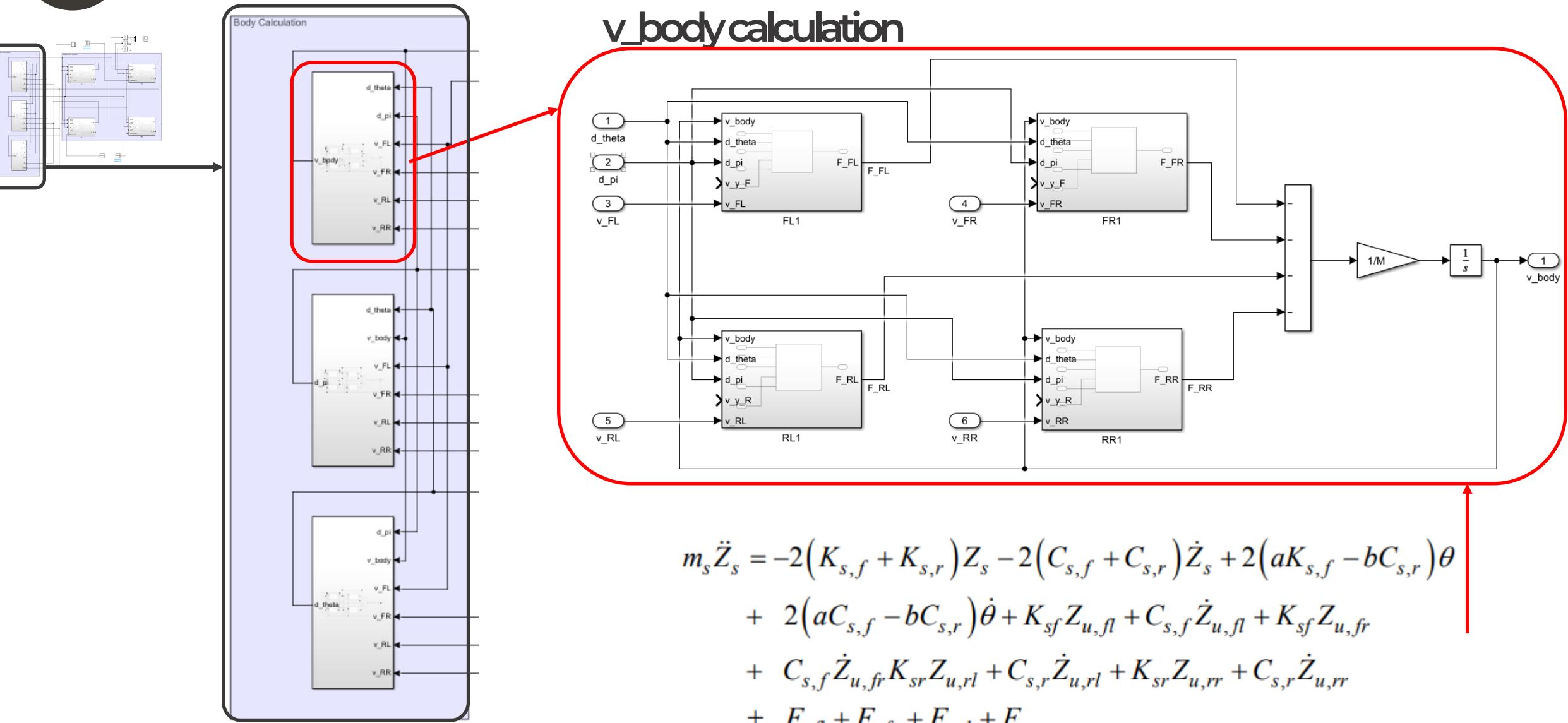
- 시스템의 상태나 변수가 순환적인 의존성을 가질 때, Simulink는 이를 해결할 방법을 찾지 못할 수 있습니다.
- 대수 루프를 해결하기 위해 Simulink는 특정 해결 방법을 사용하지만, 때때로 수치적으로 불안정할 수 있고, 이로 인해 시뮬레이션이 제대로 실행되지 않을 수 있습니다.

한 Subsystem의 output 값을 그대로 다시 input으로 사용한다면  
(input에 있는 변수를 output으로도 출력한다면)  
순환적인 의존성으로 인해 수치적 불안정



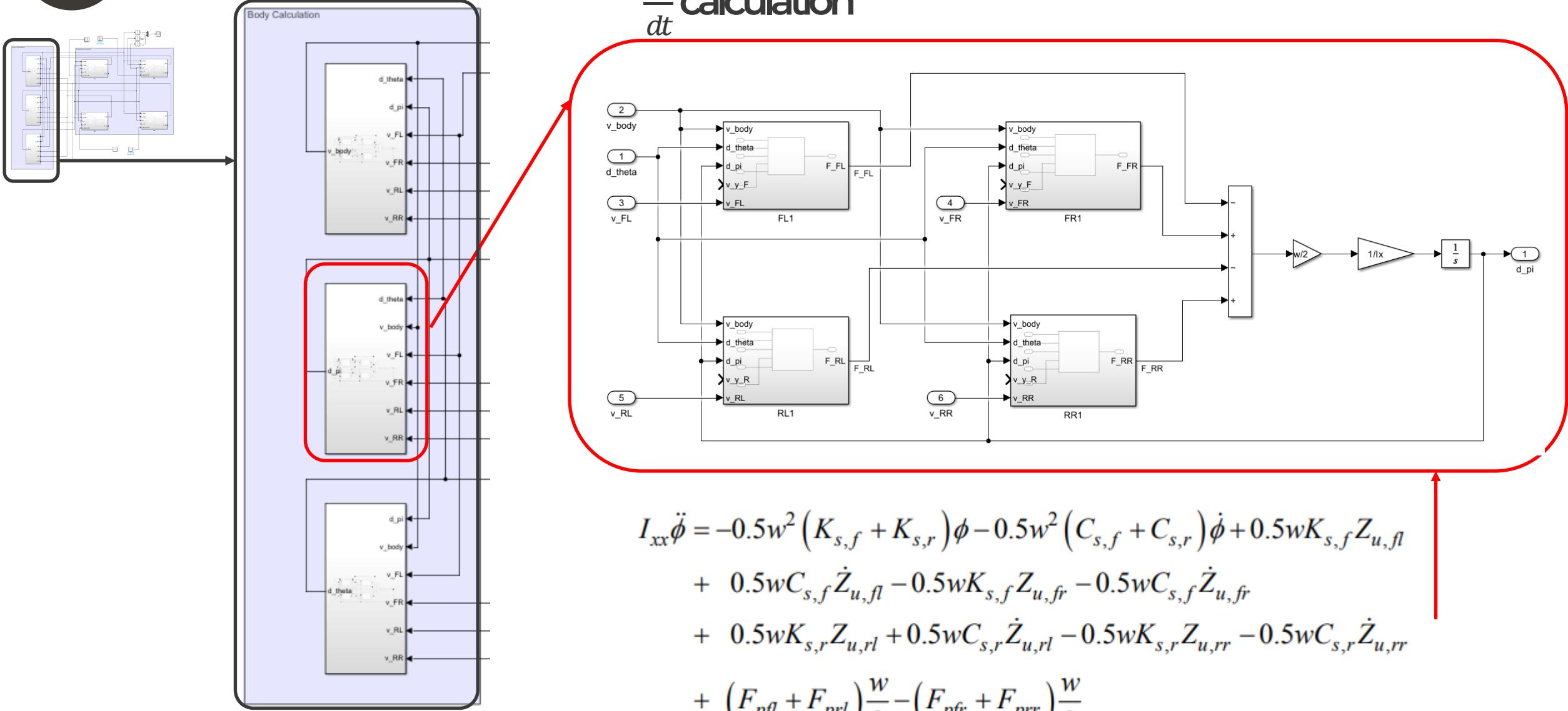
## 2

## Full-Car Model



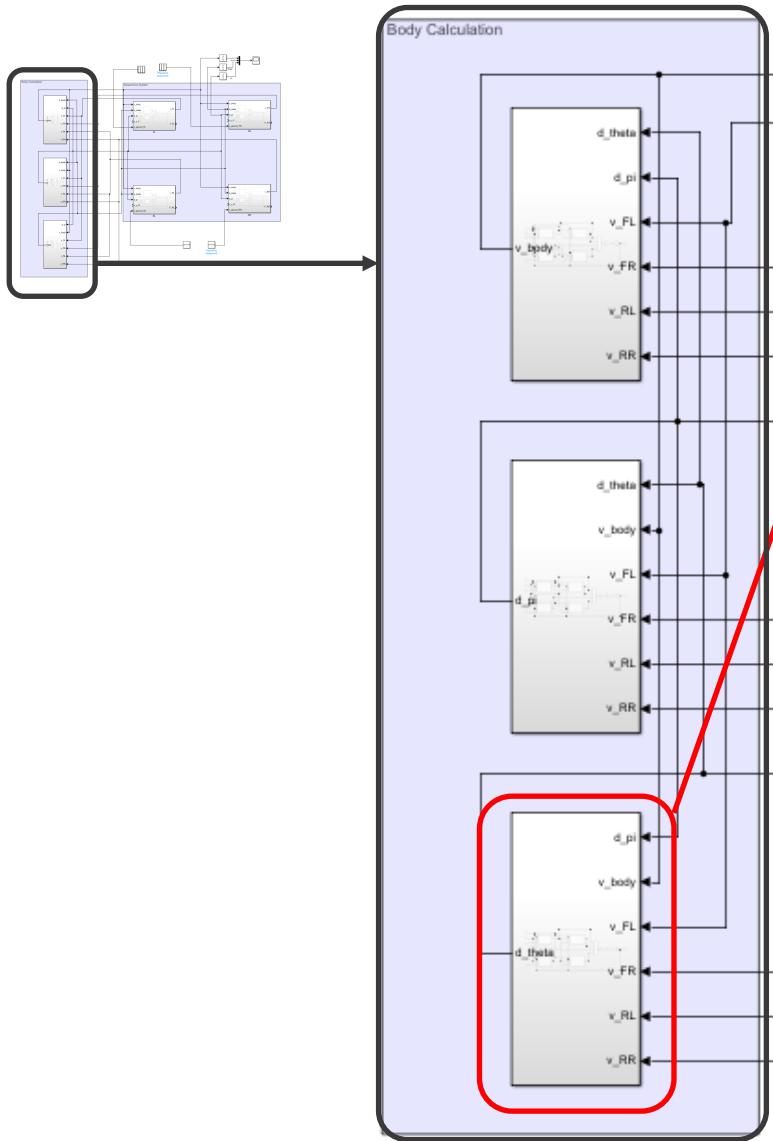
2

# Full – Car Model

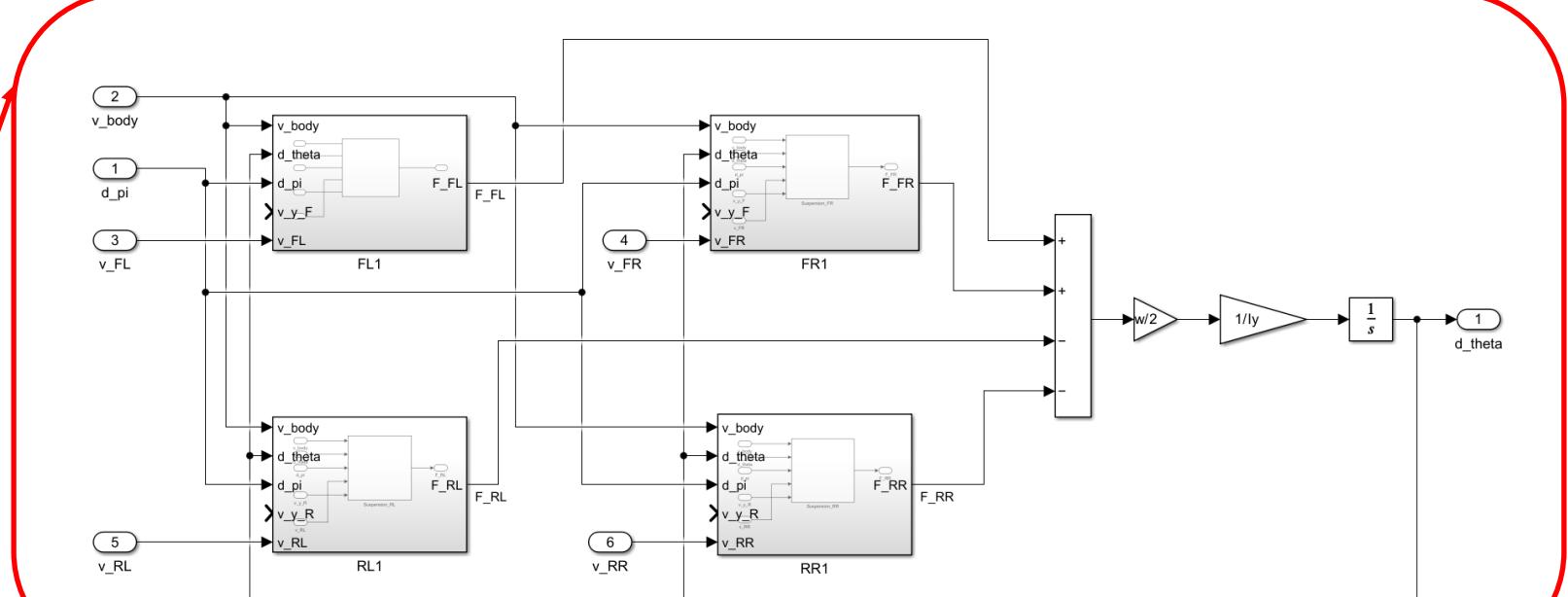


## 2

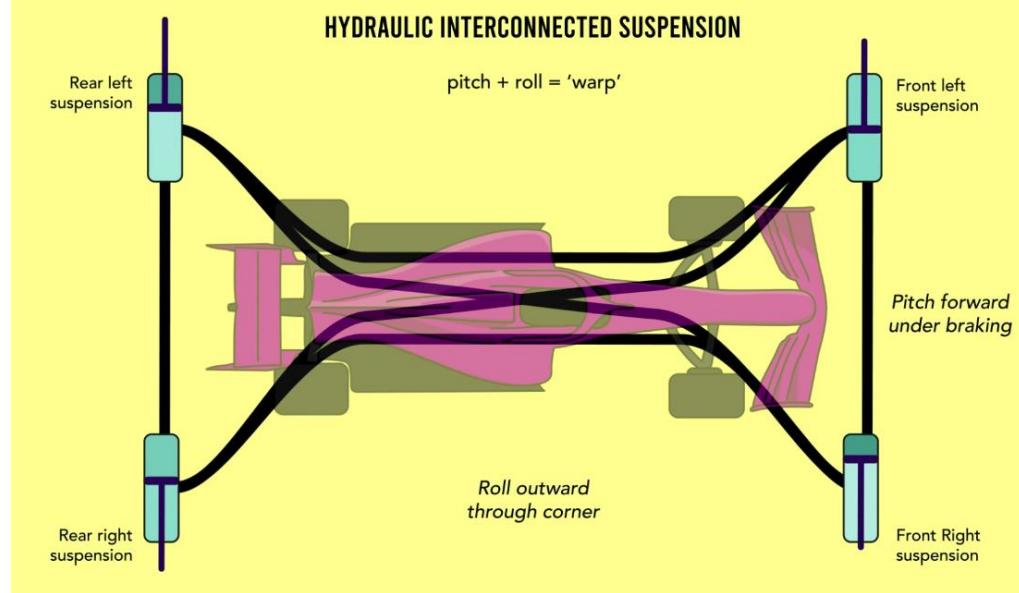
## Full-Car Model



$\frac{d\theta}{dt}$  calculation



$$\begin{aligned}
 I_{yy} \ddot{\theta} = & 2(aK_{s,f} - bK_{s,r})Z_s + 2(aC_{s,f} - bC_{s,r})\dot{Z}_s - 2(a^2K_{s,f} + b^2K_{s,r})\theta \\
 & - 2(a^2C_{s,f} + b^2C_{s,r})\dot{\theta} - aK_{s,f}Z_{u,fl} - aC_{s,f}\dot{Z}_{u,fl} - aK_{s,f}Z_{u,fr} \\
 & - aC_{s,f}\dot{Z}_{u,fr} + bK_{s,r}Z_{u,rl} + bC_{s,r}\dot{Z}_{u,rl} + bK_{s,r}Z_{u,rr} + bC_{s,r}\dot{Z}_{u,rr} \\
 & - (F_{pfl} + F_{pfr})l_f + (F_{prl} + F_{prr})l_r
 \end{aligned}$$



1

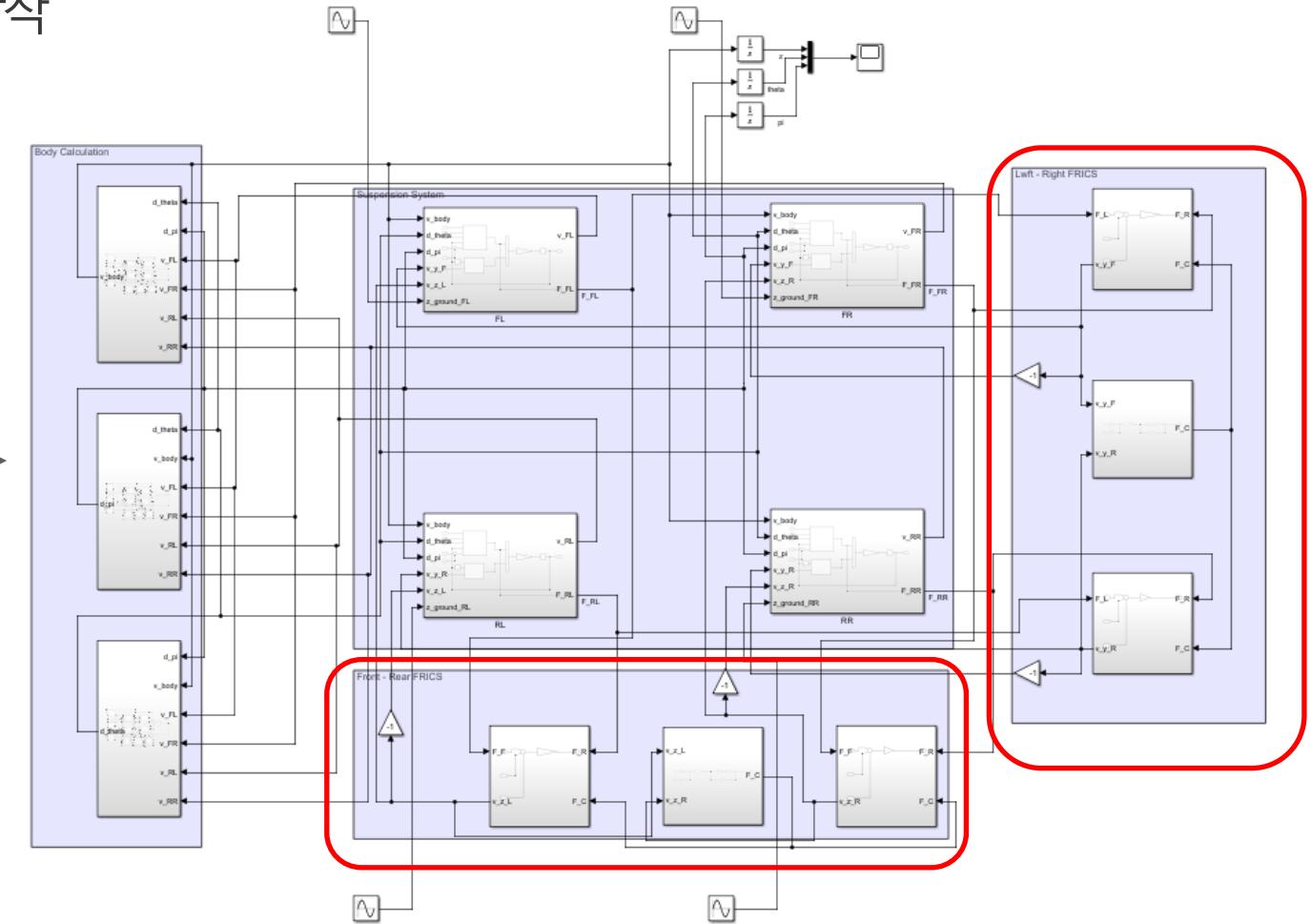
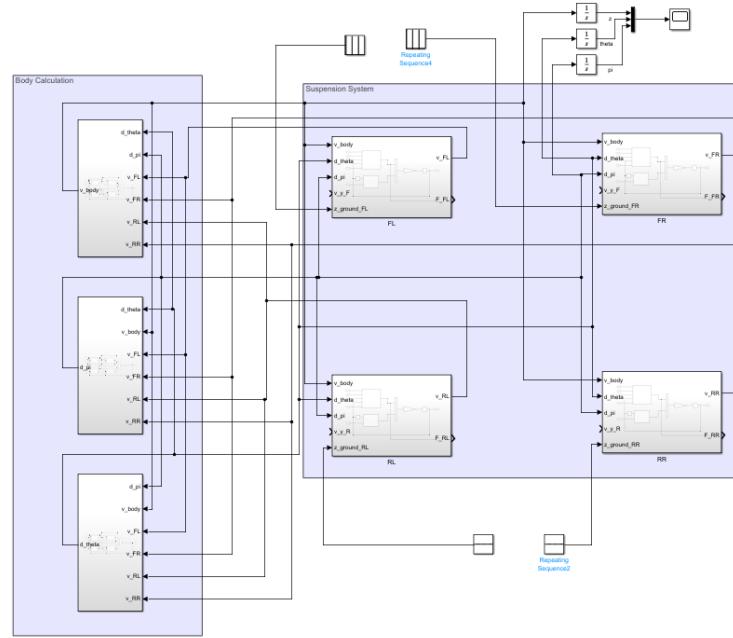
# FRICS

**Front and Rear Interconnected Suspension**

## 1

# FRICS: Front and Rear Interconnected Suspension

지금까지 만들어온 Full-Car Model에 FRICS 장착

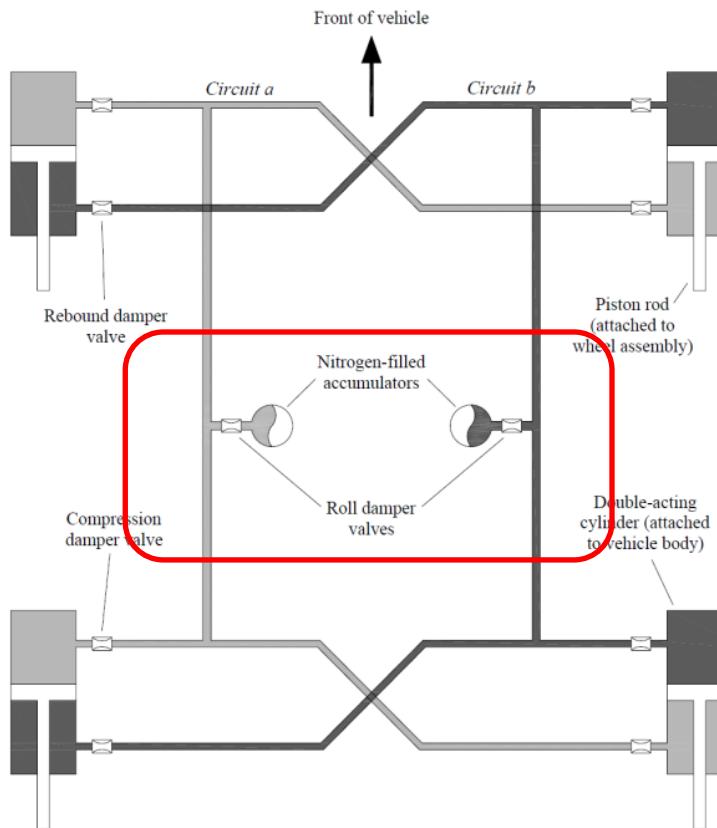


Full-Car Model

Full -Car Model + FRICS 2쌍

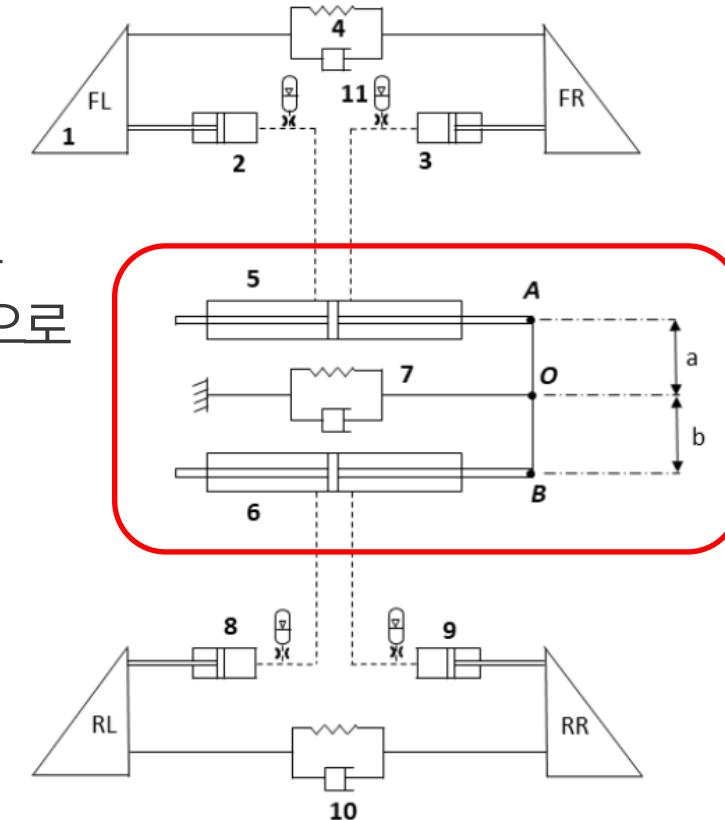
## 1

# FRICS: Front and Rear Interconnected Suspension



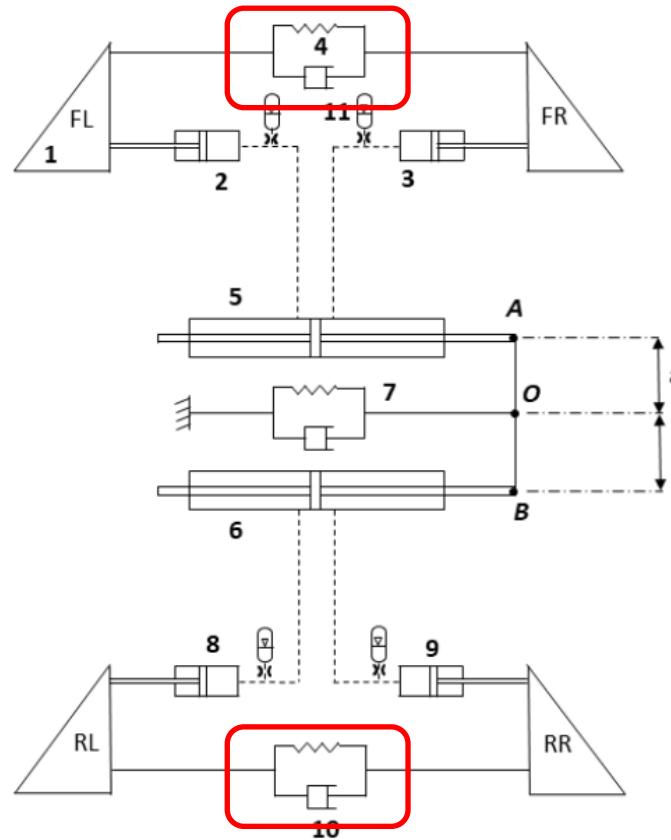
유체 시스템의 **accumulator**를  
Piston x 2, Suspension system으로

**Simplify**

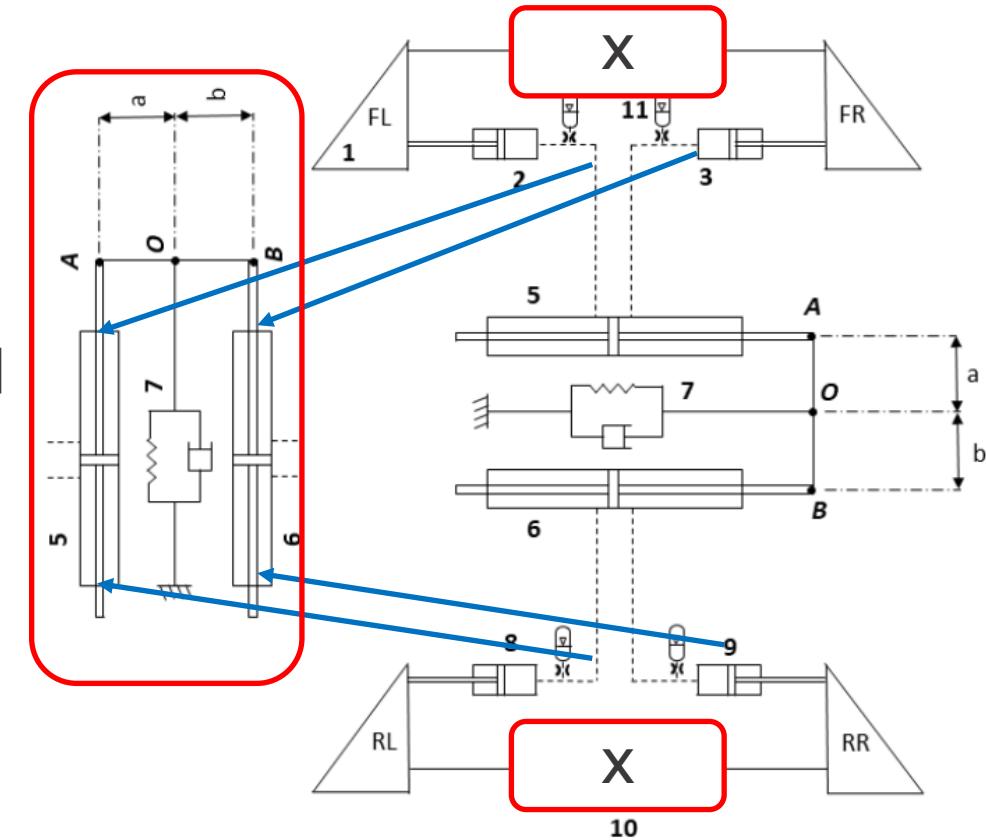


## 1

# FRICS: Front and Rear Interconnected Suspension

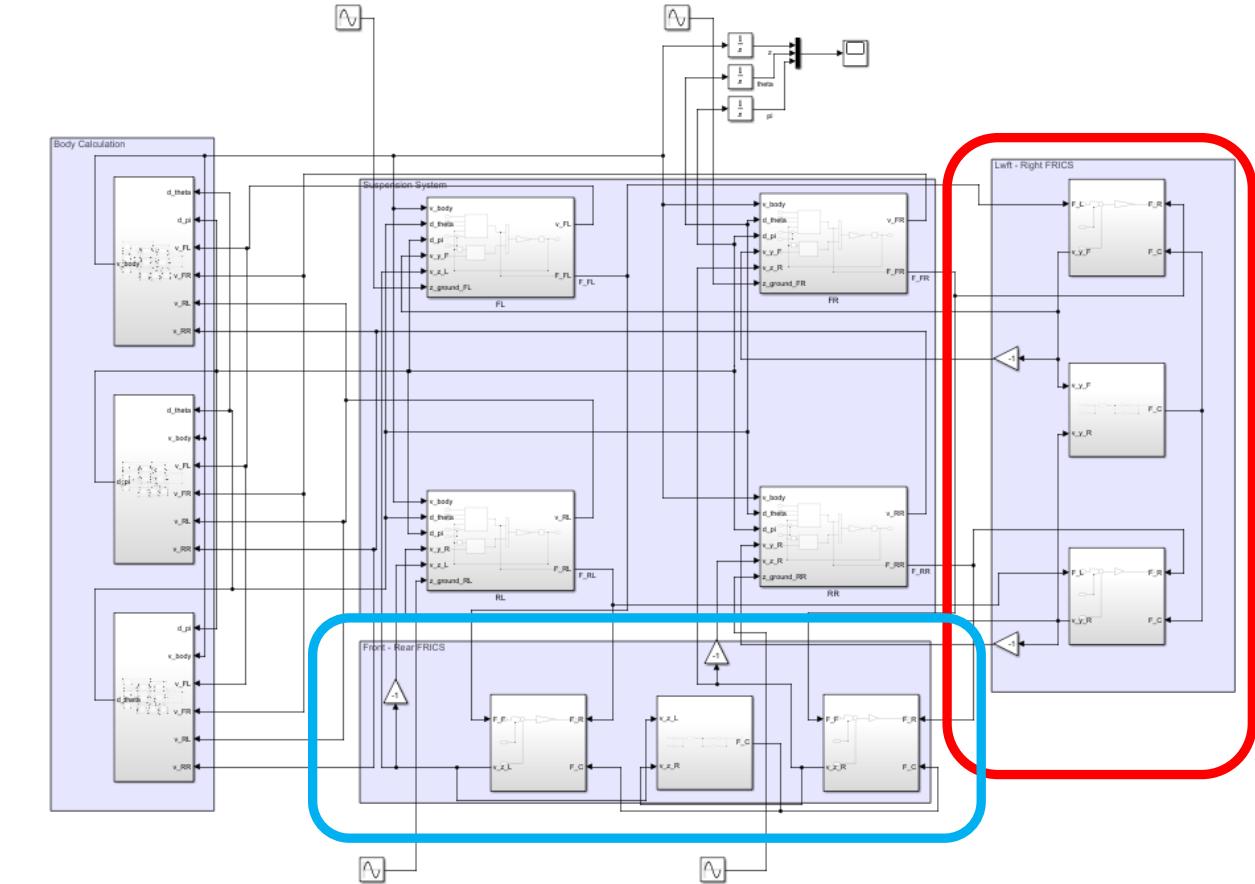
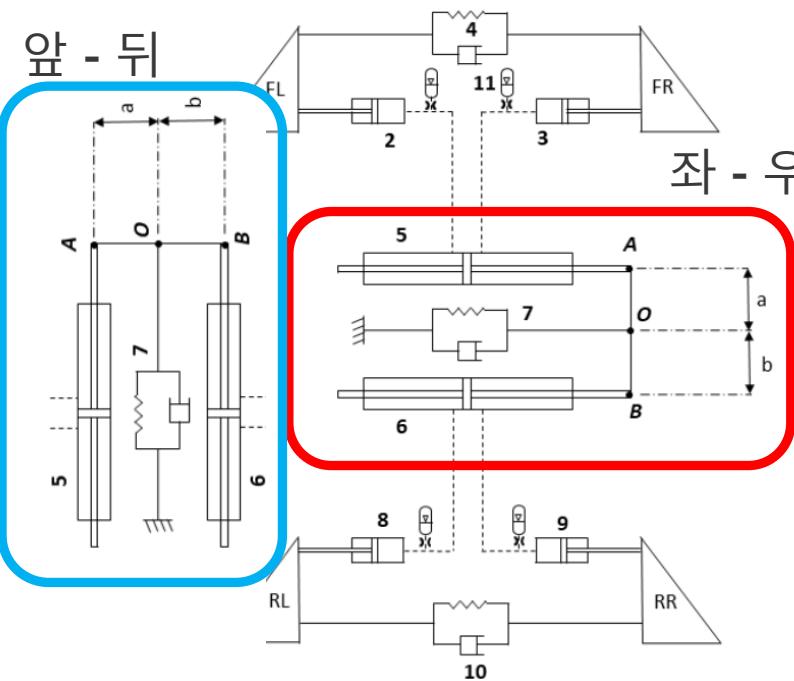


Heavespring-damper를 삭제  
앞뒤의 움직임도 제어하는  
FRICIS 추가



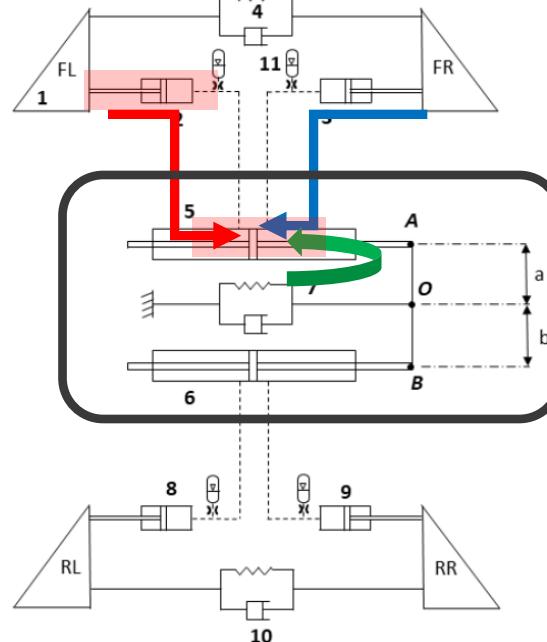
## 1

# FRICS: Front and Rear Interconnected Suspension

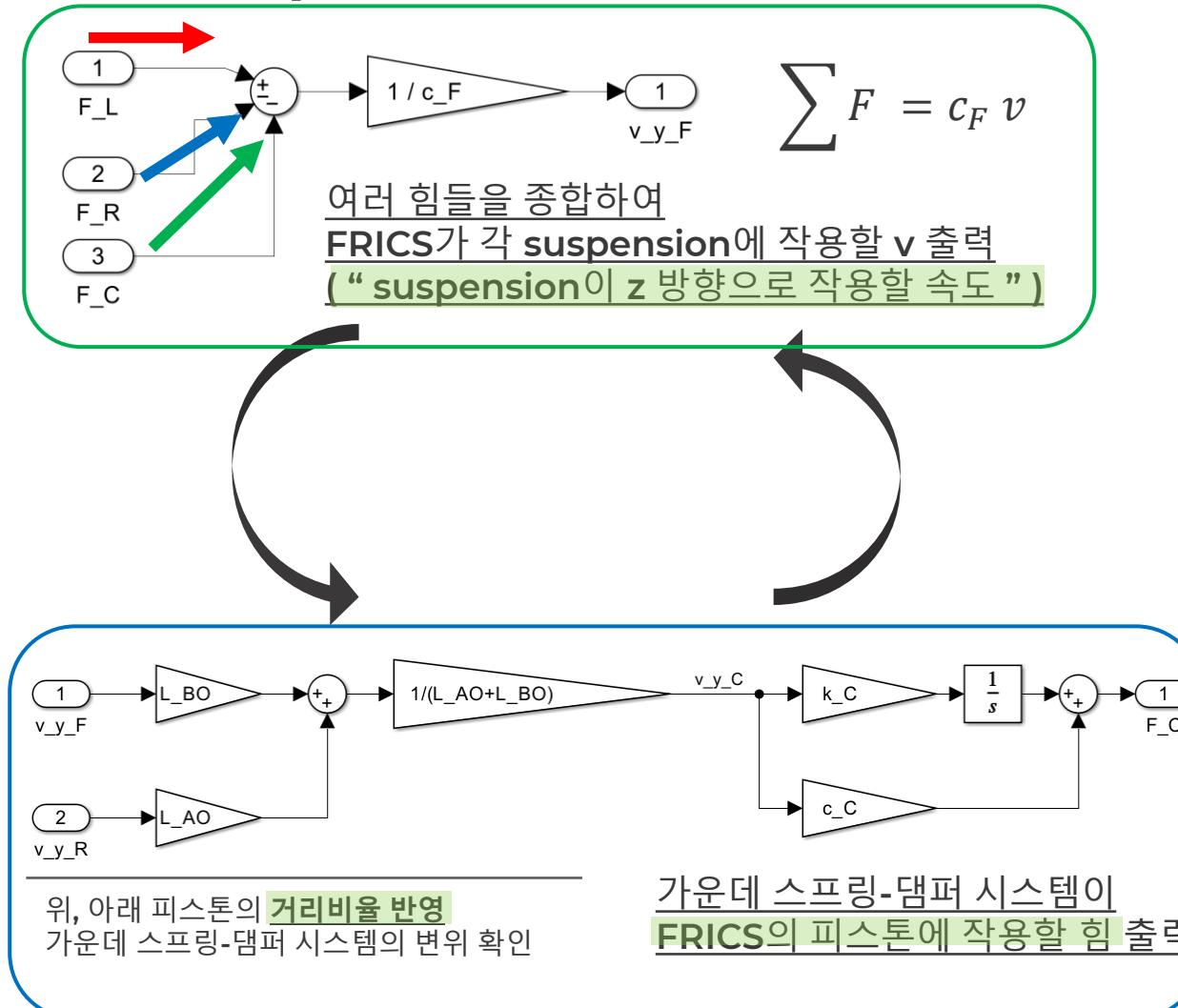
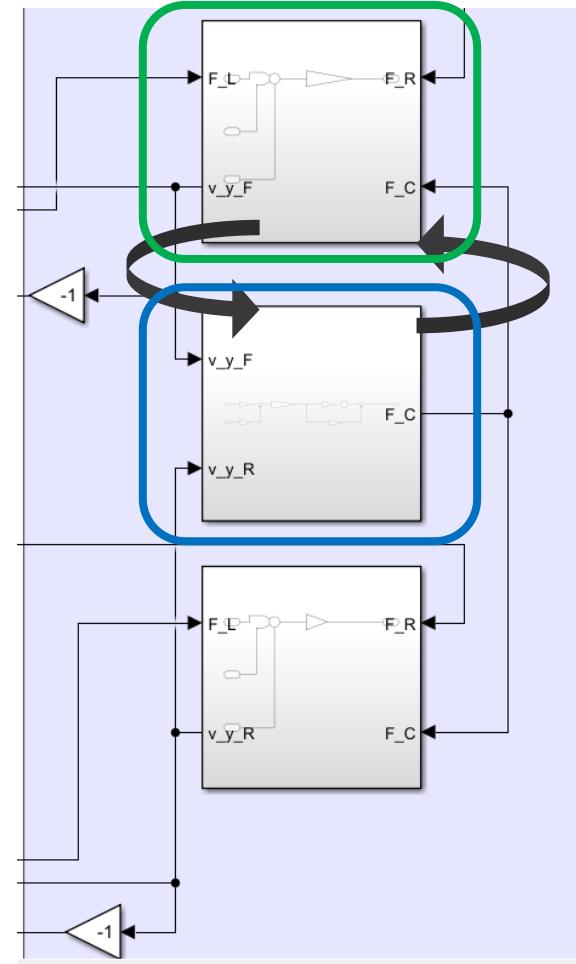


## 1

# FRICS: Front and Rear Interconnected Suspension



좌 - 우  
FRICS

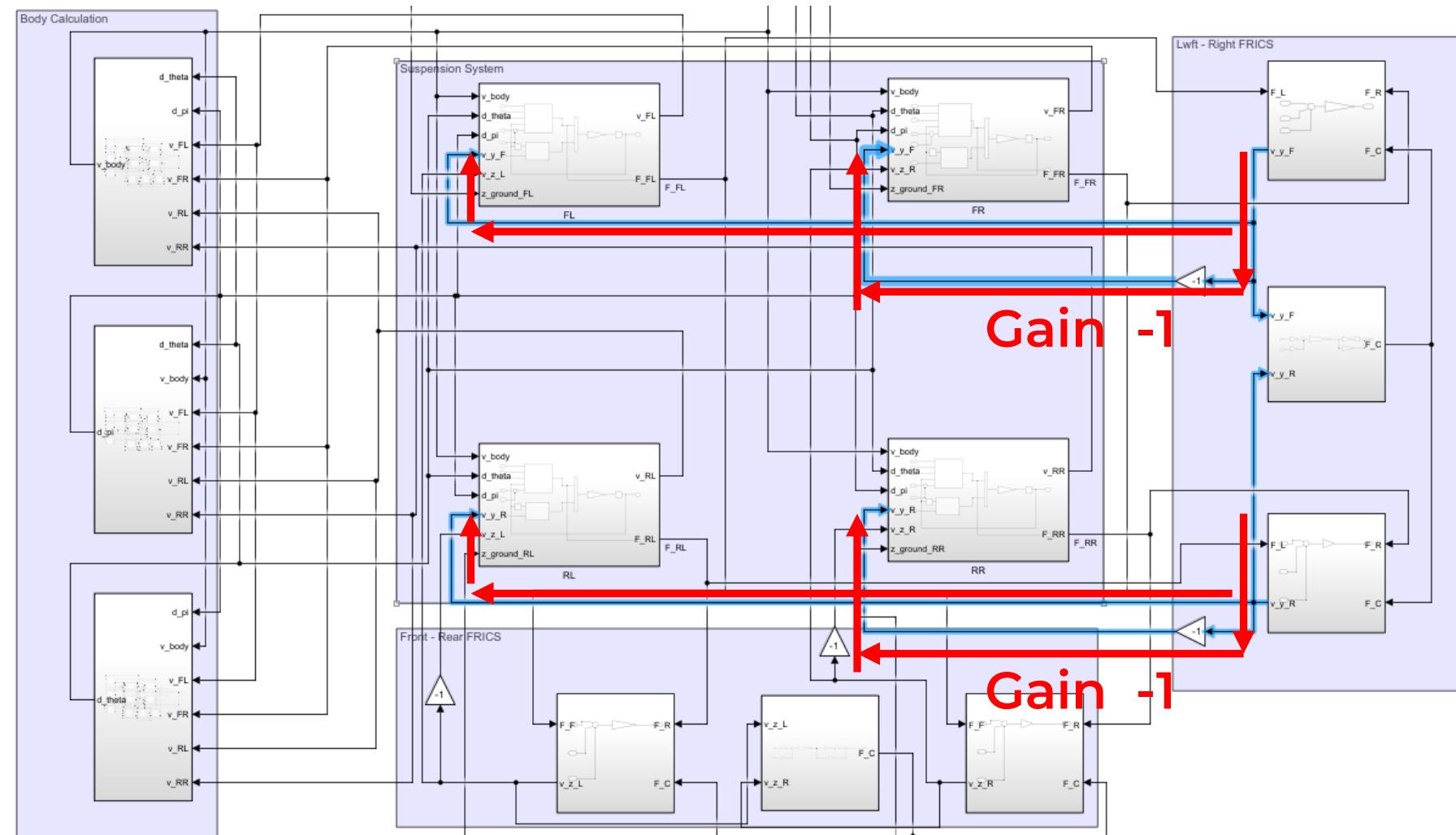


위, 아래 피스톤의 거리비율 반영  
가운데 스프링-댐퍼 시스템의 변위 확인

가운데 스프링-댐퍼 시스템이  
FRICS의 피스톤에 작용할 힘 출력

## 1

# FRICS: Front and Rear Interconnected Suspension



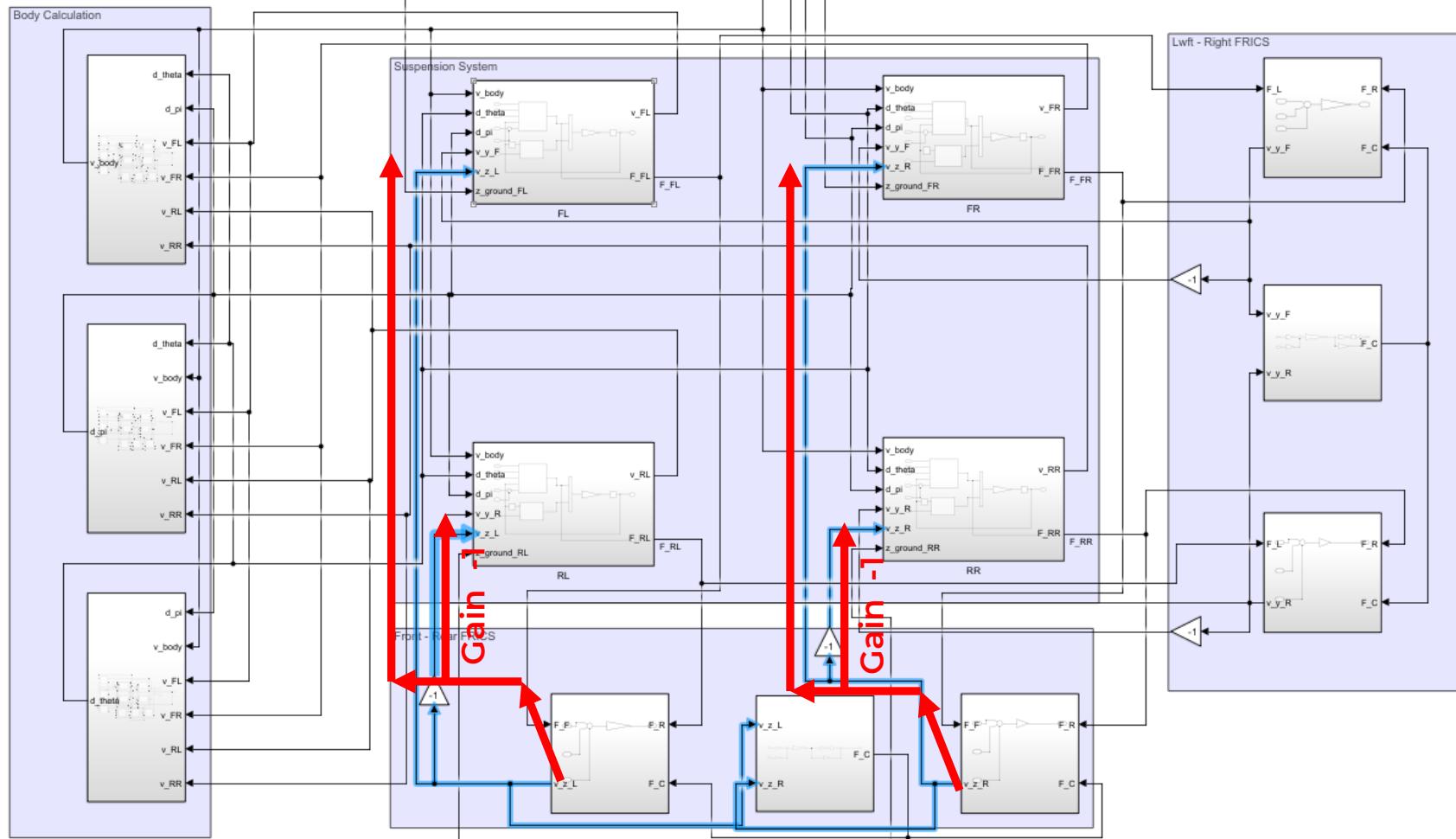
좌, 우 suspension system에  
반대 부호의 v값을 전달

Gain -1

Gain -1

## 1

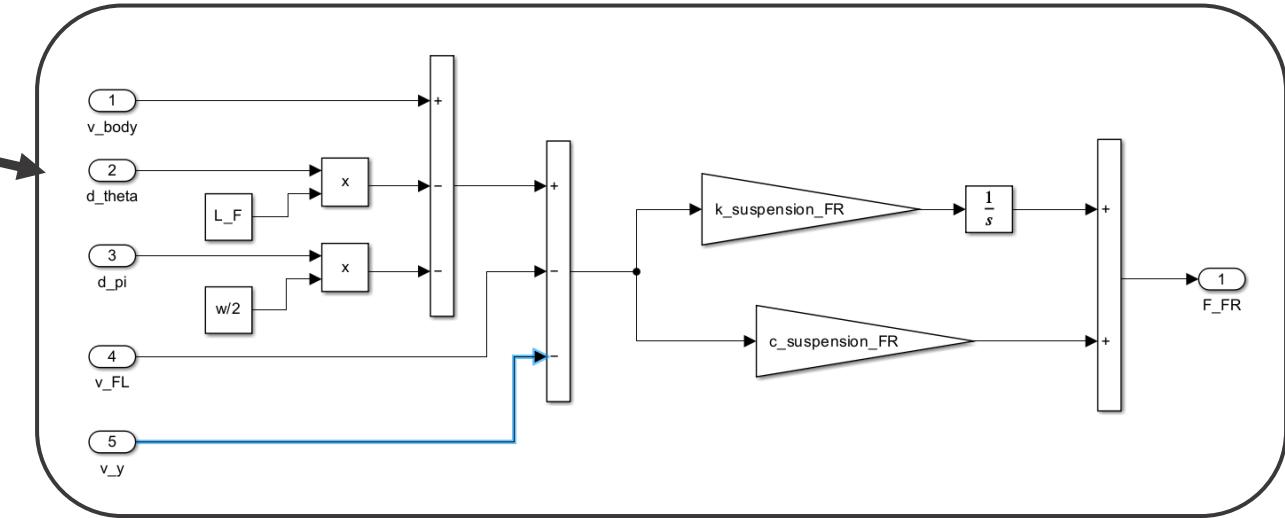
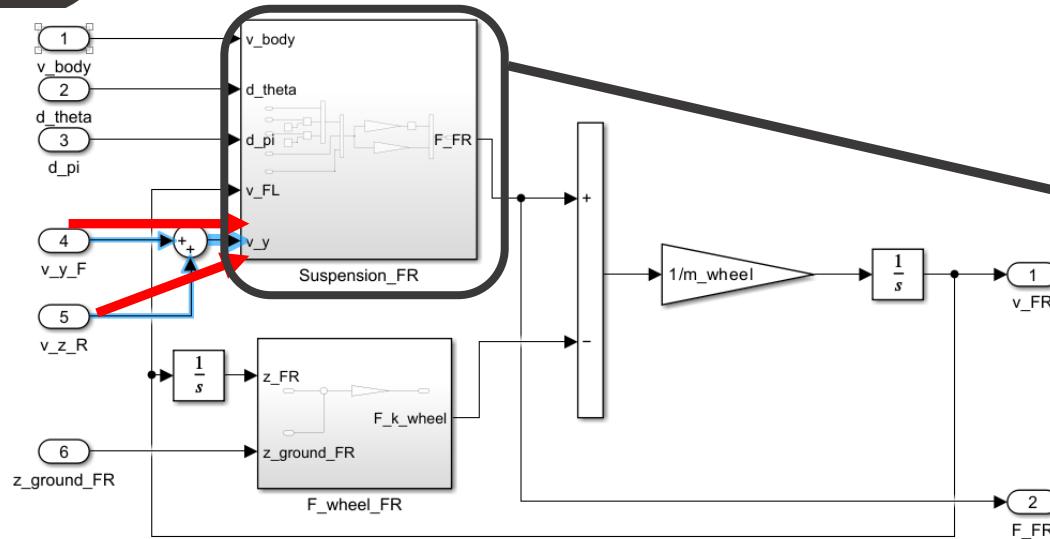
# FRICS: Front and Rear Interconnected Suspension



Front-Rear FRICS도  
동시에 작용

## 1

# FRICS: Front and Rear Interconnected Suspension



FRICS의 output이 각 바퀴의 suspension system에 전달됨

(Left-Right FRICS, Front-Rear FRICS 두 개가 같이 전달됨)

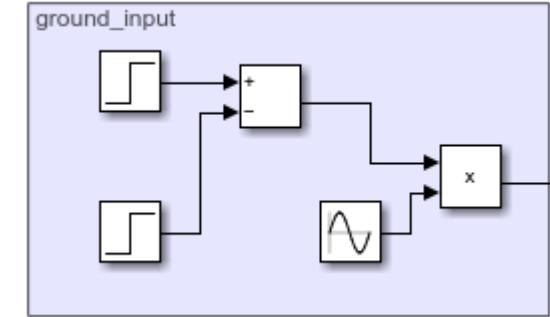
## 1

# FRICS: Front and Rear Interconnected Suspension

Full Car 와 Full Car with FRICS 를 비교

**Input :** 각각의 바퀴에 지면의 변위를 입력,  $t = 1\text{s} \sim 2\text{s}$ 에 사인파 입력

Pitch를 FRICS가 효과적으로 감쇠해주는지를 확인하기 위해  
앞바퀴와 뒷바퀴에 위상을 다르게 입력



진폭:

0.05

편향:

0

주파수(rad/s):

$10*\pi$

위상(rad):

0

FL & FR input

진폭:

0.05

편향:

0

주파수(rad/s):

$10*\pi$

위상(rad):

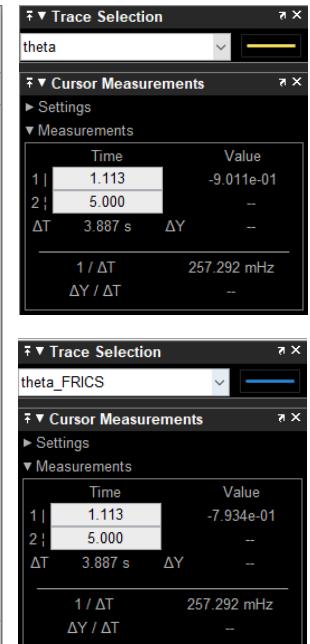
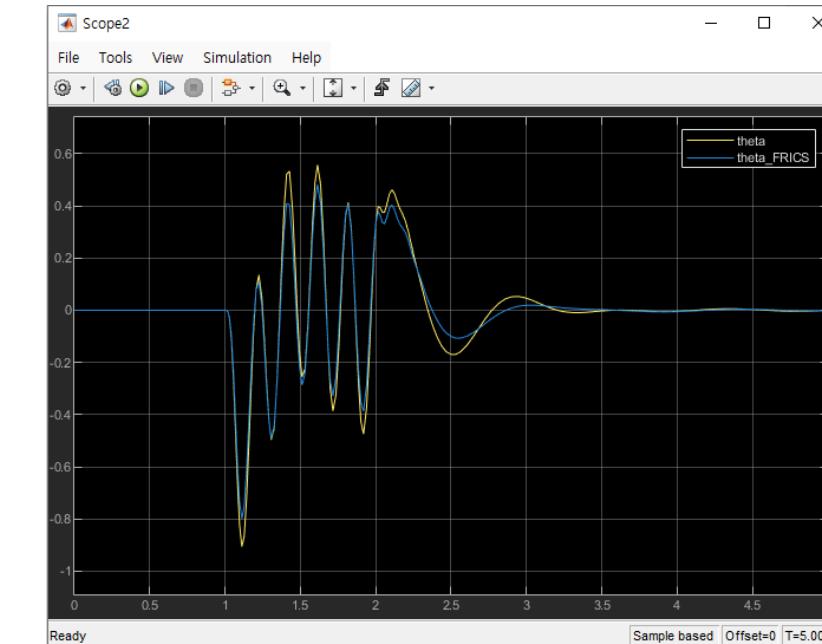
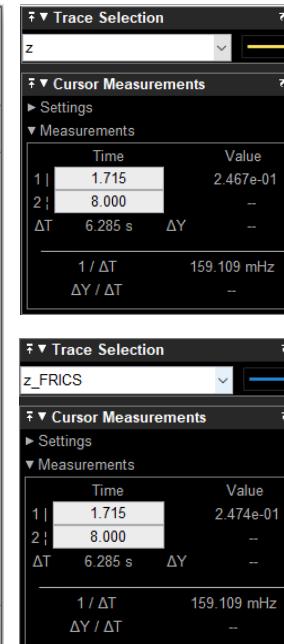
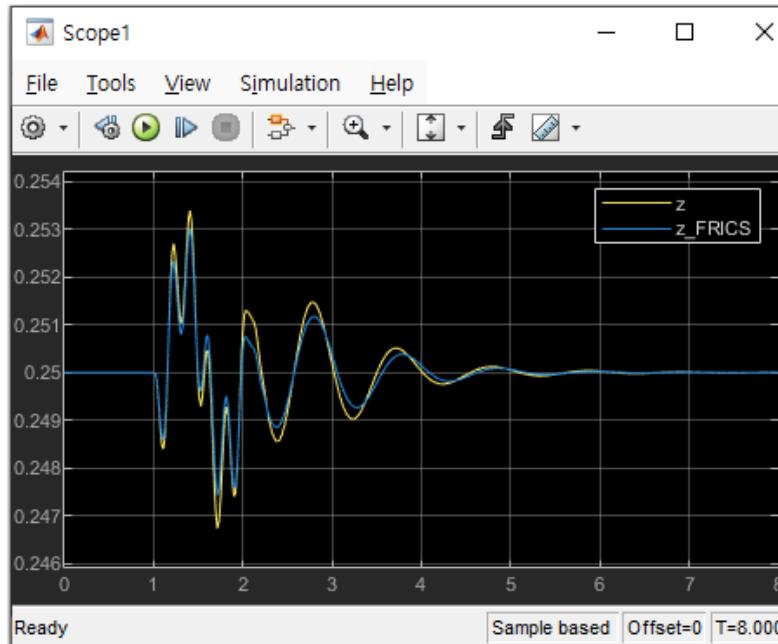
$-\pi$

RL & RR input

## 1

# FRICS: Front and Rear Interconnected Suspension

## Pitch 상황 - z변위 & theta



FRICS를 포함한 시스템에서 z변위의 최댓값이 0.0026m,  
포함하지 않은 시스템에서의 최댓값이 0.0033m로  
**21.21%의 감소**를 보임

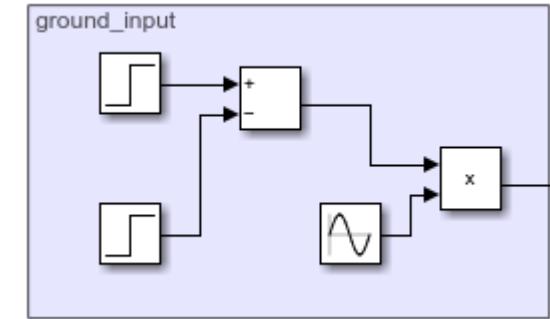
FRICS를 포함한 시스템에서 theta변화의 최댓값이 0.7934°,  
포함하지 않은 시스템에서의 최댓값이 0.9011°로  
**11.952%의 감소**를 보임

# FRICS: Front and Rear Interconnected Suspension

Full Car 와 Full Car with FRICS 를 비교

**Input :** 각각의 바퀴에 지면의 변위를 입력,  $t = 1\text{s} \sim 2\text{s}$ 에 사인파 입력

Roll을 FRICS가 효과적으로 감쇠해주는지를 확인하기 위해  
왼쪽바퀴와 오른쪽바퀴에 위상을 다르게 입력



진폭:

0.05

편향:

0

주파수(rad/s):

$10*\pi$

위상(rad):

0

FL & RL input

진폭:

0.05

편향:

0

주파수(rad/s):

$10*\pi$

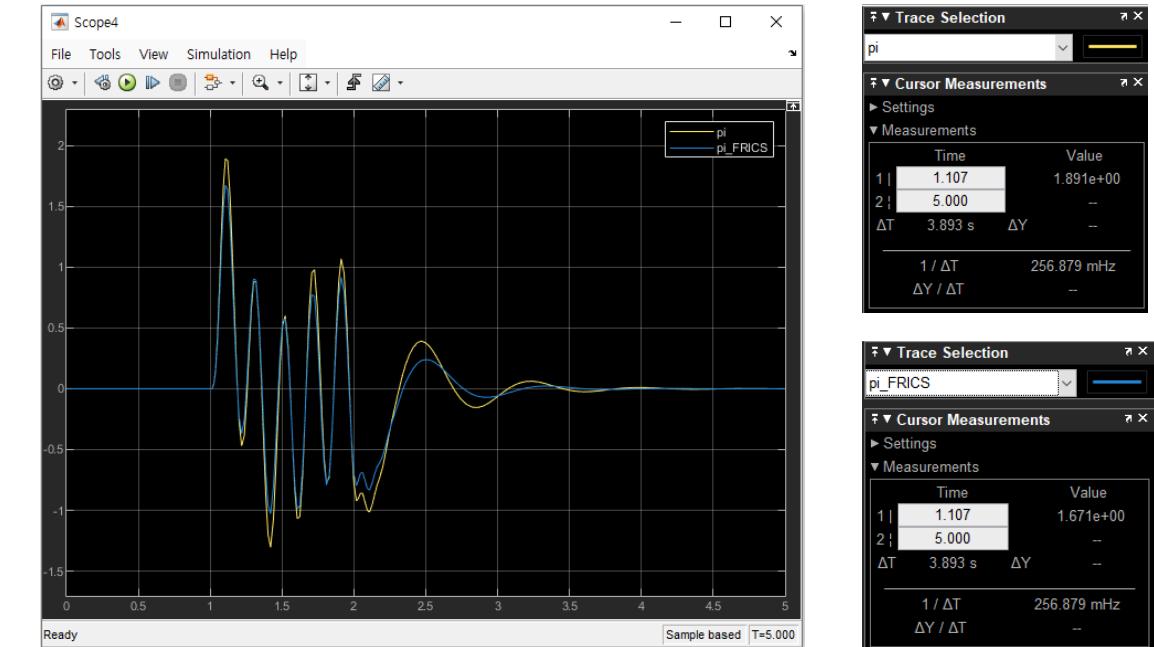
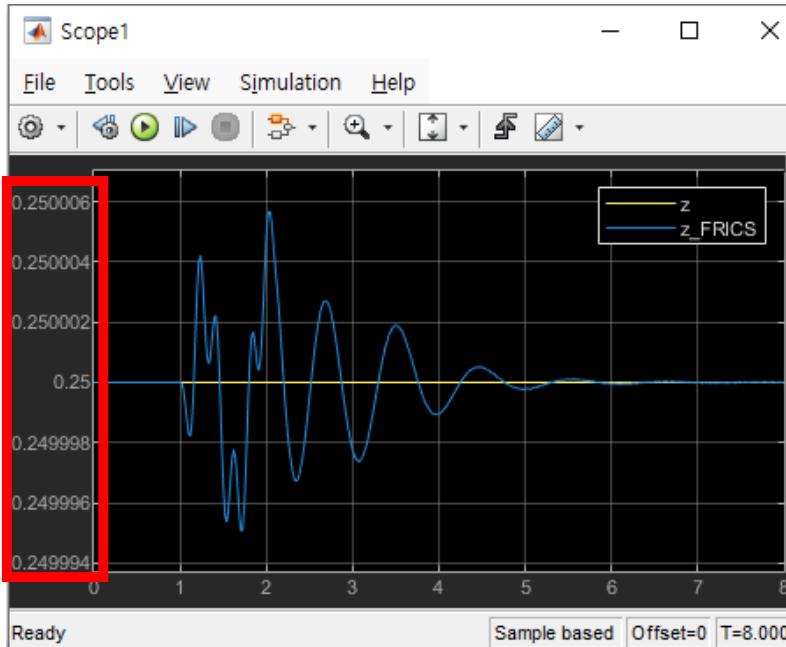
위상(rad):

$-\pi$

FR & RR input

# FRICS: Front and Rear Interconnected Suspension

## Roll 상황 - z변위 & pi



Roll 상황에서는 **body**의 무게중심의 z변위가 0이 되어야 하지만, FRICS 시스템이 포함되었을 때는 최대 변위가 약 0.000005m로 수치적 오류가 발생했다고 판단함

FRICS를 포함한 시스템에서 pi변화의 최댓값이 **1.671°**, 포함하지 않은 시스템에서의 최댓값이 **1.897°**로 **11.914%**의 감소를 보임

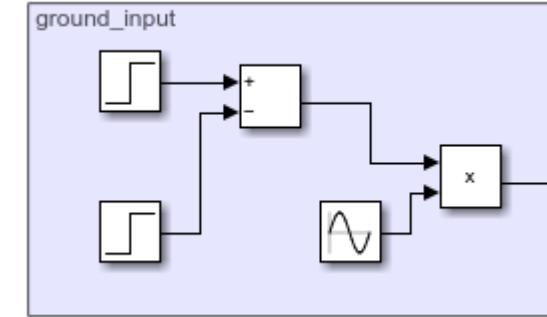
## 1

# FRICS: Front and Rear Interconnected Suspension

Full Car 와 Full Car with FRICS 를 비교

**Input :** 각각의 바퀴에 지면의 변위를 입력,  $t = 1\text{s} \sim 2\text{s}$ 에 사인파 입력

Warp(Pitch + Roll)을 FRICS가 효과적으로 감쇠해주는지를 확인하기 위해  
각 바퀴에 위상이 다르게 입력



진폭:	0.05
편향:	0
주파수(rad/s):	$10\pi$
위상(rad):	0

FL input

진폭:	0.05
편향:	0
주파수(rad/s):	$10\pi$
위상(rad):	$-0.5\pi$

FR input

진폭:	0.05
편향:	0
주파수(rad/s):	$10\pi$
위상(rad):	$-\pi$

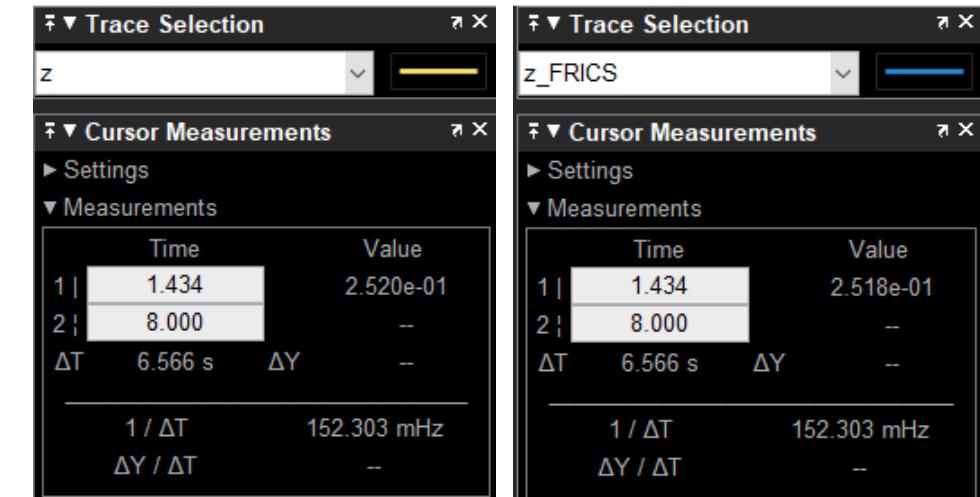
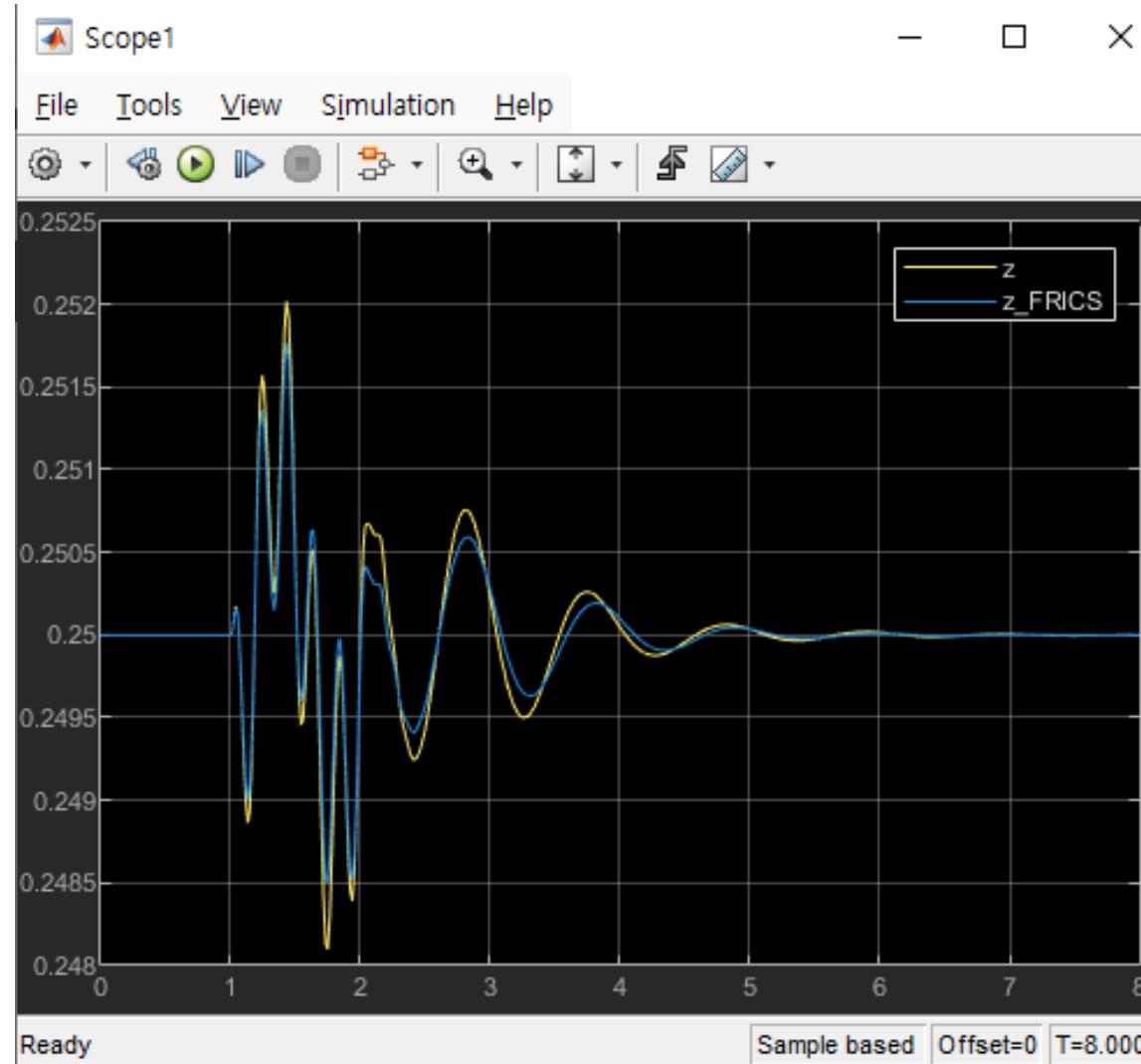
RL input

진폭:	0.05
편향:	0
주파수(rad/s):	$10\pi$
위상(rad):	$-1.5\pi$

RR input

# FRICS: Front and Rear Interconnected Suspension

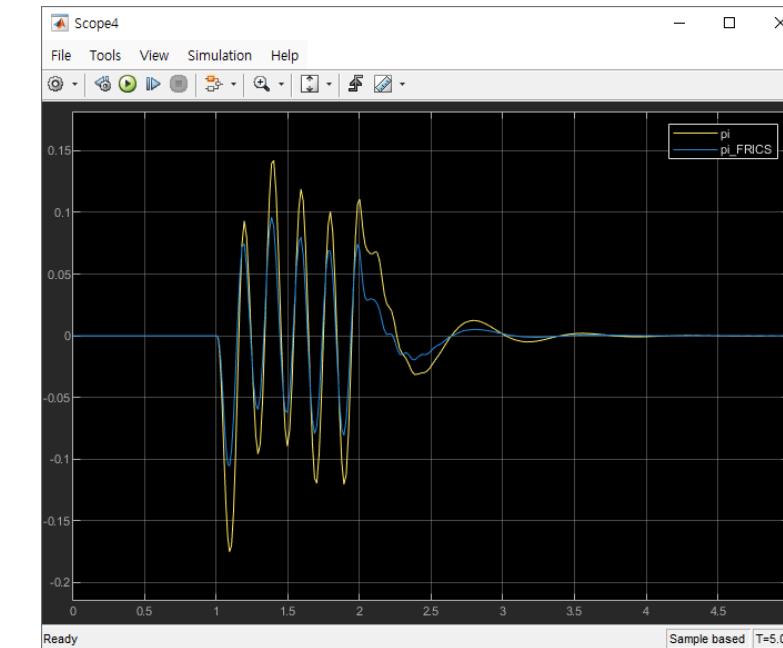
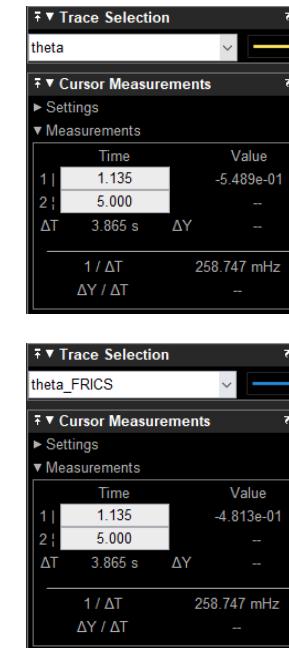
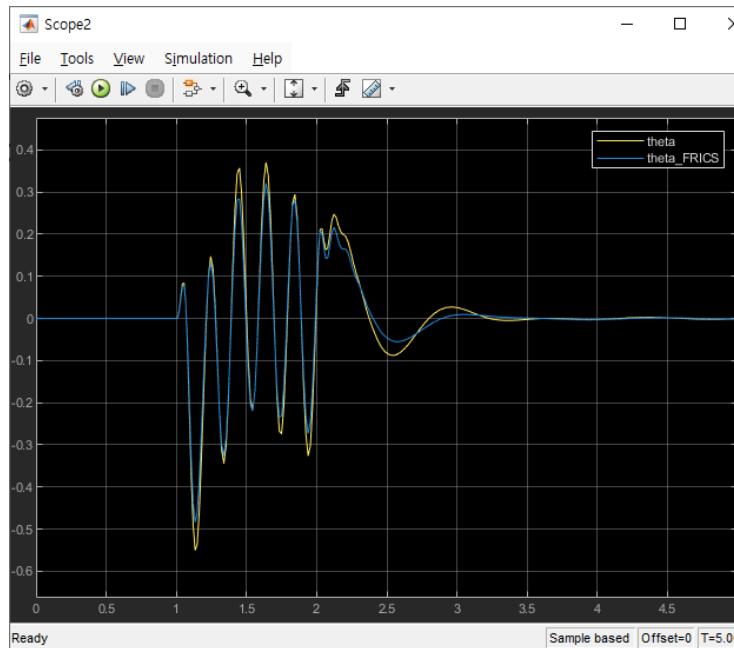
Warp(Pitch + Roll) 상황 - z변위



FRICS를 포함한 시스템에서 z변위의 최댓값이 0.0018m,  
포함하지 않은 시스템에서의 최댓값이 0.002m로  
10%의 감소를 보임

# FRICS: Front and Rear Interconnected Suspension

## Warp(Pitch + Roll) 상황 – theta & pi



FRICS를 포함한 시스템에서 theta변화의 최댓값이  $0.4813^\circ$ ,  
포함하지 않은 시스템에서의 최댓값이  $0.5489^\circ$ 로  
**12.315%**의 감쇠를 보임

FRICS를 포함한 시스템에서 theta변화의 최댓값이  $0.1048^\circ$ ,  
포함하지 않은 시스템에서의 최댓값이  $0.1749^\circ$ 로  
**40.08%**의 감쇠를 보임

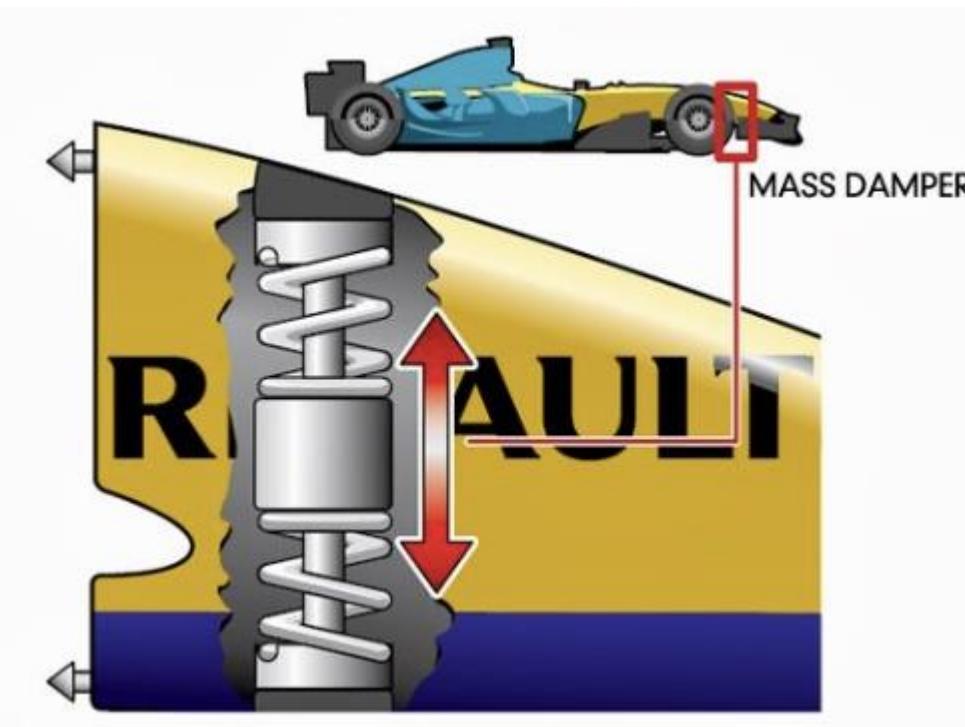


3

# Mass Damper

## 3

## Mass Damper

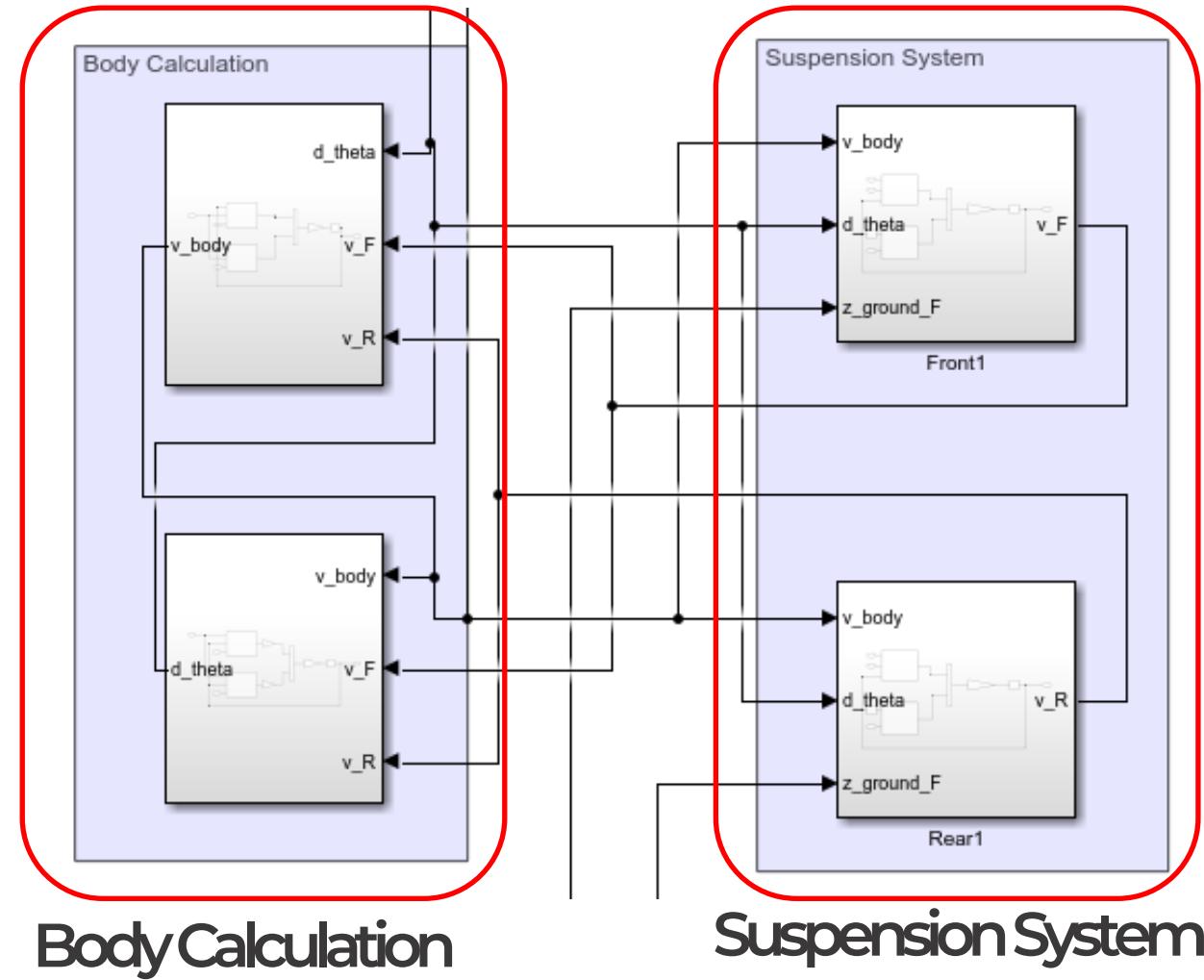


Mass Damper : 진동을 상쇄시키기 위한 장치

가속 & 제동 시 전방 하중의 이동에 따른 Pitch 변화 감소

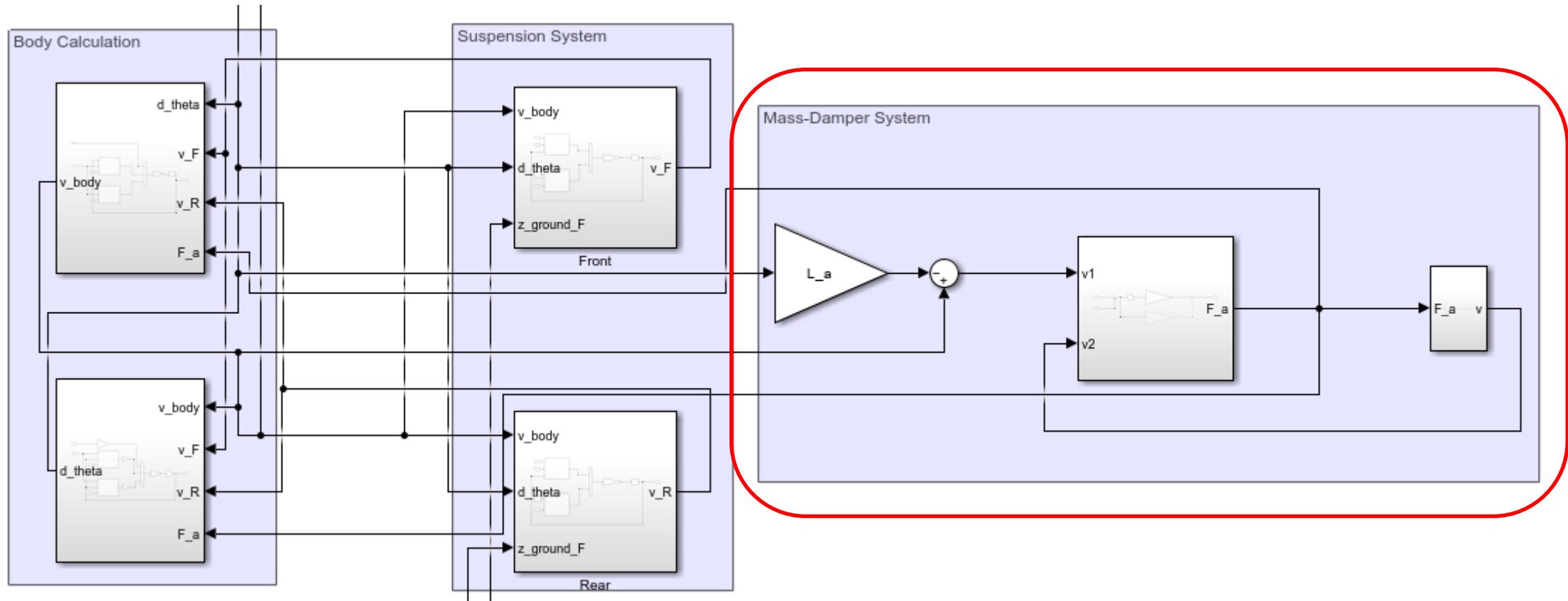
지상고 일정하게 유지  
→ Downforce 일정하게 유지, 안정성 향상

# 3 Mass Damper – Half Car Model



## 3

## Mass Damper



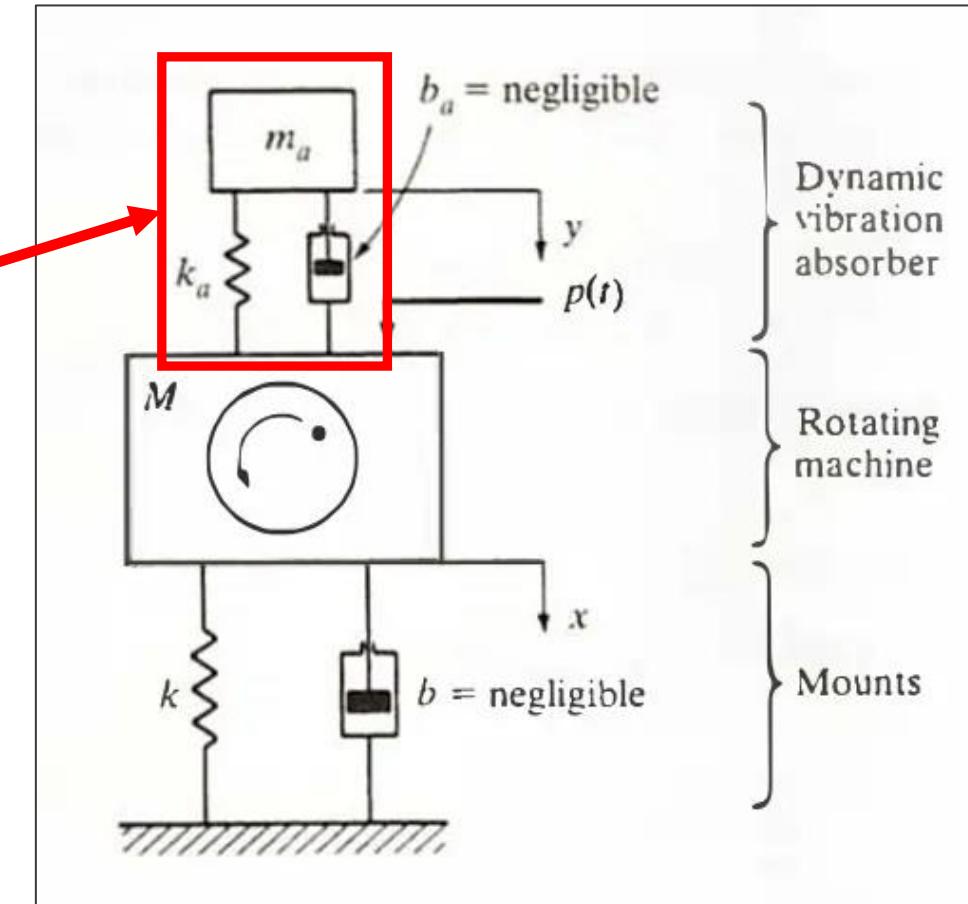
Half-Car Model

+

Mass Damper

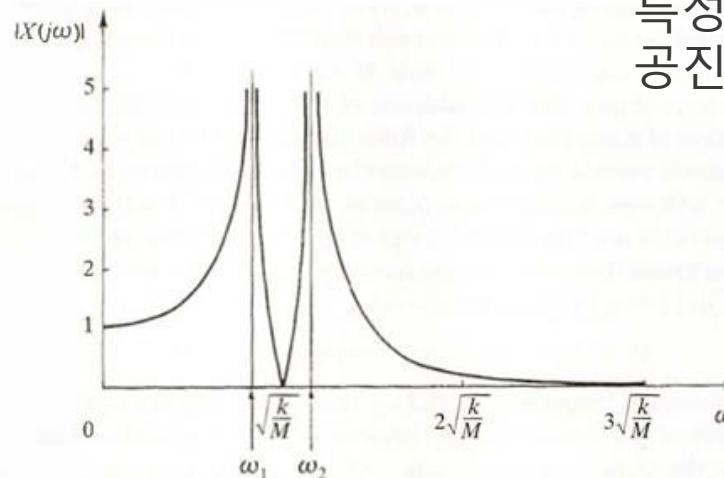
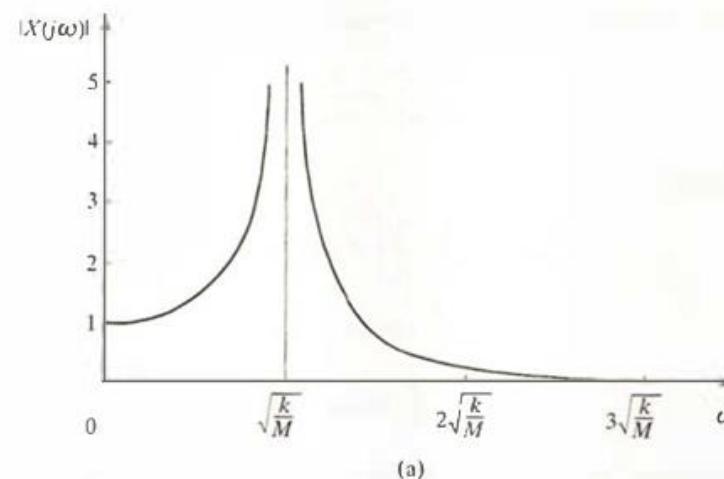
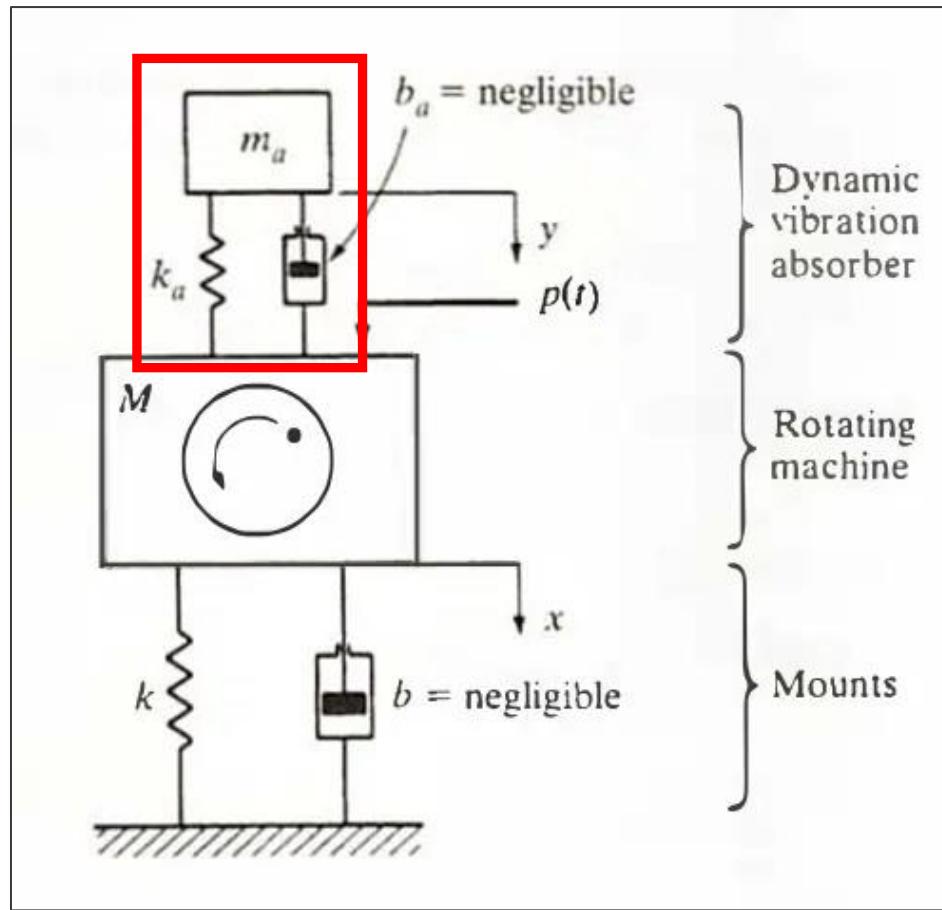
## 3

## Mass Damper



## 3

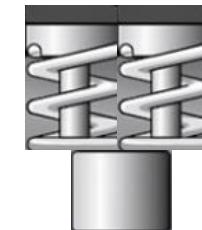
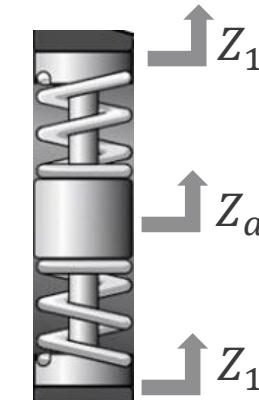
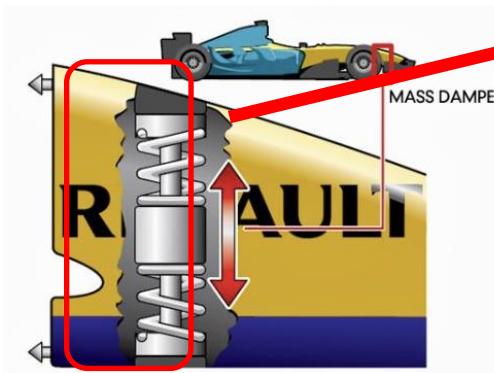
## Mass Damper



특정 주파수에서의  
공진을 대폭 줄여줌

## 3

# Mass Damper – Modeling



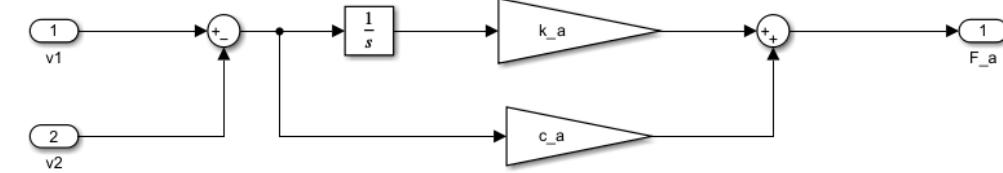
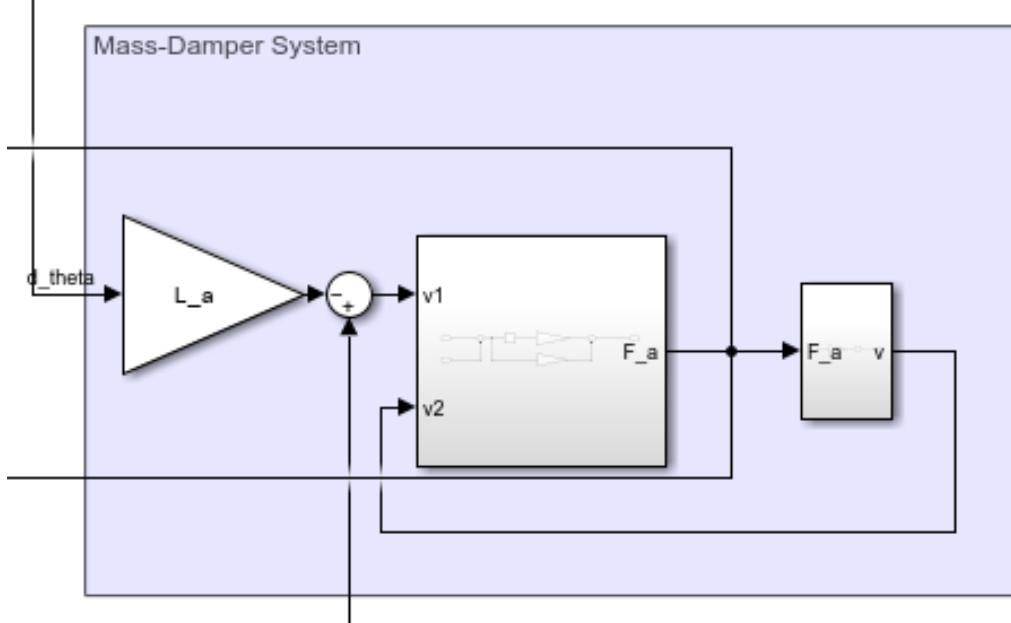
$$m_a a_a = k_1(Z_1 - Z_a) + k_2(Z_1 - Z_a) + c_1(Z_1 - Z_a) + c_2(Z_1 - Z_a)$$

$$m_a a_a = (k_1 + k_2)(Z_1 - Z_a) + (c_1 + c_2)(Z_1 - Z_a)$$

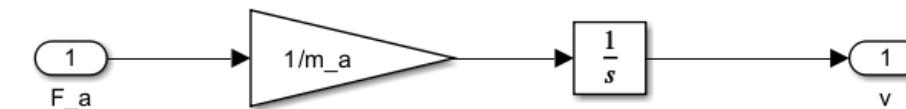
$$m_a a_a = k_{eq}(Z_1 - Z_a) + c_{eq}(Z_1 - Z_a),$$
$$k_{eq} = k_1 + k_2, \quad c_{eq} = c_1 + c_2$$

## 3

## Mass Damper



각 속도에 무게 중심에서  
Mass Damper까지의 거리( $L_a$ )를 곱해  $v(v1)$ 를 입력,  
이를 통해 Mass Damper에서의 힘( $F_a$ ) 출력



위에서 구한 힘( $F_a$ )을 입력,  
이를 통해 Mass Damper의 z방향 속도 출력

## 3

## Mass Damper

시스템 해석 활용

4개의 subsystem : body ( $x_s, \theta_s$ ), tire( $x_{u1}, x_{u2}$ )  
에서의 식을 통합하여 matrix 형태로 정리

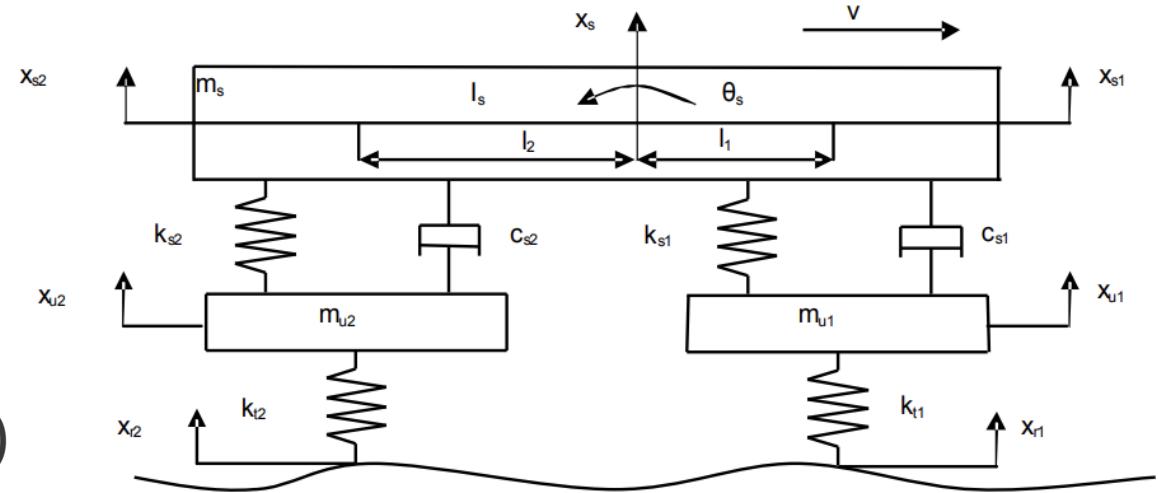


Figure 1. The half-car model of the vehicle.

$$X = [x_s \quad \theta_s \quad x_{u1} \quad x_{u2}]^T$$

$$\begin{bmatrix} m_s & 0 & 0 & 0 \\ 0 & I_s & 0 & 0 \\ 0 & 0 & m_{u1} & 0 \\ 0 & 0 & 0 & m_{u2} \end{bmatrix} \ddot{X} + \begin{bmatrix} c_{s1} + c_{s2} & -l_1 c_{s1} + l_2 c_{s2} & -c_{s1} & -c_{s2} \\ -l_1 c_{s1} + l_2 c_{s2} & l_1^2 c_{s1} + l_2^2 c_{s2} & l_1 c_{s1} & -l_2 c_{s2} \\ -c_{s1} & l_1 c_{s1} & c_{s1} & 0 \\ -c_{s2} & -l_2 c_{s2} & 0 & c_{s2} \end{bmatrix} \dot{X}$$

$$+ \begin{bmatrix} k_{s1} + k_{s2} & -l_1 k_{s1} + l_2 k_{s2} & -k_{s1} & -k_{s2} \\ -l_1 k_{s1} + l_2 k_{s2} & l_1^2 k_{s1} + l_2^2 k_{s2} & l_1 k_{s1} & -l_2 k_{s2} \\ -k_{s1} & l_1 k_{s1} & k_{s1} + k_{t2} & 0 \\ -k_{s2} & -l_2 k_{s2} & 0 & k_{s2} + k_{t2} \end{bmatrix} X = \begin{bmatrix} 0 \\ 0 \\ k_{t1} x_{r1} \\ k_{t2} x_{r2} \end{bmatrix}$$

## 3

# Mass Damper

MATLAB를 활용하여

## Natural Frequency 구함

명령 창

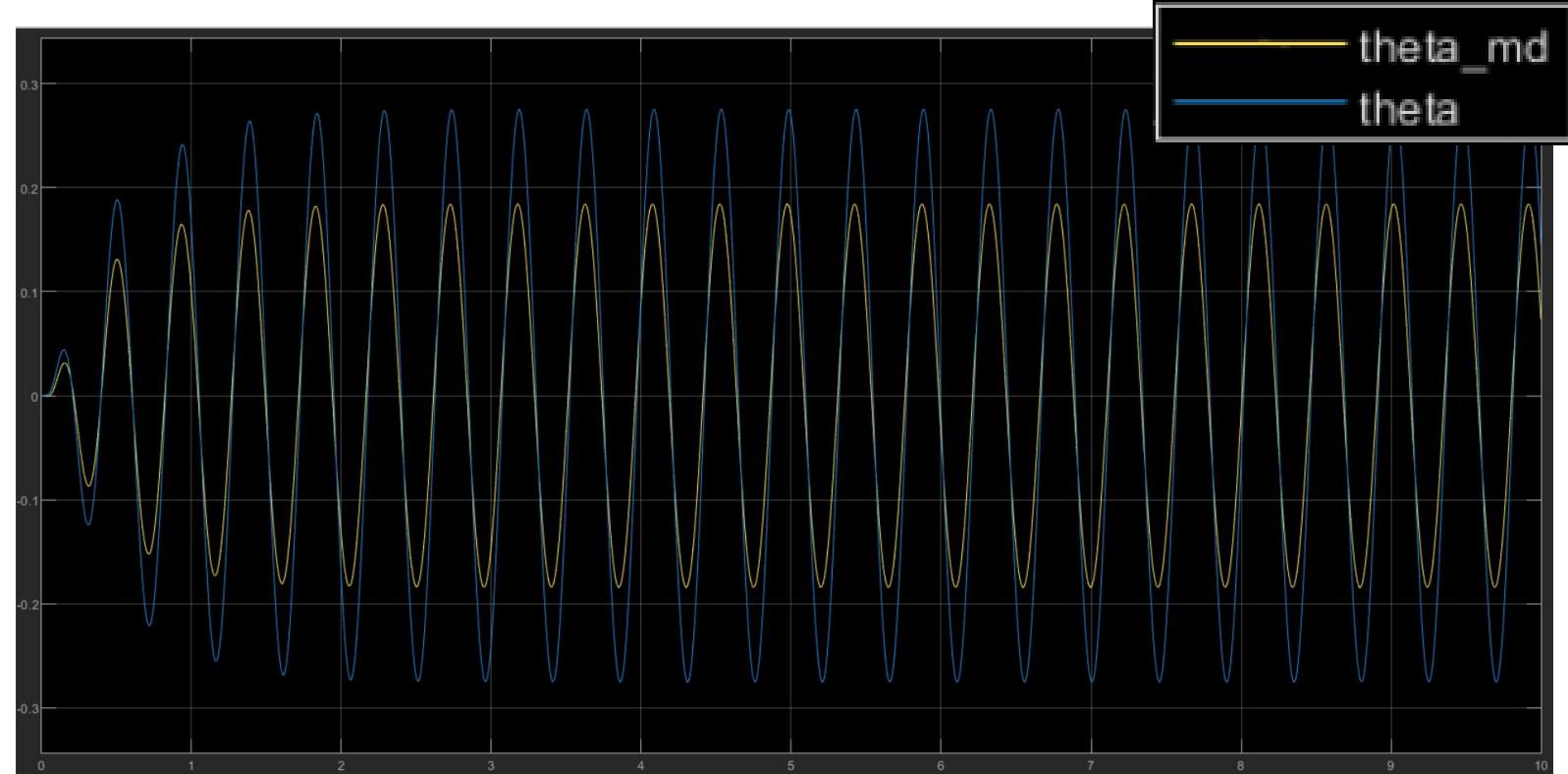
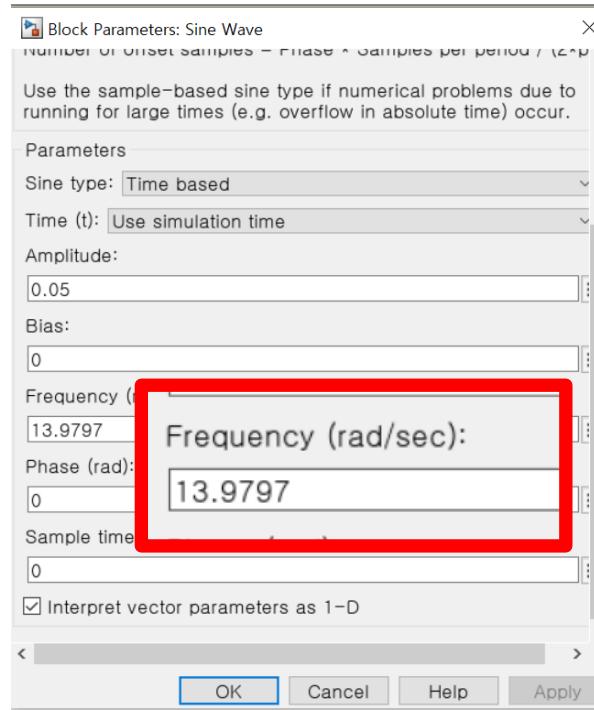
```
Damped Natural Frequencies (rad/s):
365.4438
248.1517
95.6587
62.8427
13.9791
13.9791
22.4966
22.4966
```

The screenshot shows a MATLAB code editor window with a script file named 'Natural\_Frequency.m'. The code calculates natural frequencies for a system with two masses and two springs. It defines matrices [M], [C], and [K], performs state-space formulation, and extracts damped natural frequencies and damping ratios.

```
Natural_Frequency.m
1 clc;clear;close all;
2 ms = 798; Is = 819; mu1 = 12; mu2 = 12;
3 l1 = 1.6; l2 = 1.5;
4 cs1 = 4000; cs2 = 5000;
5 ks1 = 110000; ks2 = 120000; ku1 = 200000; ku2 = 200000;
6 % Define the matrices
7 % [M] matrix
8 M_matrix = [ms 0 0 0;
9     0 Is 0 0;
10    0 0 mu1 0;
11    0 0 0 mu2];
12 % [C] matrix
13 C = [cs1+cs2 -l1*cs1+l2*cs2 -cs1 -cs2;
14     -l1*cs1+l2*cs2 l1^2*cs1+l2^2*cs2 l1*cs1 -l2*cs2;
15     -cs1 l1*cs1 cs1 0;
16     -cs2 -l2*cs2 0 cs2];
17 % [K] matrix
18 K = [ks1+ks2 -l1*ks1+l2*ks2 -ks1 -ks2;
19     -l1*ks1+l2*ks2 l1^2*ks1+l2^2*ks2 l1*ks1 -l2*ks2;
20     -ks1 l1*ks1 ks1+ku1 0;
21     -ks2 -l2*ks2 0 ks2+ku2];
22 % State-space formulation
23 A = [zeros(size(M_matrix)), eye(size(M_matrix));
24     -M_matrix\K, -M_matrix\C];
25 eigenvalues = eig(A); % Complex eigenvalues
26
27 % Extract damped natural frequencies and damping ratios
28 damped_natural_frequencies = abs(eigenvalues); % Magnitude of eigenvalues
29
30 % Display results
31 disp('Damped Natural Frequencies (rad/s):');
32 disp(damped_natural_frequencies);
```

## 3

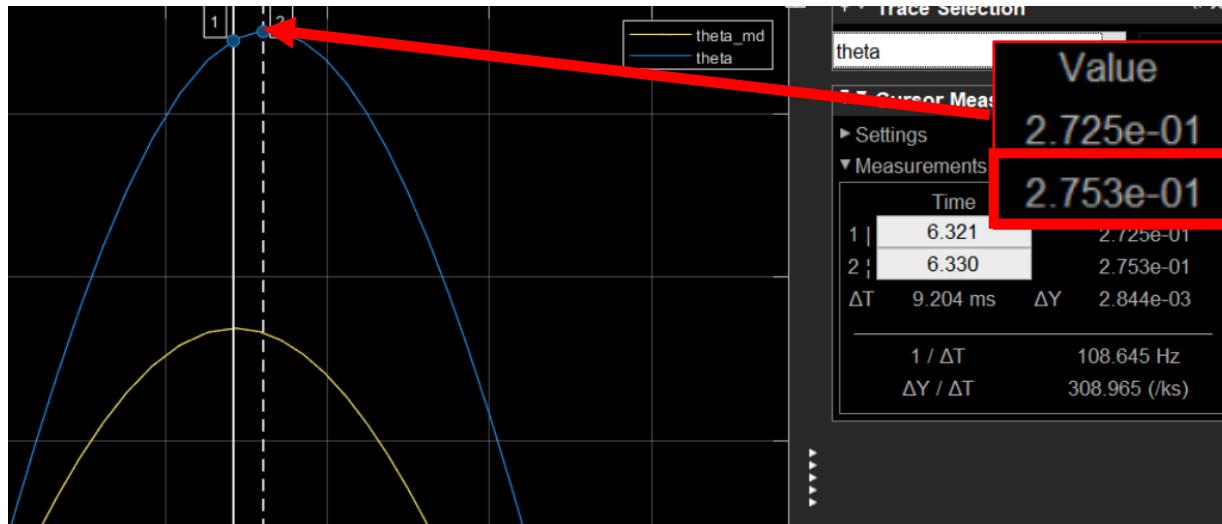
# Mass Damper



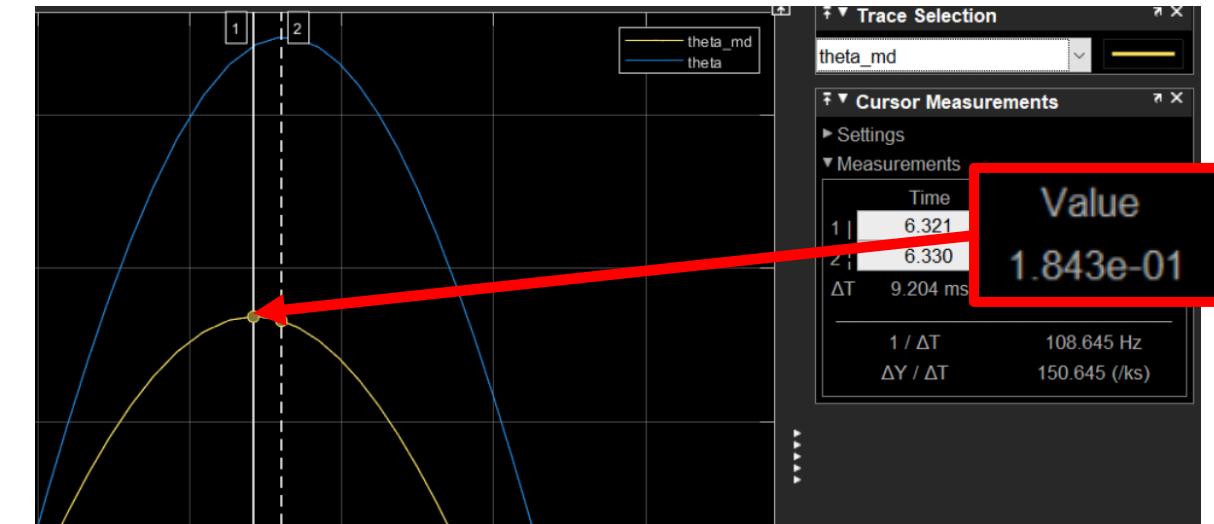
공진 주파수  $\omega = 13.9797 \text{ rad/sec}$ 에서 mass damper에 의해 진폭이 감소함을 볼 수 있다

## 3

# Mass Damper

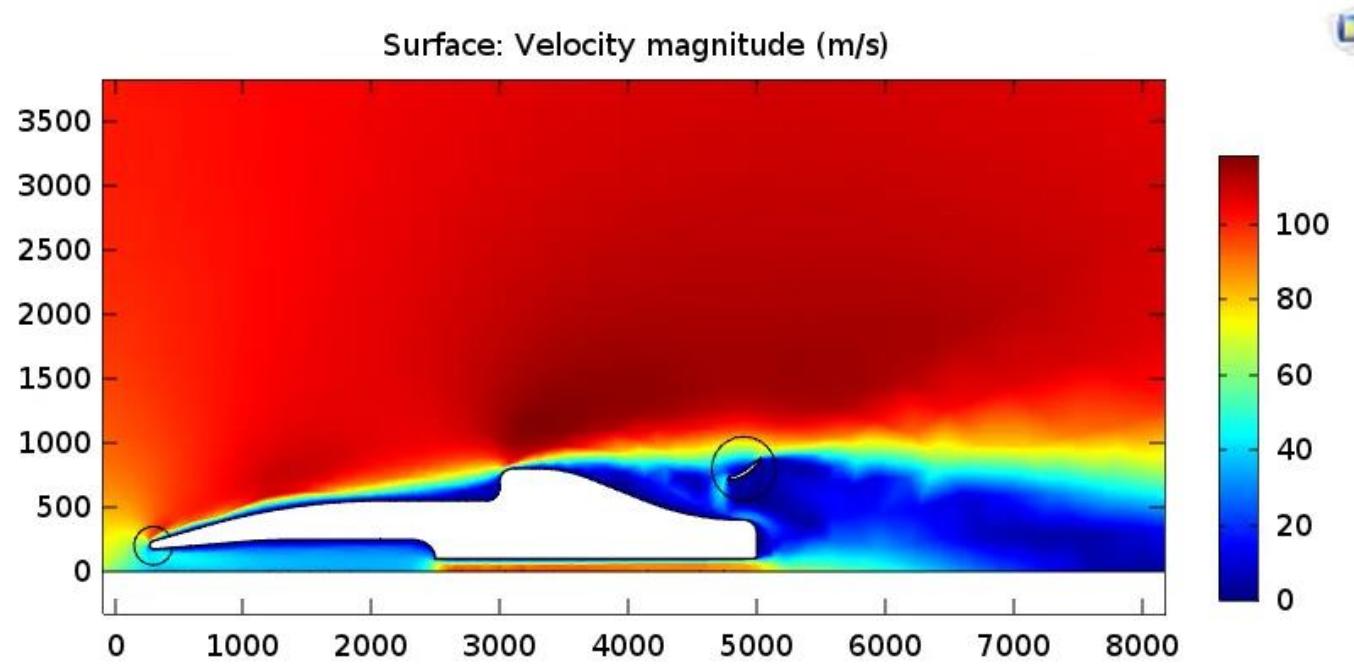


Mass damper가 없는 모델의 진폭:  $0.2753^\circ$



Mass damper가 있는 모델의 진폭:  $0.1843^\circ$

- 약  $0.1^\circ$  의 차이
- 비슷한 범위에서 차체의 pitch가  
응력에 미치는 영향 분석



4

# Aero Dynamics

고작  $0.1^\circ$  보정을 위해 복잡한 장치들이 필요했을까?

# Aero Dynamics – Comsol Settings

File ▾ Home Definitions Geometry Materials Physics Mesh Study Results

### Select Space Dimension

3D    2D Axisymmetric    2D    1D Axisymmetric    1D    0D

### Select Physics

Fluid-Structure Interaction (fsi)  
Solid Mechanics (solid)  
Beam (beam)  
AC/DC  
Acoustics  
Chemical Species Transport  
Fluid Flow  
Single-Phase Flow  
Laminar Flow (spf)  
Fluid-Structure Interaction, Fixed Geometry  
Fluid-Structure Interaction (fsi)  
Heat Transfer  
Structural Mechanics  
Mathematics

Search Add

### Select Study

- ▲ ↗ Preset Studies
  - Stationary
  - Time Dependent
- ▷ ↗ Custom Studies
- ↗ Empty Study

Added study:



Added physics interfaces:

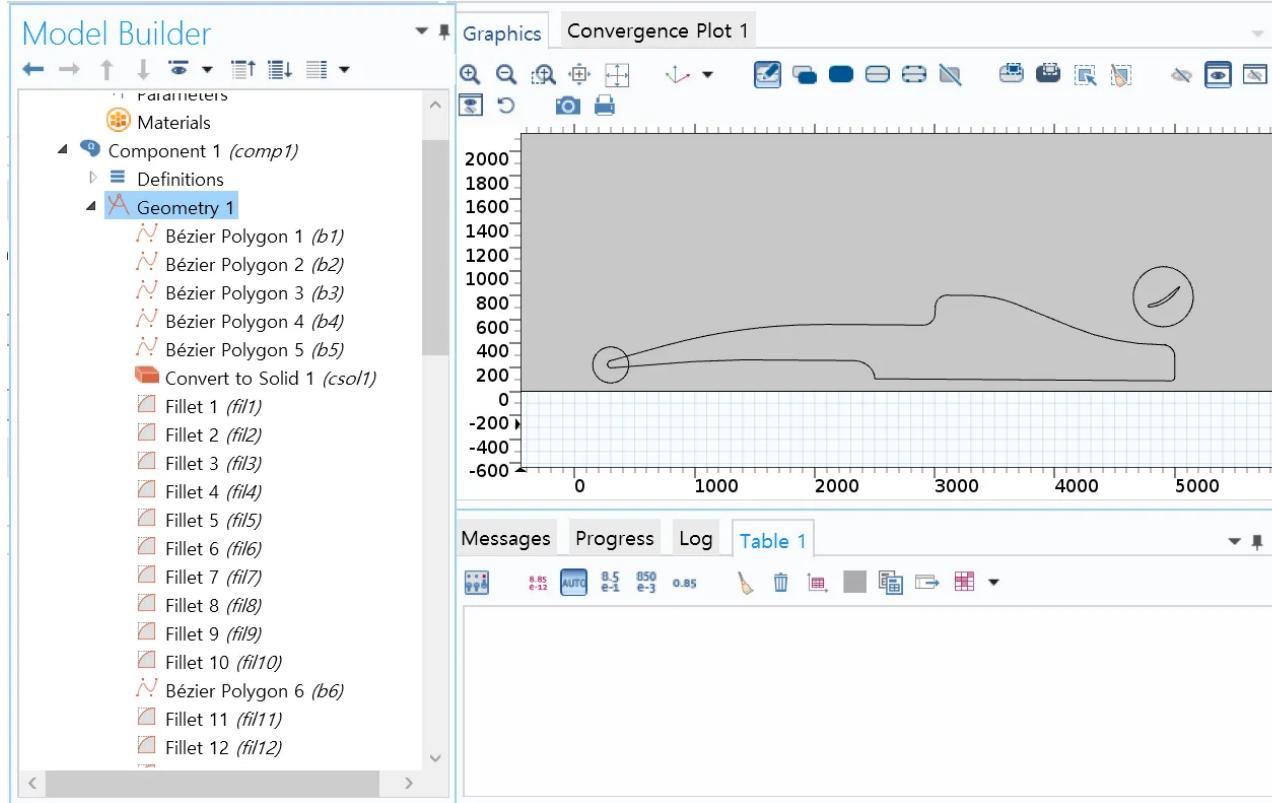


## <Study>

**2D – Laminar Flow – Stationary**

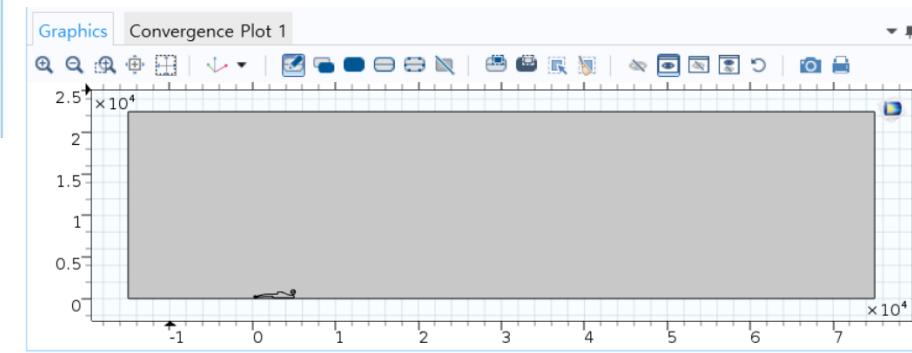
**(Turbulent Flow는 License 제한)**

# 4 Aero Dynamics – Comsol Settings

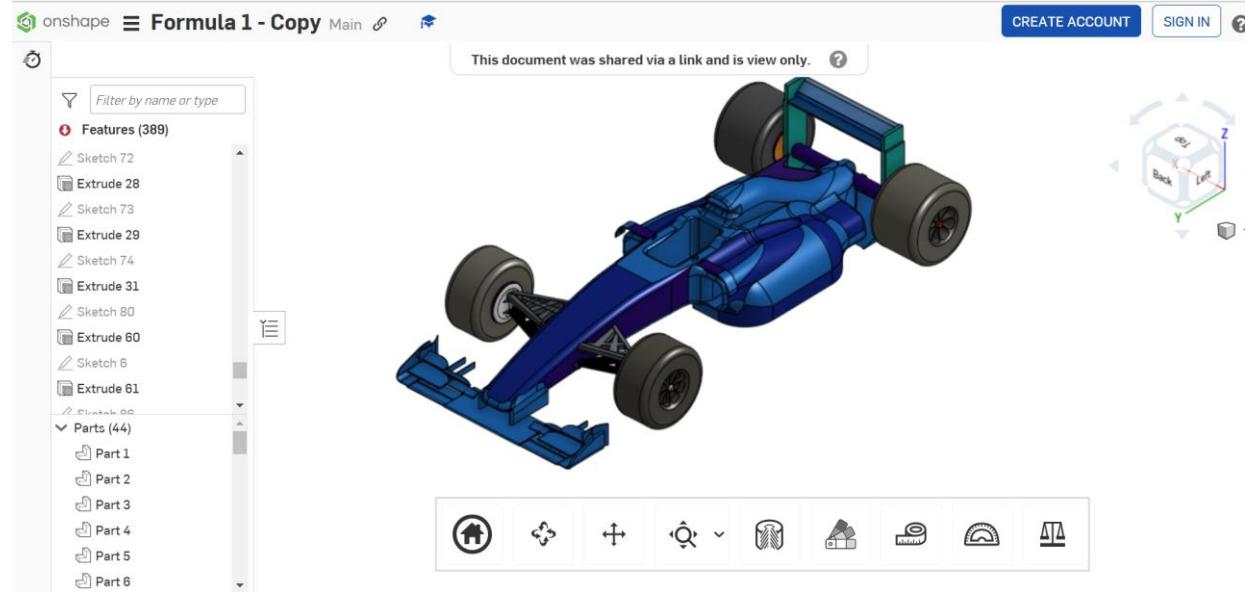


## <Geometry>

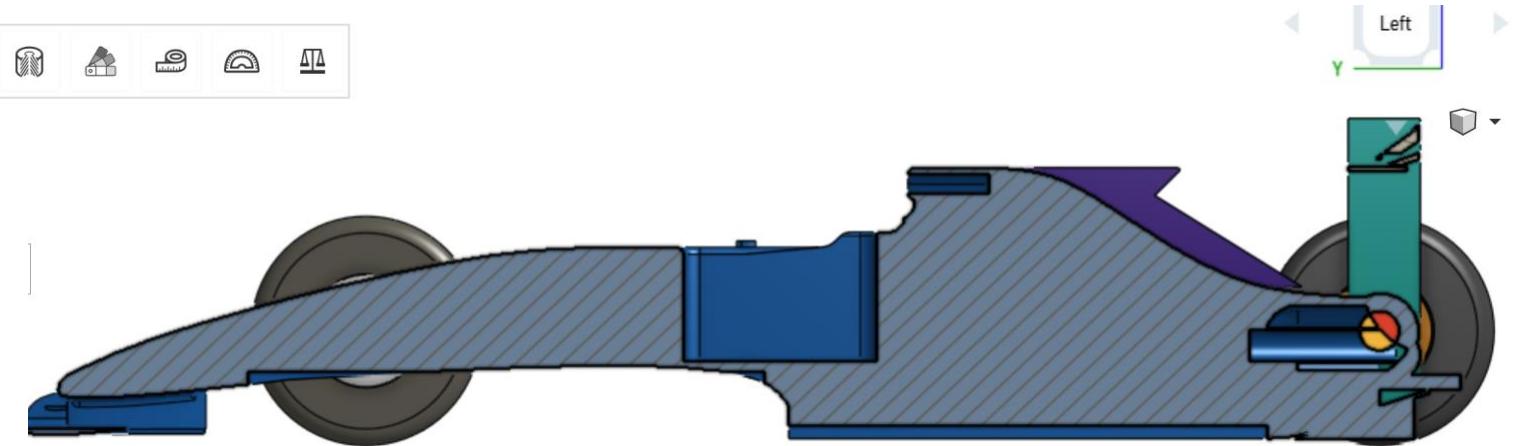
Catia로 그린 dxf파일 import  
→ 형상이 너무 복잡해짐  
→ COMSOL 상에서 그렸음



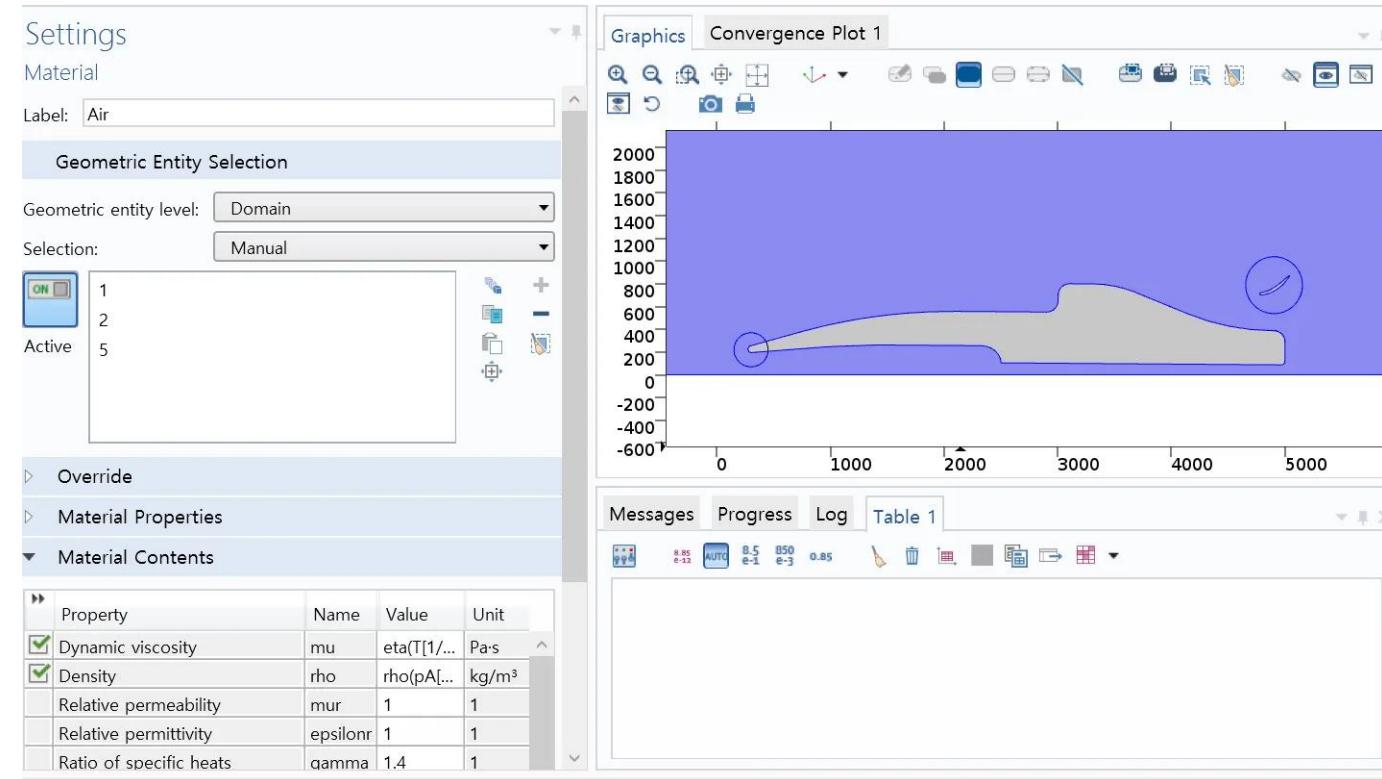
# 4 Aero Dynamics – Comsol Settings



Onshape 의 public source의 section view  
를 참고하여 형성



# 4 Aero Dynamics – Comsol Settings



<Material>  
COMSOL 내의 built-in material 중  
Air 사용

# 4 Aero Dynamics – Comsol Settings

The screenshot shows the Comsol Multiphysics software interface for a Laminar Flow simulation. A red box highlights the 'Initial Values' and 'Boundary Condition' sections.

**Laminar Flow (spf)**

- Fluid Properties 1
- Initial Values 1
- Wall 1
- Inlet 1
- Wall 2
- Outlet 1
- Wall 3

**Graphics Convergence Plot 1**

**Initial Values**

Velocity field:

$u$	100	x
	0	y

Pressure:

$p$	1 [atm]	Pa
-----	---------	----

**Boundary Condition**

Boundary condition:

No slip

**<Laminar Flow>**  
100m/s로 달린다고 가정

# 4 Aero Dynamics – Comsol Settings

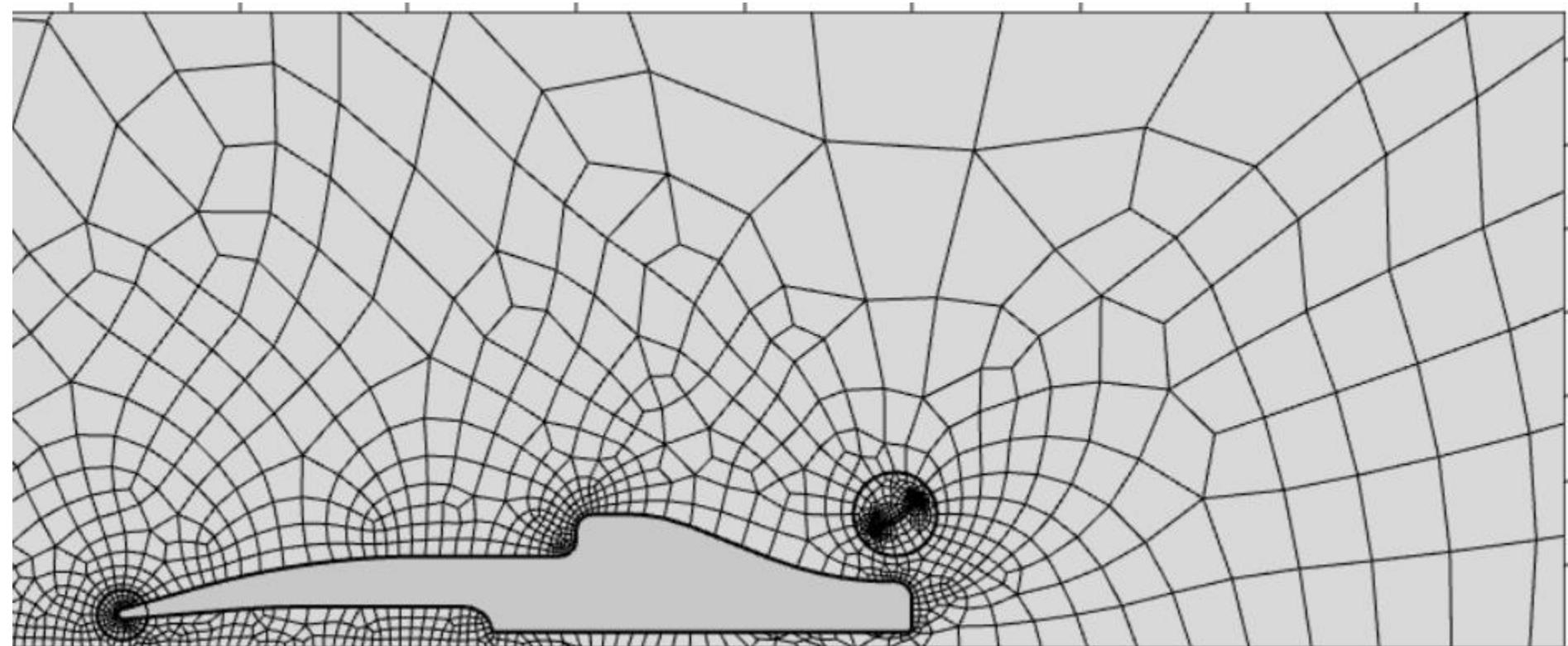


<Laminar Flow>  
100m/s로 달린다고 가정

# 4 Aero Dynamics – Comsol Settings

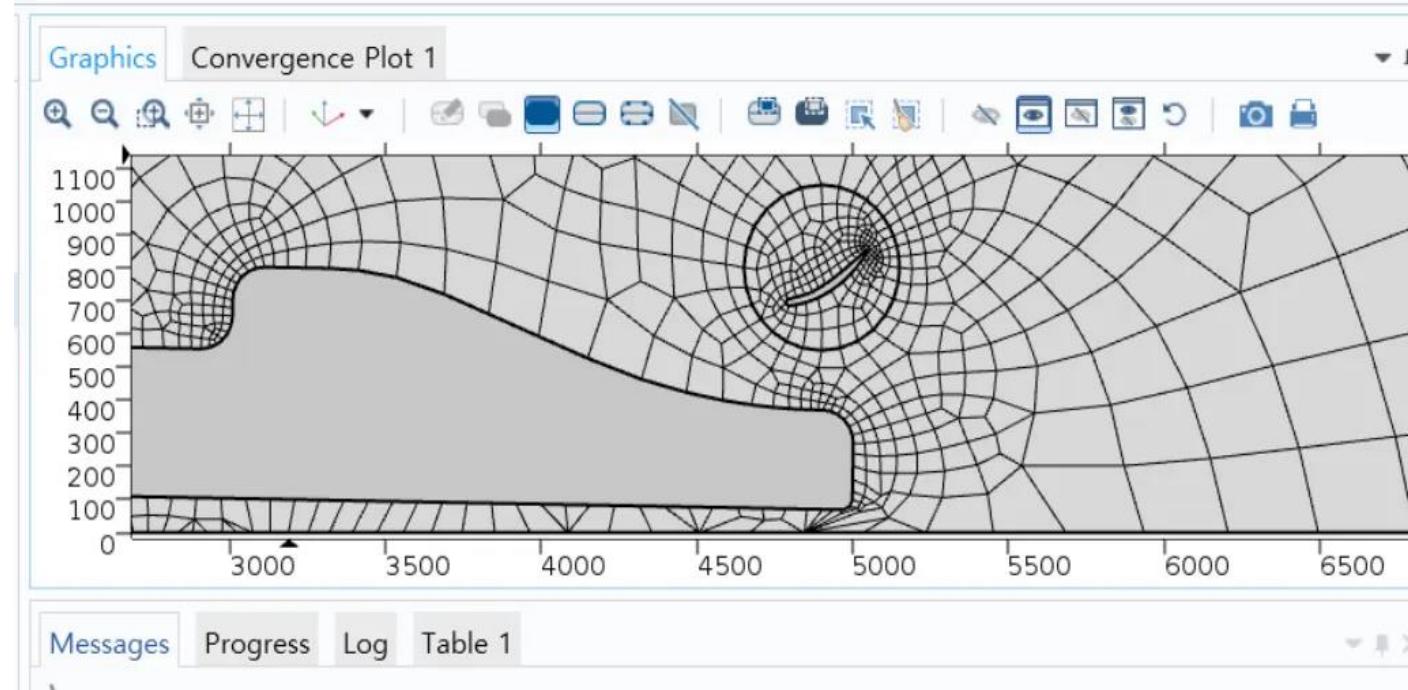
<Mesh>

- ▲ Mesh 1
- ▲ Size
- ▲ Free Quad 1
- ▲ Size 1
- ▲ Free Quad 2
- ▲ Size 1



# 4 Aero Dynamics – Comsol Settings

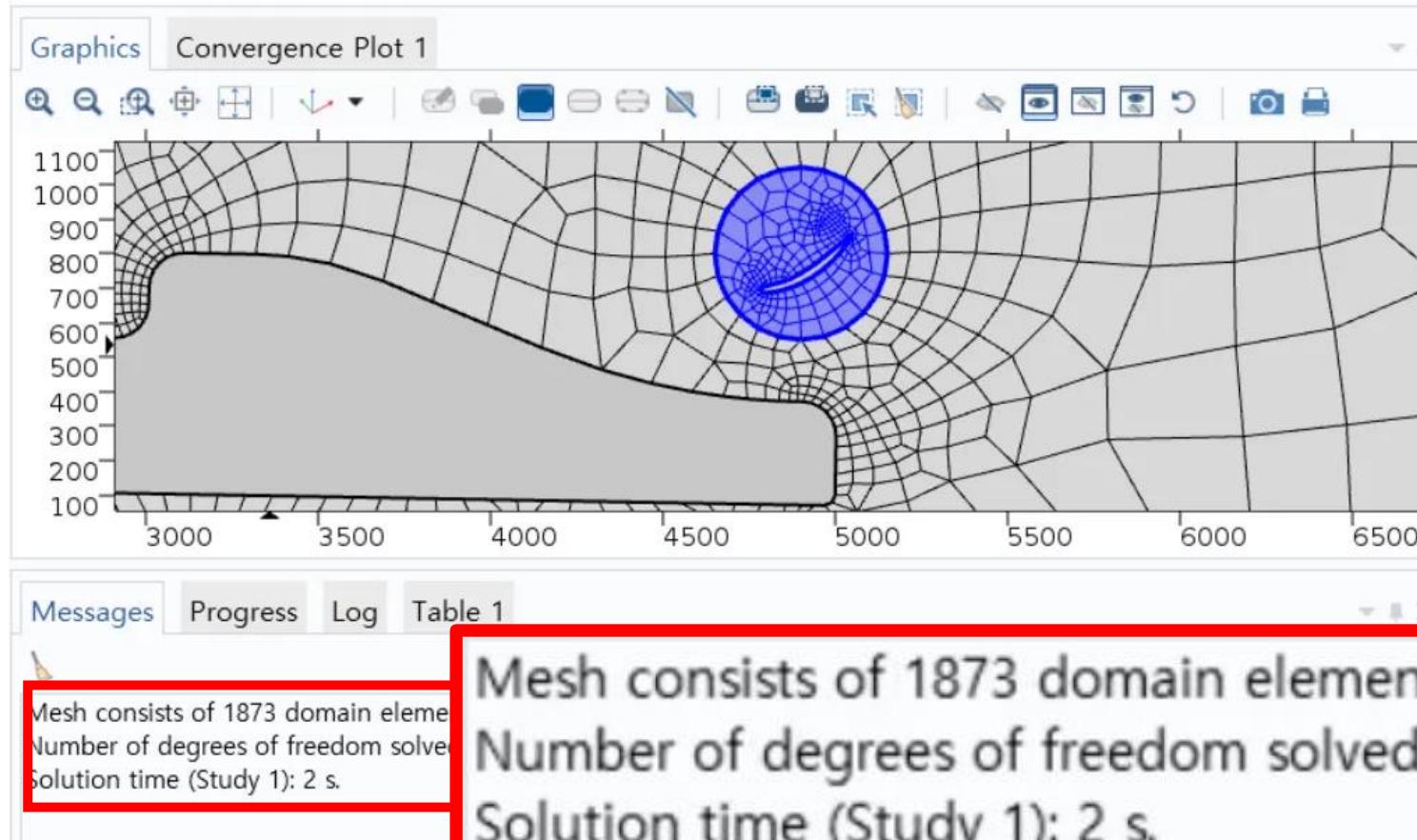
<Mesh>



Mesh consists of 1715 domain elements and 432 boundary elements.  
Number of degrees of freedom solved for: 5694.  
Solution time (Study 1): 2 s.

# 4 Aero Dynamics – Comsol Settings

## <Mesh>



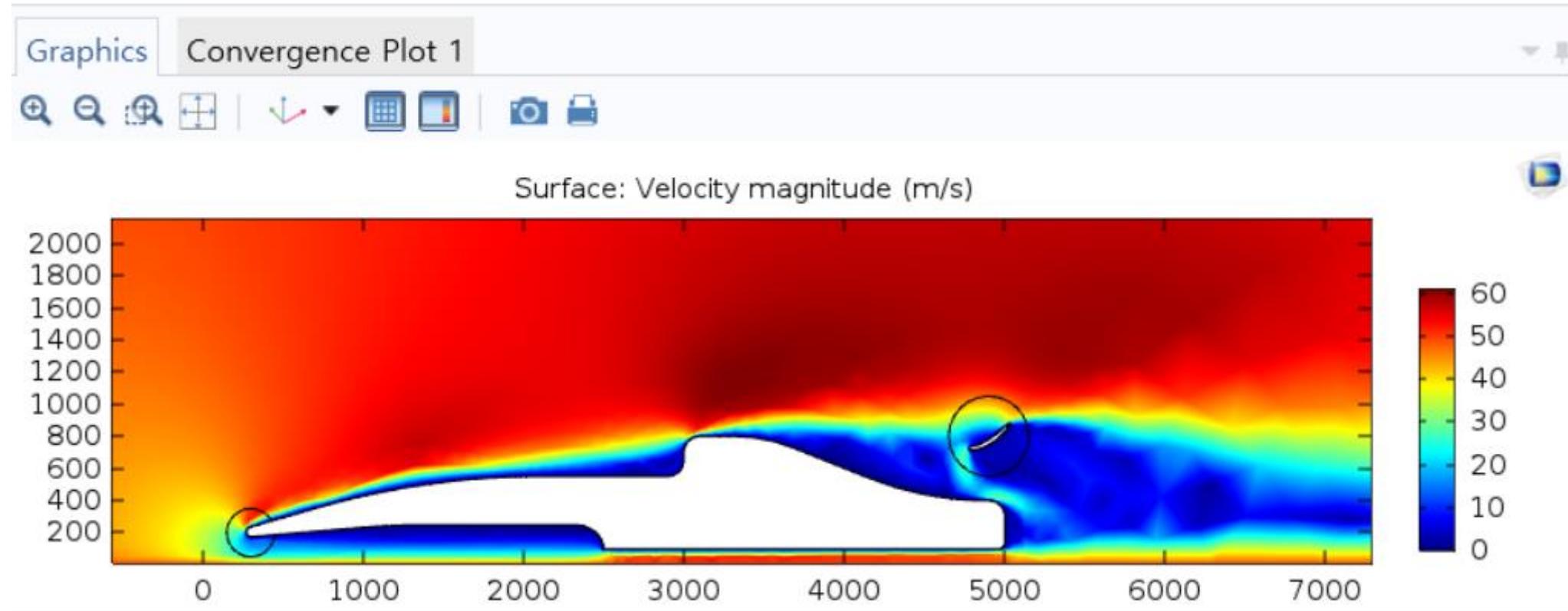
## <Mesh>

더 정확한  
**downforce**의 계산  
을 위해 **rear wing**  
부분의 **mesh**를  
**finer**하게 설정

## 4

# Aero Dynamics - Analysis

$V = 50\text{m/s}$

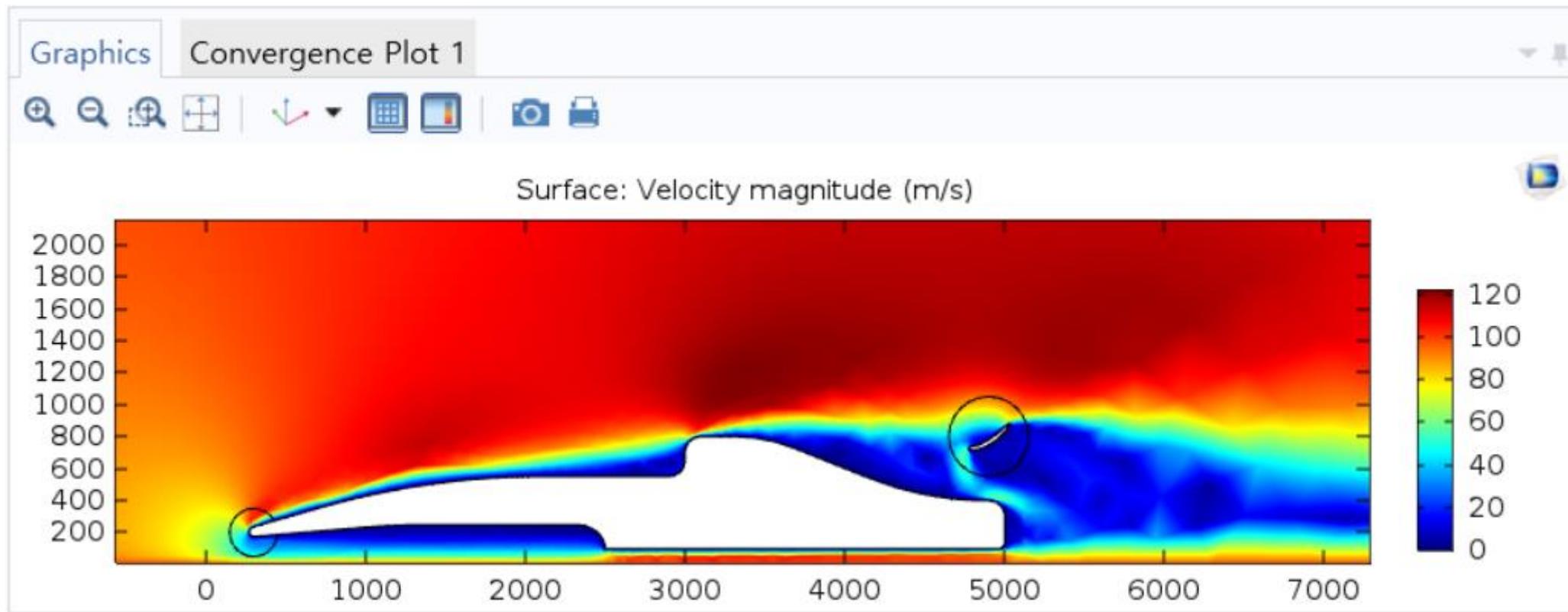


속도에 따라

## 4

# Aero Dynamics - Analysis

$V = 100\text{m/s}$

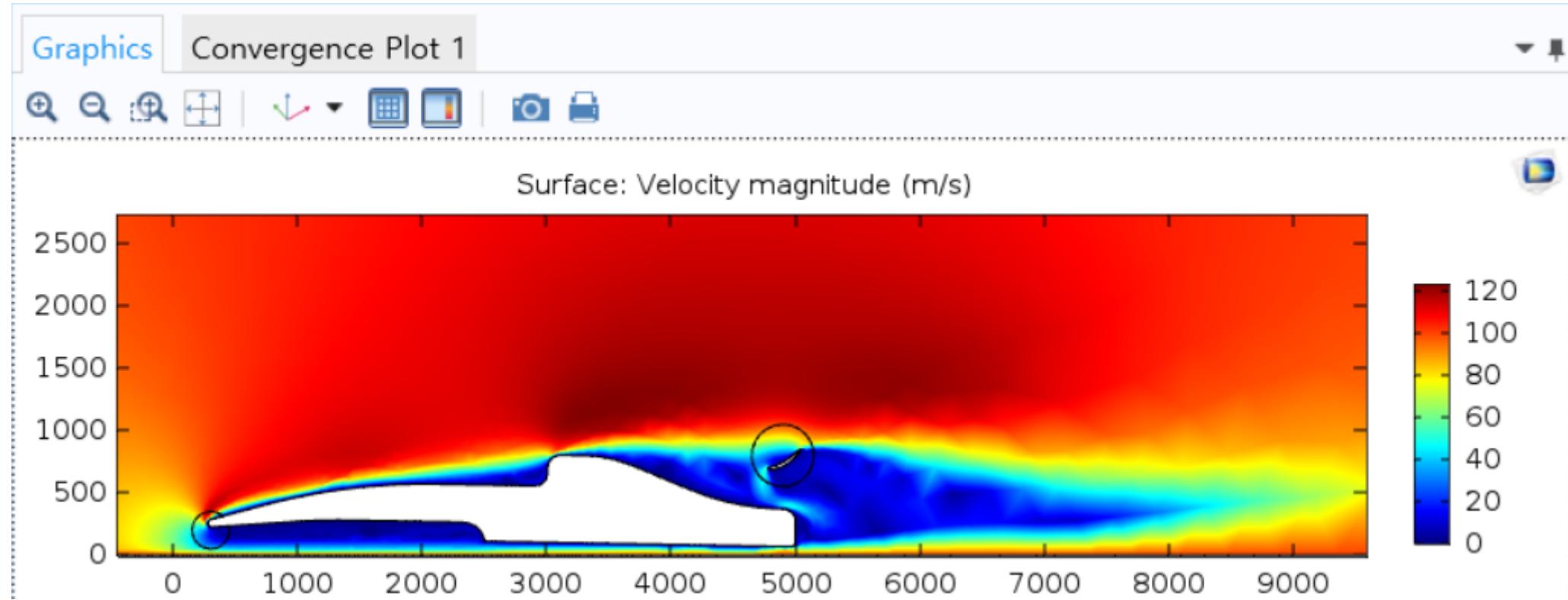


속도에 따라

## 4

# Aero Dynamics - Analysis

Pitch  $\theta$ :  $-0.3^\circ \sim 0.3^\circ$



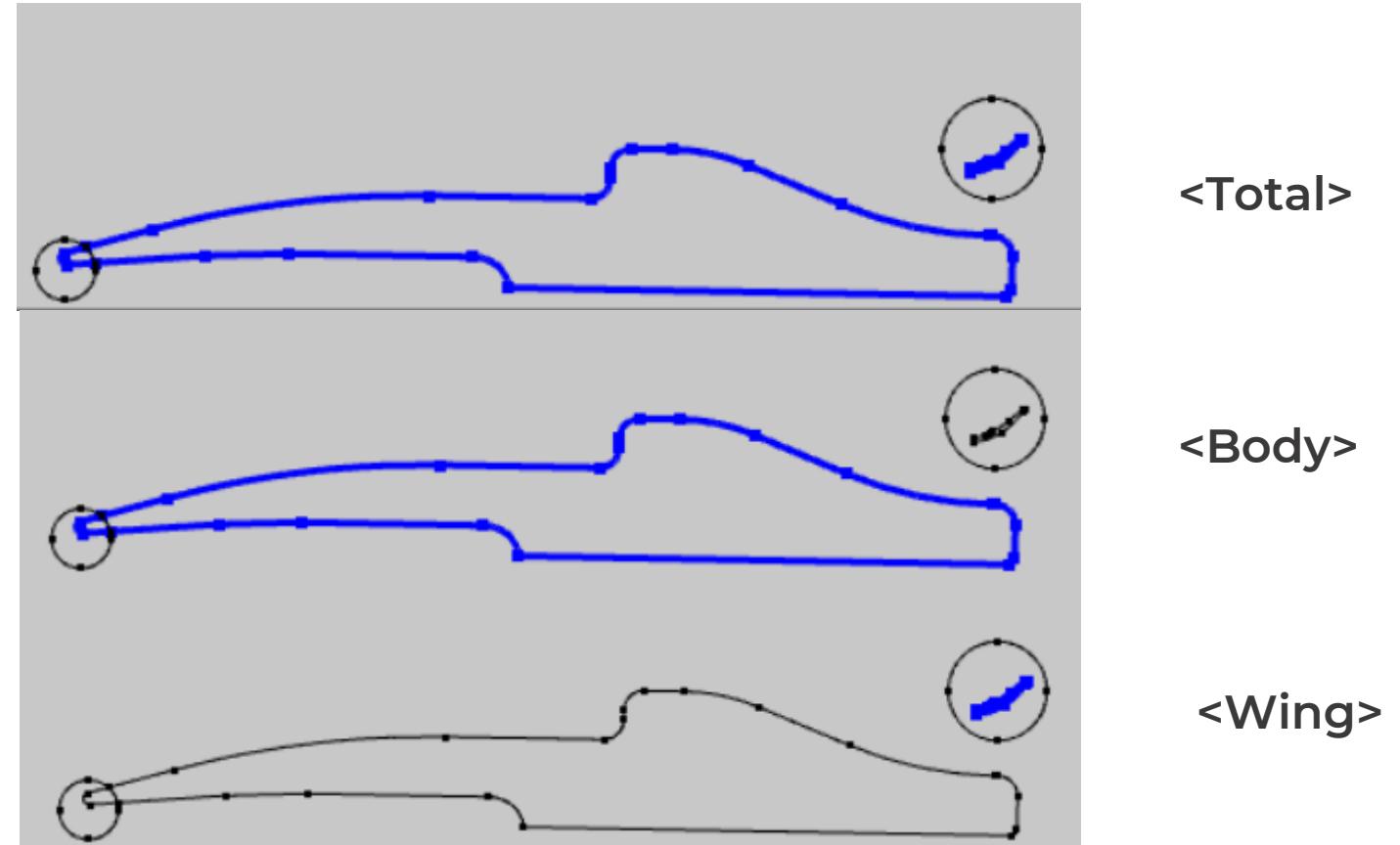
각도에 따라

## 4

# Aero Dynamics - Analysis

## Derived Values

- X-direction drag force\_total
- X-direction drag force\_body
- X-direction drag force\_wing
- Y-direction drag force\_total
- Y-direction drag force\_body
- Y-direction drag force\_wing



## 4

# Aero Dynamics - Analysis

Vehicle Speed (m/s)	Total Stress, x component(N/m)		Body Stress, x component (N/m)		Wing Stress, x component (N/m)		Total Stress, y component (N/m)		Body Stress, y component (N/m)		Wing Stress, y component (N/m)	
Pitch Angle(degree)	50	100	50	100	50	100	50	100	50	100	50	100
0	-835.49	-3341.8	-690.79	-2763	-144.7	-578.84	-4339.3	-17355	-4570.3	-18279	230.97	923.98
0.1°	-852.4	-3409.3	-691.52	-2765.8	-160.88	-643.51	-5665.4	-22661	-5922.2	-23688	256.79	1027.1
-0.1°	-836.33	-3378.8	-690.63	-2767.9	-145.7	-610.94	-7288.2	-32072	-7521.8	-33053	233.63	980.69
0.2°	-873.27	-3492.4	-705.61	-2821.1	-167.66	-671.29	-6464.5	-25864	-6729.5	-26925	265	1061.2
-0.2°	-844.76	-3378.8	-692.03	-2767.9	-152.73	-610.94	-8018.4	-32072	-8263.6	-33053	245.16	980.69
0.3°	-890.11	-3560.2	-732.89	-2931.3	-157.23	-628.87	-4229.2	-16915	-4476.4	-17904	247.23	988.88
-0.3°	-844.93	-3379.6	-697.25	-2788.9	-147.68	-590.71	-8292	-33167	-8531	-34123	239.07	956.28

# Aero Dynamics - Analysis

## Down force

Vehicle Speed (m/s)	Wing Stress, y component (N/m)	
Pitch Angle(degree)	50	100
0	230.97	923.98
0.1°	256.79	1027.1
-0.1°	233.63	980.69
0.2°	265	1061.2
-0.2°	245.16	980.69
0.3°	247.23	988.88
-0.3°	239.07	956.28

Downforce를 만드는 응력

$$1061.2 - 923.98 = 137.22 \text{ N/m}$$

0.2° 차이 → 12.94 % 차이

## Drag force

Vehicle Speed (m/s)	Total Stress, x component(N/m)	
Pitch Angle(degree)	50	100
0	-835.49	-3341.8
0.1°	-852.4	-3409.3
-0.1°	-836.33	-3378.8
0.2°	-873.27	-3492.4
-0.2°	-844.76	-3378.8
0.3°	-890.11	-3560.2
-0.3°	-844.93	-3379.6

Dragforce를 만드는 응력

$$890.11 - 835.49 = 54.62 \text{ N/m}$$

0.3° 차이 → 6.13 % 차이

Scale Modeling 시도 : 1/10 모델 활용으로 연산량 ↓ 시도

“Renolds number, Froude number 같은 dynamic viscosity를 설정한다면

1/n배로 scale된 모델에서도 같은 Cd값을 활용할 수 있게 된다” → 연산량을 획기적으로 줄일 수 있을 것으로 기대.

$$\text{prototype} \quad \text{model}$$

$$Re_p = Re_m$$

$$\frac{V_p L_p}{\nu_p} = \frac{V_m L_m}{\nu_m}$$

$$Z_m = \frac{V_m L_m}{V_p L_p} \cdot Z_p$$

$$\frac{V_m}{V_p} = \sqrt{\frac{L_m}{L_p}} = \sqrt{\frac{1}{10}}$$

$$\frac{Z_m}{Z_p} = \left(\frac{L_m}{L_p}\right)^{\frac{3}{2}}$$

동점성계수 비

속도비

Drag Coefficient.

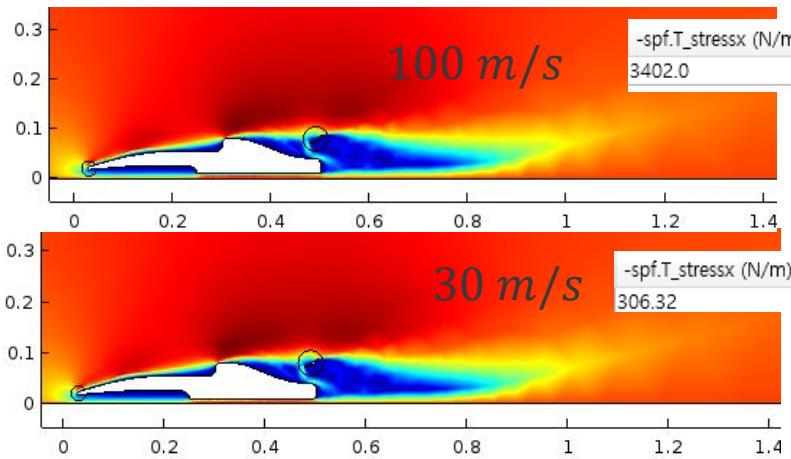
$$C_D = \frac{F_d}{\frac{1}{2} \rho V^2 A}$$

$F_d \rightarrow$  drag force

## 4

## Aero Dynamics

## Scale Modeling???



1/10 size로 scale modeling :

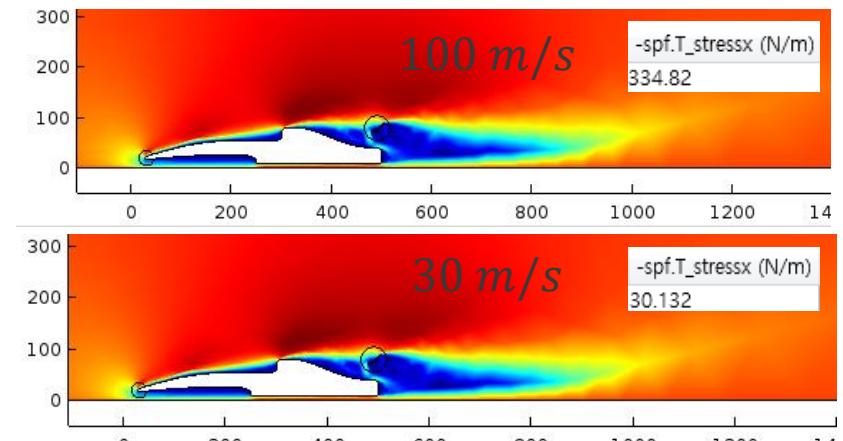
$$\text{dynamic viscosity} : \left(\frac{1}{10}\right)^{1.5} = \frac{1}{31.62} \text{ 배}$$

→ 결과 Cd는 동일



$$\text{Scale} : \frac{1}{10}$$

$$\text{Dynamic Viscosity: } \left(\frac{L_{model}}{L_{prototype}}\right)^{1.5} = \left(\frac{1}{10}\right)^{1.5} = \frac{1}{31.62}$$



	Original Model	1/10 Model
	$DOF = 6066$	$DOF = 5991$
<b>100 m/s</b>	$F_D = 3402.0 N/s$	$F_D = 334.82 N/s$
<b>30 m/s</b>	$F_D = 306.32 N/s$	$F_D = 30.132 N/s$

$F_d = C_d \frac{1}{2} \rho A v^2$  이므로, **F/length** 는 1/10배가 되어야 함. → 높은 정확도를 보임

그러나 **Mesh**수와 연산시간에 큰 변화가 없어 사용할 이유를 보여주지 못함

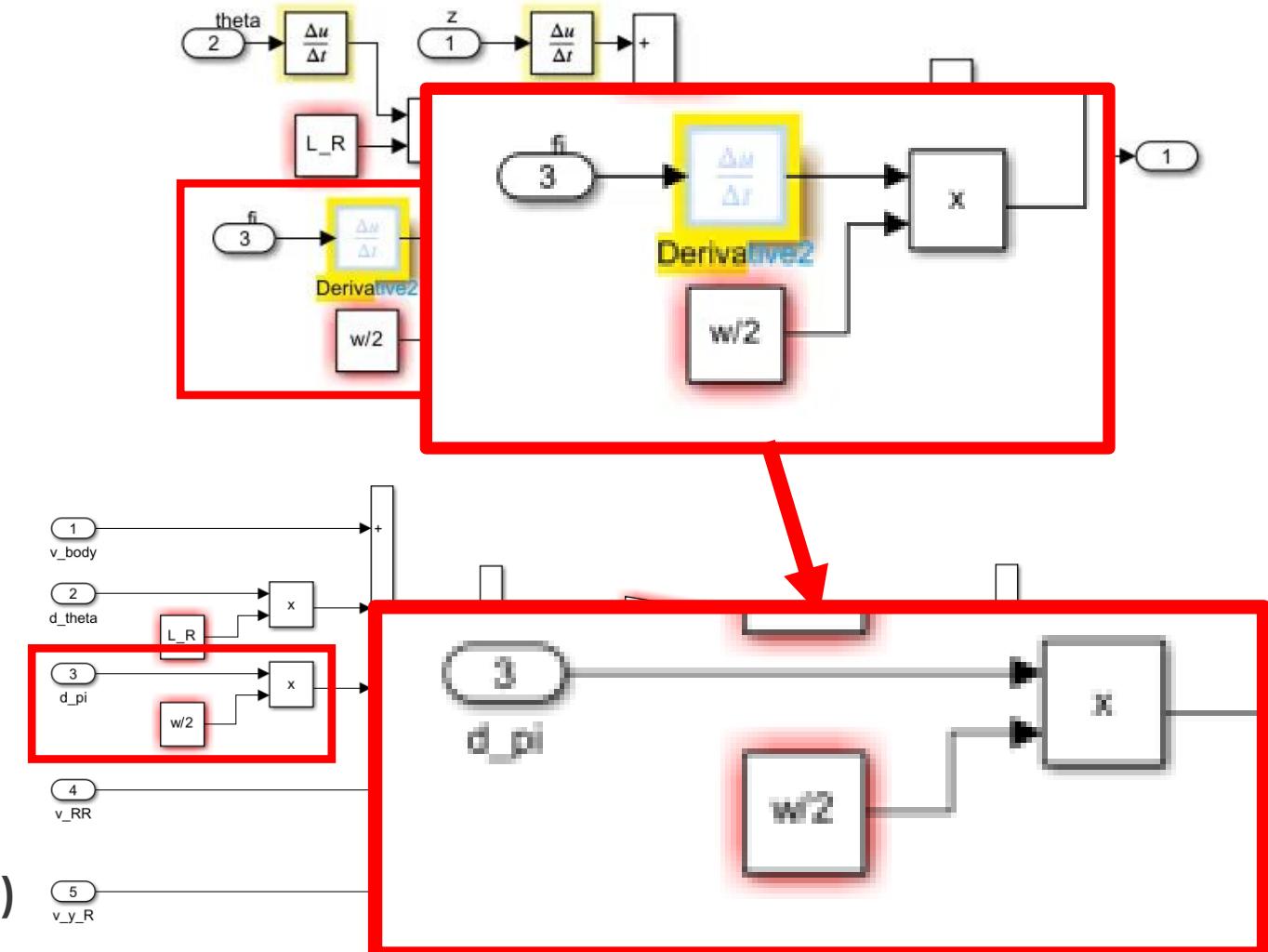
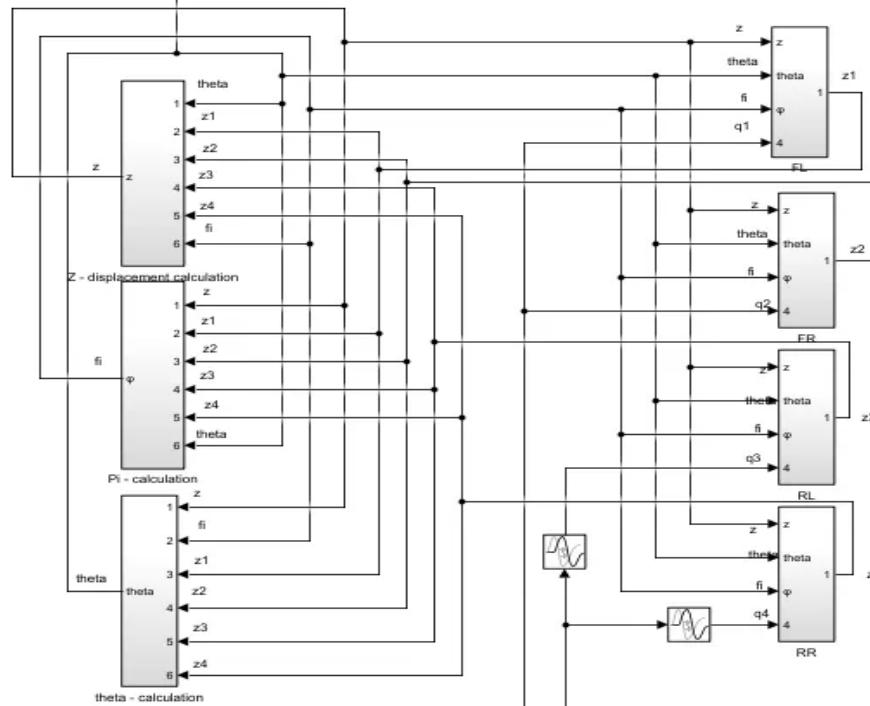
Scale Modeling???

5

## Difficulties & Reflections

## 5

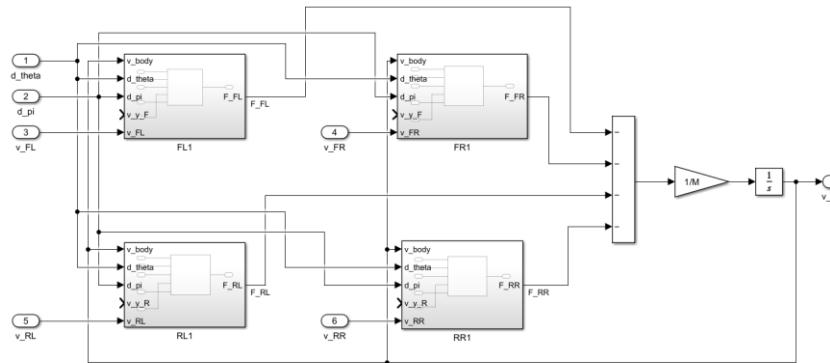
# Difficulties & Reflections – 미분기→적분기



논문대로 변위 기준의 모델링(미분기 포함)  
→ 속도 기반의 모델링(적분기 포함, 미분기 제거)

# Difficulties & Reflections – 대수 루프

Q) 왜 외부의 서스펜션 (FL, FR, RL, RR) 값을 그대로 사용하지 않고 내부에서 subsystem을 또다시 구현했는가?

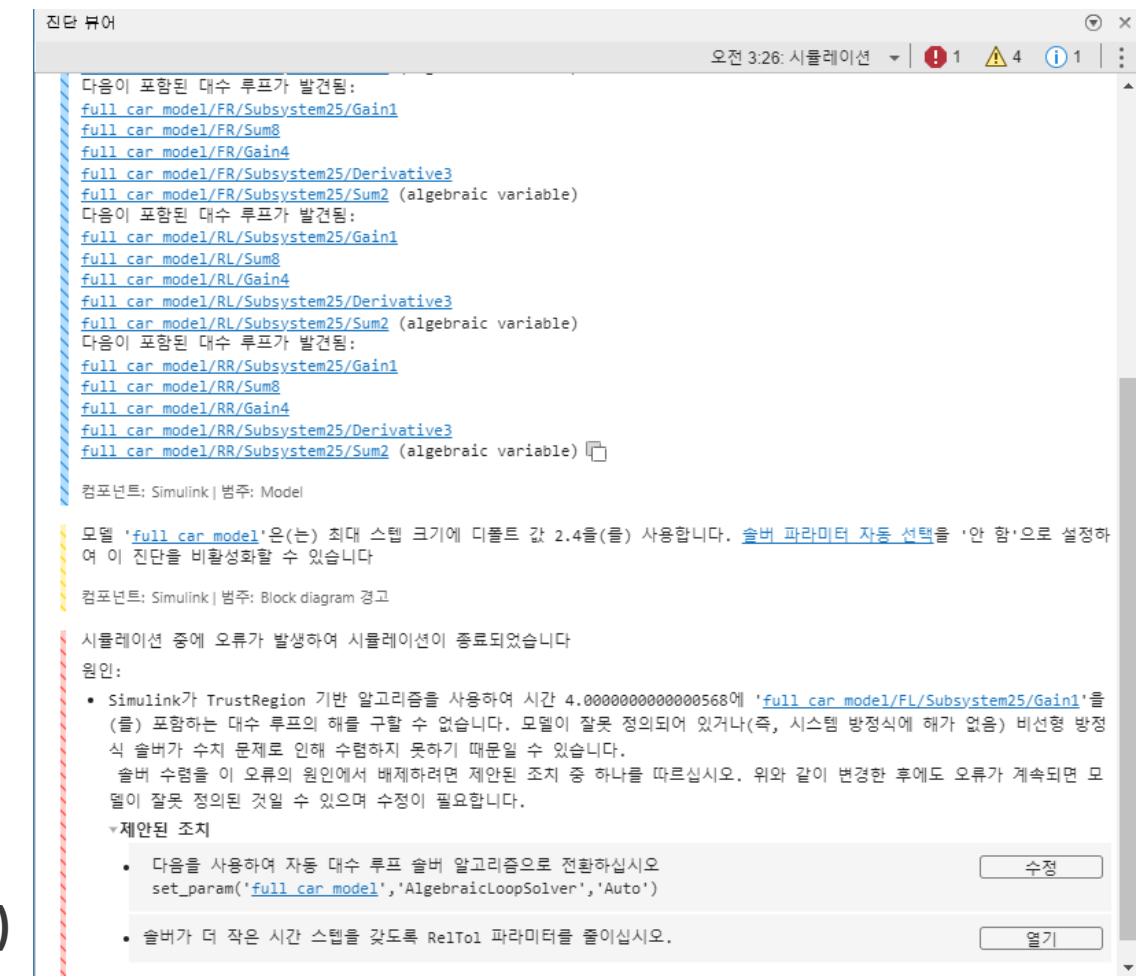


### 3. 대수 루프 주의 사항

입력과 출력에 동일한 변수를 사용할 때는 대수 루프가 발생할 가능성이 큽니다. 대수 루프는 다음과 같은 문제를 일으킬 수 있습니다:

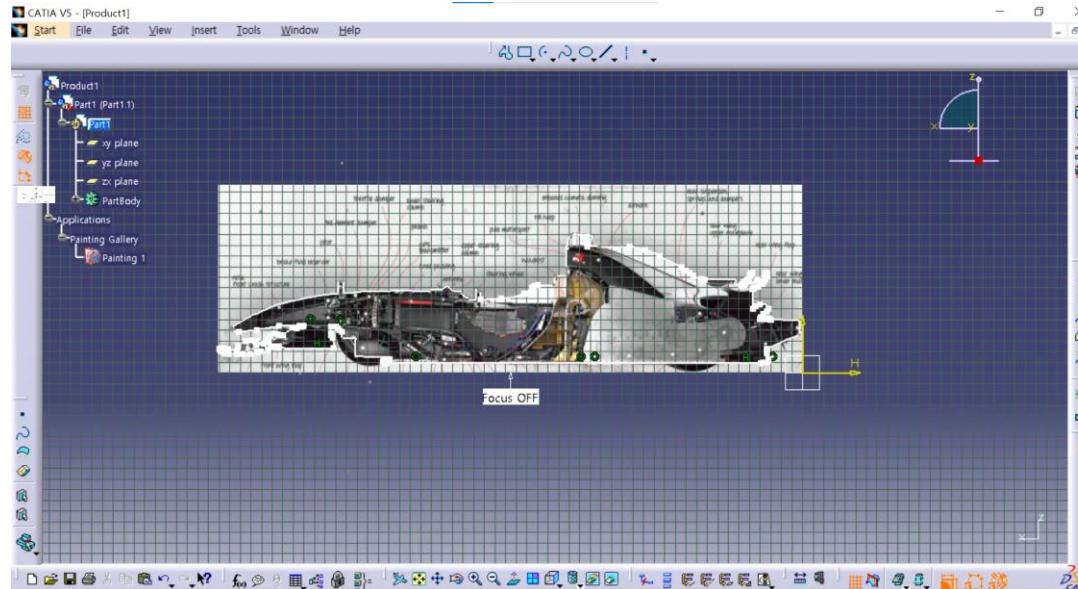
- 시스템의 상태나 변수가 순환적인 의존성을 가질 때, Simulink는 이를 해결할 방법을 찾지 못할 수 있습니다.
- 대수 루프를 해결하기 위해 Simulink는 특정 해결 방법을 사용하지만, 때때로 수치적으로 불안정할 수 있고, 이로 인해 시뮬레이션이 제대로 실행되지 않을 수 있습니다.

한 Subsystem의 input에 있는 변수를 output으로도 출력한다면  
(즉 output 값을 그대로 다시 input으로 사용한다면)  
순환적인 의존성으로 인해 수치적 불안정

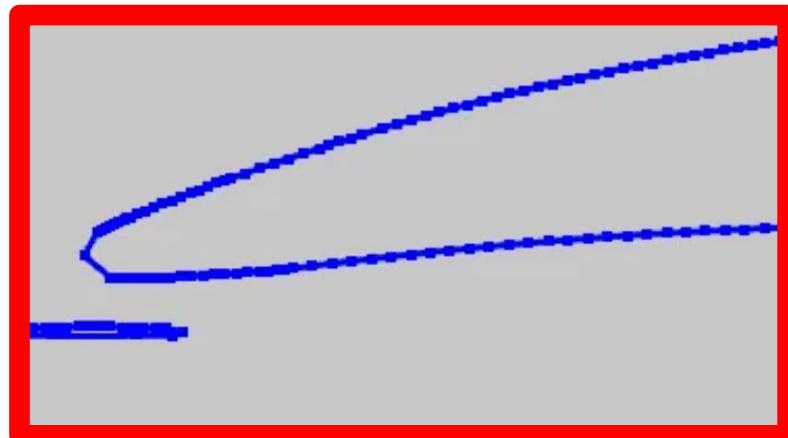


## 5

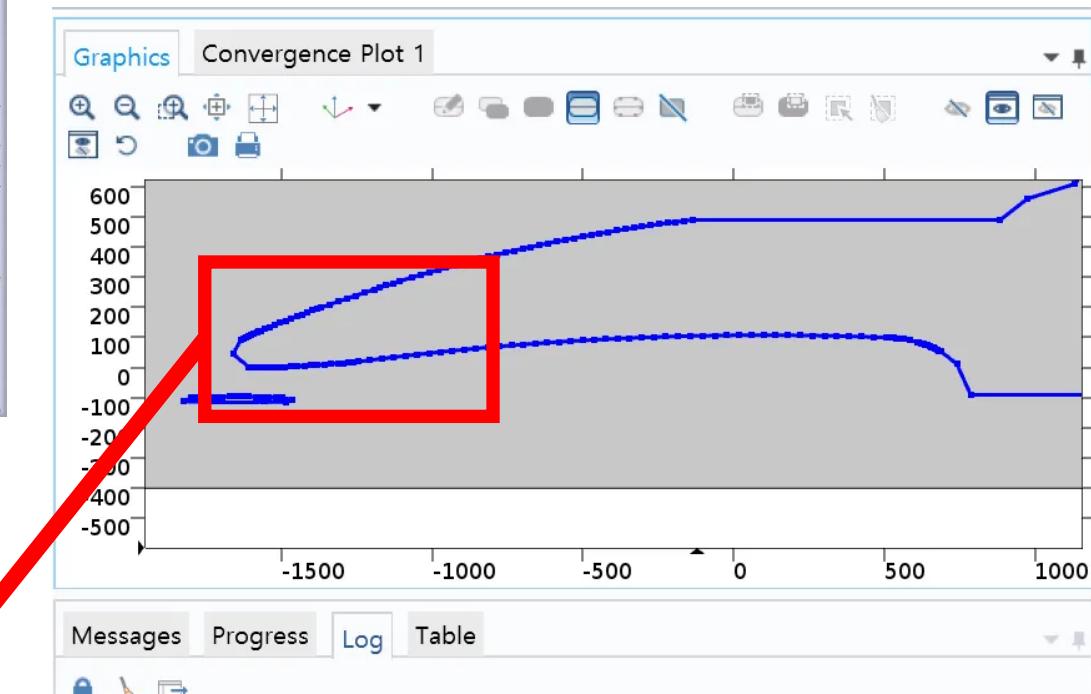
# Difficulties & Reflections – 2D 형상 모델링



<Catia>



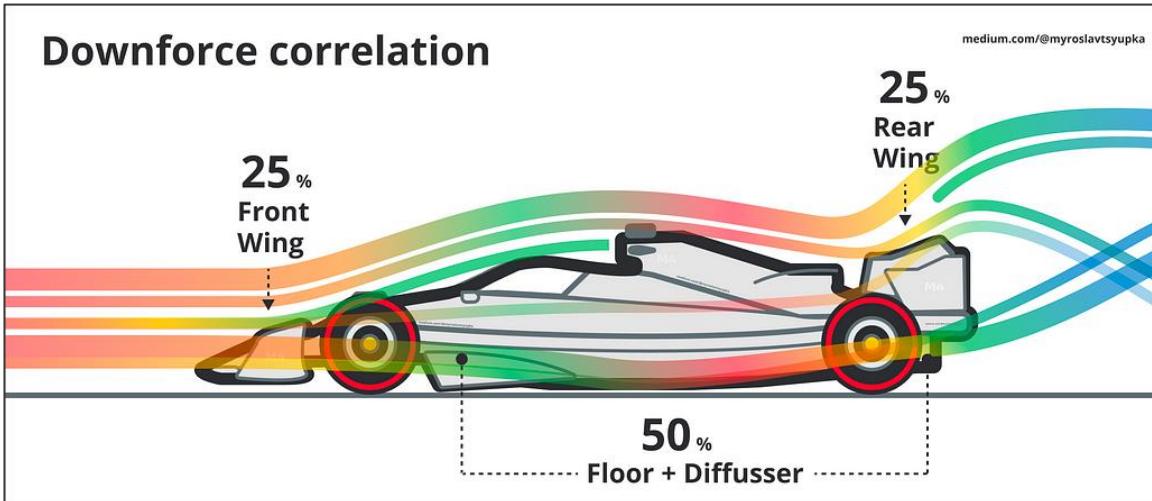
Import



<COMSOL>

## 5

# Difficulties & Reflections – COMSOL 결과의 타당성



Vehicle Speed (m/s)	Total Stress, x component(N/m)		Wing Stress, y component (N/m)	
Pitch Angle(degree)	50	100	50	100
0	-835.49	-3341.8	230.97	923.98
0.1°	-852.4	-3409.3	256.79	1027.1
-0.1°	-836.33	-3378.8	233.63	980.69
0.2°	-873.27	-3492.4	265	1061.2
-0.2°	-844.76	-3378.8	245.16	980.69
0.3°	-890.11	-3560.2	247.23	988.88
-0.3°	-844.93	-3379.6	239.07	956.28

$$\text{downforce} = \frac{1}{2\rho} AC_d v^2$$

## 5

## Difficulties & Reflections – etc.

- 타이어와 로드 간의 마찰계수와 차량 가속도 간의 관계를 구해 가속, 감속에 의한 **pitch** 현상을 동역학적으로 분석해보려 했으나 실패
- F1 차량처럼 고속으로 움직이는 물체에 대해서는 **laminar flow**가 아니라 **turbulent flow**가 더 적합  
→ COMSOL 기능에 제한이 있어서 더 정확한 시뮬레이션 불가



## CAE TEAM PROJECT

### F1 BANNED TECHNOLOGY

2020044466 이호연

2022091285 김지원

2020029107 송이찬

CAE : Computer Aided Engineering

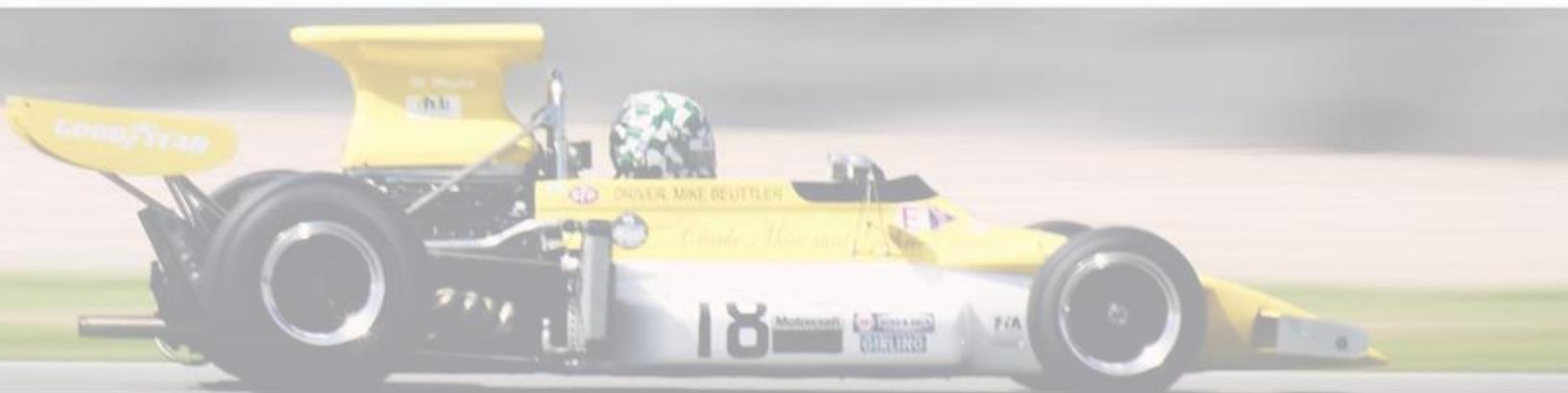
HYU Department of Automotive Engineering

Prof. Seungjae Min

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 <https://cdl.hanyang.ac.kr/education/aue3028-2024/>



# 감사합니다

Full-body Model (14 dof vehicle model)

 Full-body Model (14 dof vehicle model)

FRICS(Front to Rear Interconnected Suspension)

 FRICS(Front to Rear Interconnected Suspension)

Aerodynamics

 Aerodynamics

매스 댐퍼(Tuned mass damper)

 매스 댐퍼(Tuned mass damper)

DAS(Dual Axis Steering)

 DAS(Dual Axis Steering)

## PROJECT NOTION

<https://substantial-workshop-80b.notion.site/CAE-TEAM-PROJECT-5b6961eb4be743d2af1c7c0254bc6c77>